

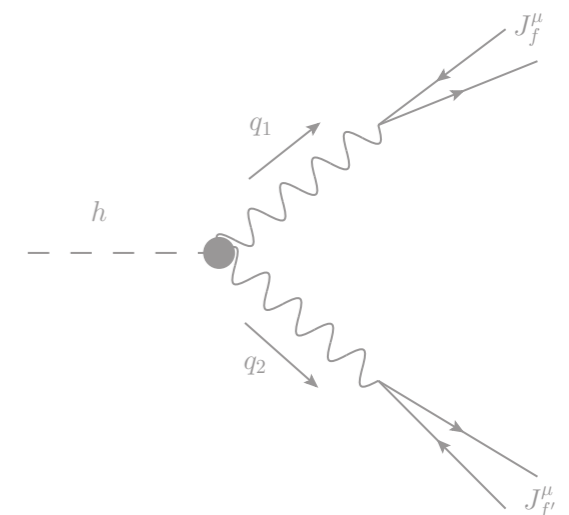
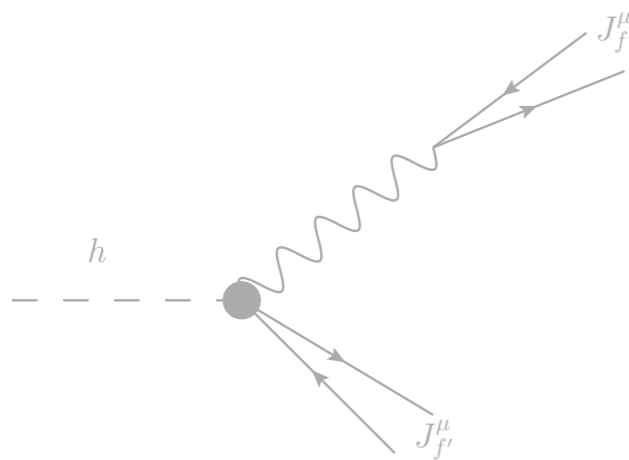
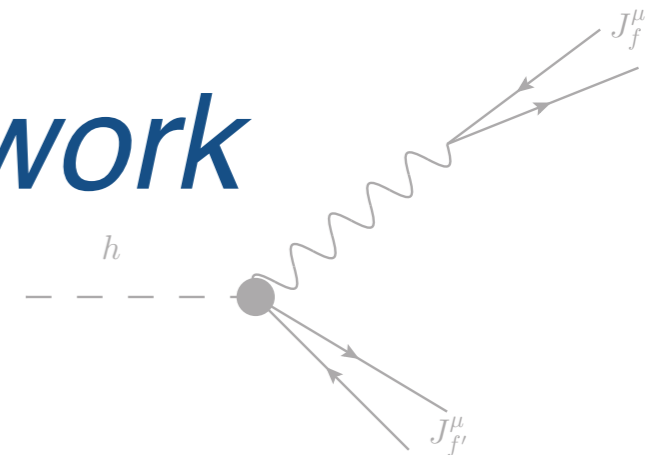
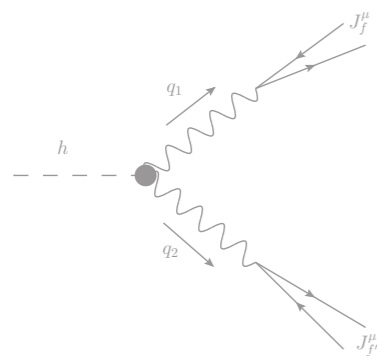
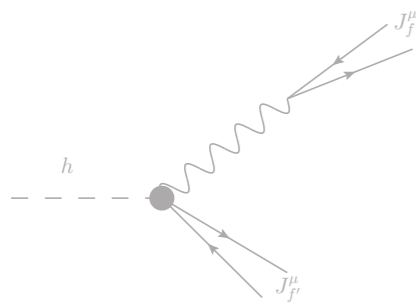
# Higgs PO

## *Production and decay beyond the kappa-framework*

David Marzocca



Universität  
Zürich<sup>UZH</sup>



*Particle Theory Seminar, UZH, 13/10/2015*

# Outline

- Motivation and introduction. What are **pseudo-observables (PO)**?
- **PO in Higgs Decay.**
- **PO in Electroweak Higgs Production.**
- **Linear EFT** and Higgs PO.

## Based on:

works with various subsets of

*{M. Bordone, A. Falkowski, M. Gonzalez-Alonso, A. Greljo, G. Isidori, J. Lindert, D.M., A. Pattori}*

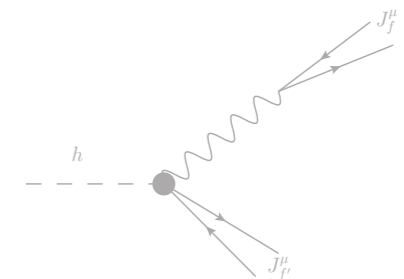
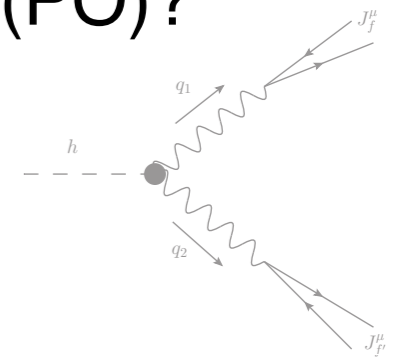
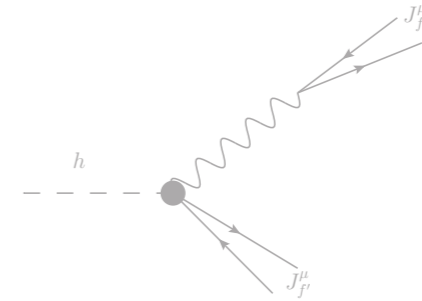
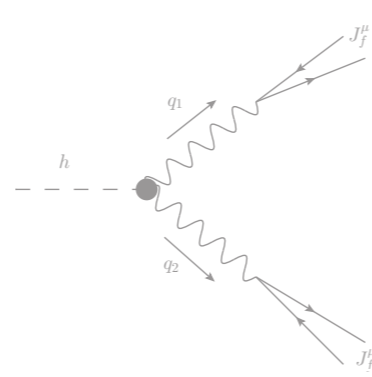
Eur. Phys. J. C75 (2015) 3, 128 arXiv: [1412.6038](https://arxiv.org/abs/1412.6038)

Eur. Phys. J. C75 (2015) 7, 341 arXiv: [1504.04018](https://arxiv.org/abs/1504.04018)

Eur. Phys. J. C75 (2015) 8, 385 arXiv: [1507.02555](https://arxiv.org/abs/1507.02555)

arXiv: [1508.00581](https://arxiv.org/abs/1508.00581)

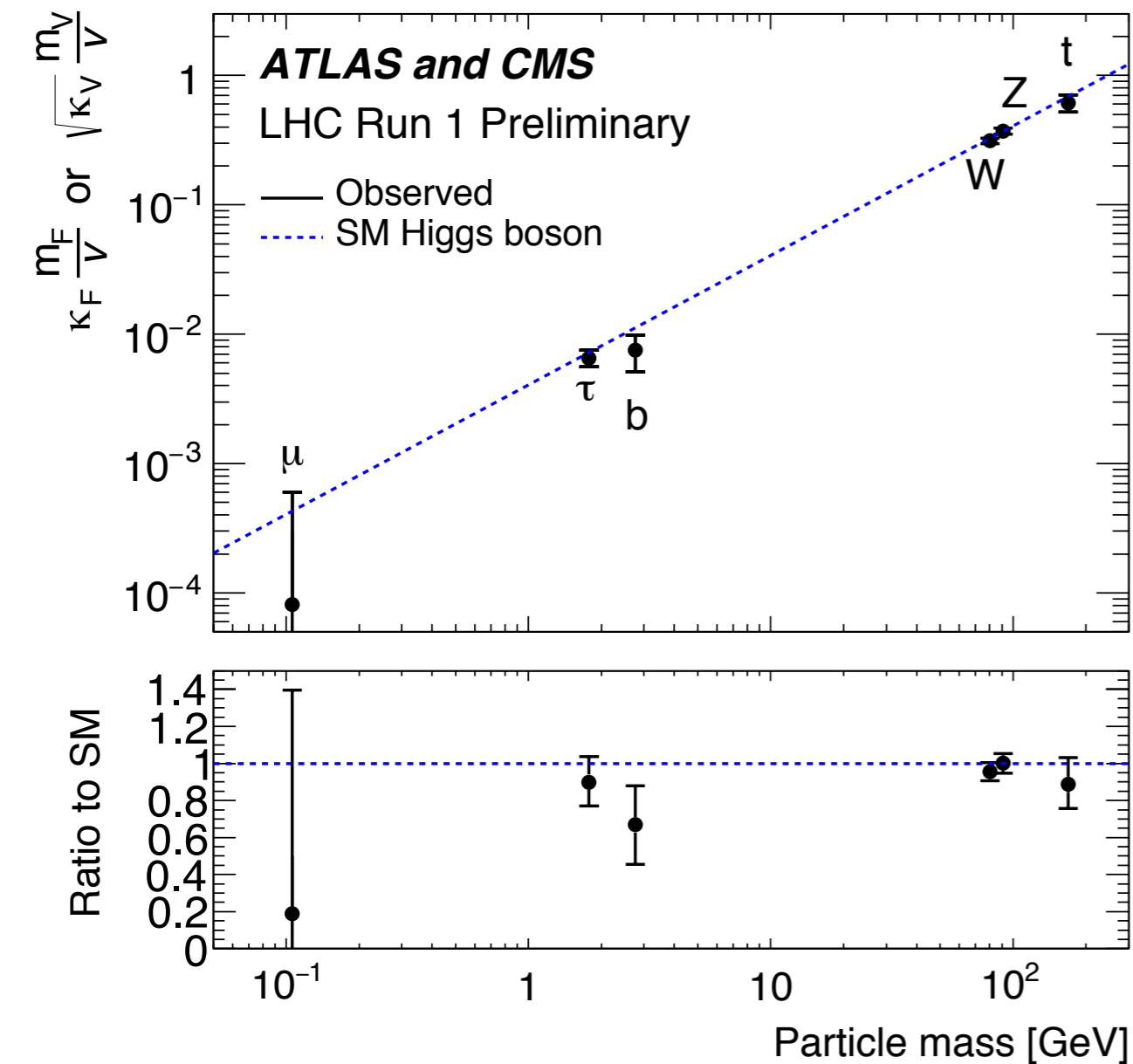
+ some work in progress



# Introduction: LHC Run-1 in one slide



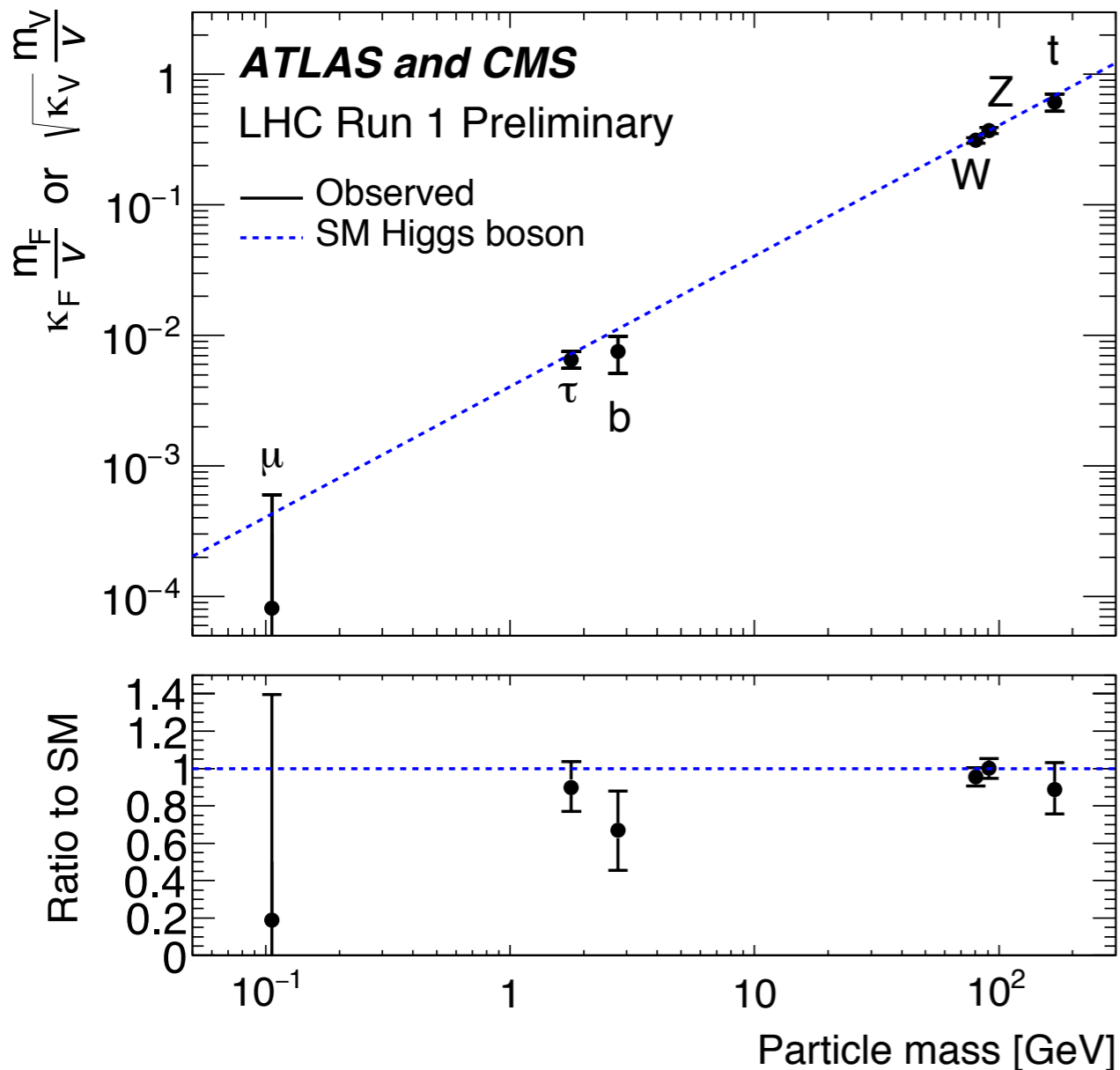
discovery of the Higgs and  
good measurement of many of its couplings.  
The **Standard Model** is complete.



# Introduction: LHC Run-1 in one slide



discovery of the Higgs and good measurement of many of its couplings. The **Standard Model** is complete.



So far, no compelling evidence of new physics from direct searches:  
Scale of New Physics is high

$$\Lambda_{NP} \gg m_h$$

## Questions we still have to find answers to:

Naturalness problem  
of the Higgs mass

WIMP Dark Matter

Flavour puzzle

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**Pragmatic goal:**  
Understand the physics at the TeV scale.

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Naturalness problem  
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**Pragmatic goal:**  
Understand the physics at the TeV scale.

### How we are doing this

- **Direct searches** of new particles: LHC, DM, ...
- **Precision** SM measurements: **Higgs**, **Electroweak**, Flavour, Neutrinos, ...
- **Cosmology**: CMB, Large Scale Structures, BBN, ...

**We do not know what the New Physics will be like.**  
**How to approach its search?**



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**How to approach its search?**

*Top-down approach*

Suitable for: **LHC direct searches**

Choose some **well motivated explicit model** and study its predictions.

**Pro:** very predictive

**Cons:** very model-dependent

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***Bottom-up approach***

Suitable for: **Precision measurements**

Work in a **well-defined framework** with the least possible number of assumptions, in order to cover as many new physics scenarios as possible.

**Pro:** model-independent

**Cons:** less predictive

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***Generality* × *Predictivity* ~ const.**

***Bottom-up approach***

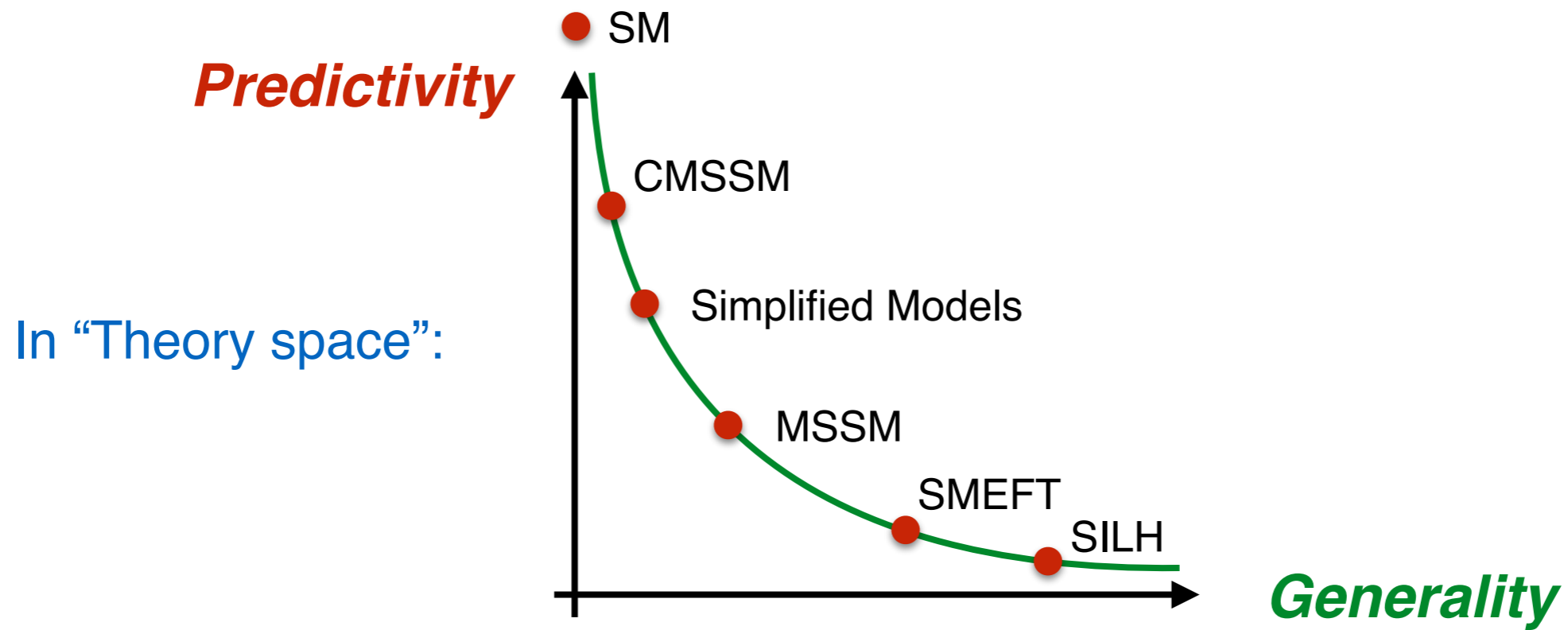
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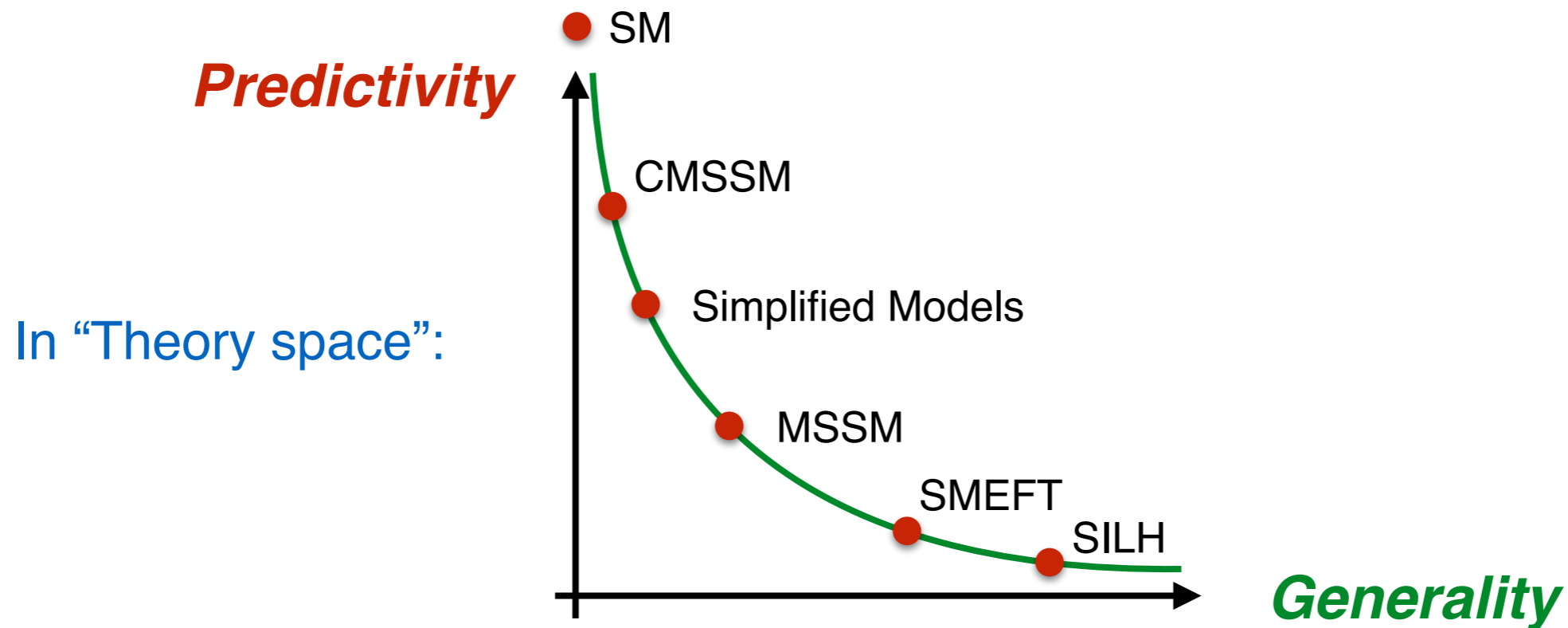
**Pro:** model-independent

**Cons:** less predictive

$$\text{Generality} \times \text{Predictivity} \sim \text{const.}$$



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## LHC - Higgs Legacy

How to **collect all available information** on a the Higgs,  
in the **most general** and **theoretically unbiased** way?

We want to be able to come back to LHC Higgs data in the future and still be able to reinterpret it in terms of any New Physics model which would have been discovered.

It will be extremely difficult to be able to repeat many experimental analysis.

# How should the experiments present their result

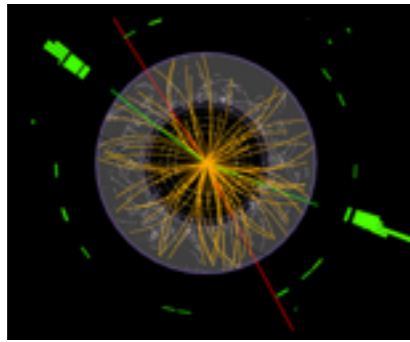
***Generality***



***Predictivity***

**Generality**

**How should the experiments present their result**



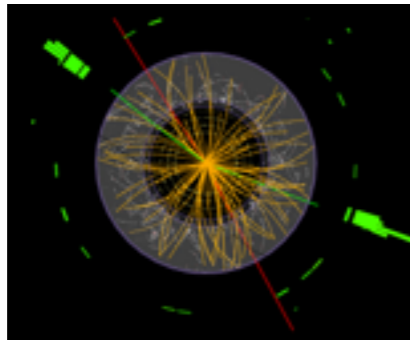
## **Physical observables**

*Fiducial cross sections,  
Number of events in a given bin, etc ...*

**Predictivity**

**Generality**

How should the experiments present their result



## Physical observables

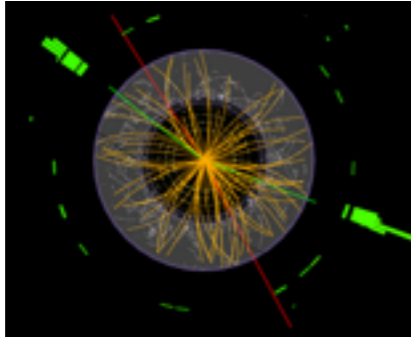
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ALL the observables??

Difficult for theorists to control experimental effects.

**Predictivity**





**Physical observables**

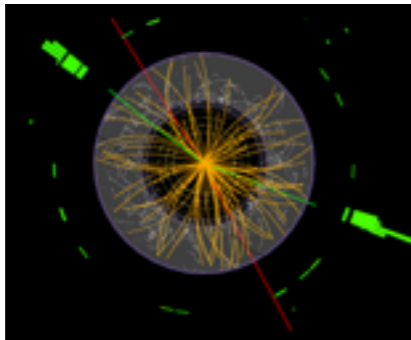
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$$\begin{aligned} \mathcal{L} = & -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} \\ & + i\bar{\psi}\not{D}\psi + h.c. \\ & + \bar{\psi}_i y_{ij} \psi_j \phi + h.c. \\ & + \frac{1}{2} \partial_\mu \phi^2 - V(\phi) \end{aligned}$$

**Lagrangian parameters**

*Couplings, running masses,  
Wilson coefficients, etc ...*



### Physical observables

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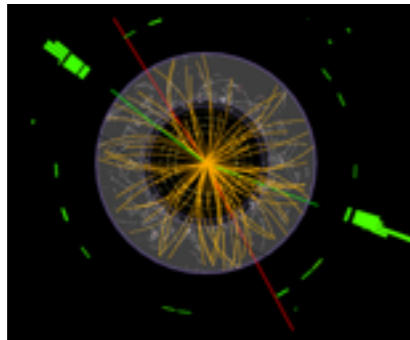
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### Lagrangian parameters

*Couplings, running masses,  
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Which model?  
Which parameters?  
Fit at LO, NLO..?



### Physical observables

*Fiducial cross sections,  
Number of events in a given bin, etc ...*

ALL the observables??  
Difficult for theorists to control experimental effects.



### Pseudo-observables

*Pole masses, decay widths,  
kappas, form factors, etc ...*

$$\begin{aligned} \mathcal{L} = & -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} \\ & + i\bar{\psi}\not{D}\psi + h.c. \\ & + \bar{\psi}_i y_{ij} \psi_j \phi + h.c. \\ & + \frac{1}{2} D_\mu \phi^\dagger D^\mu \phi - V(\phi) \end{aligned}$$

### Lagrangian parameters

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Which model?  
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# Experimental data

Experiments



Theorists



Unfolding of **collider** &  
**soft radiation** effects

**PO**

**idealized observables**,  
well defined (in **QFT**) **quantities**.



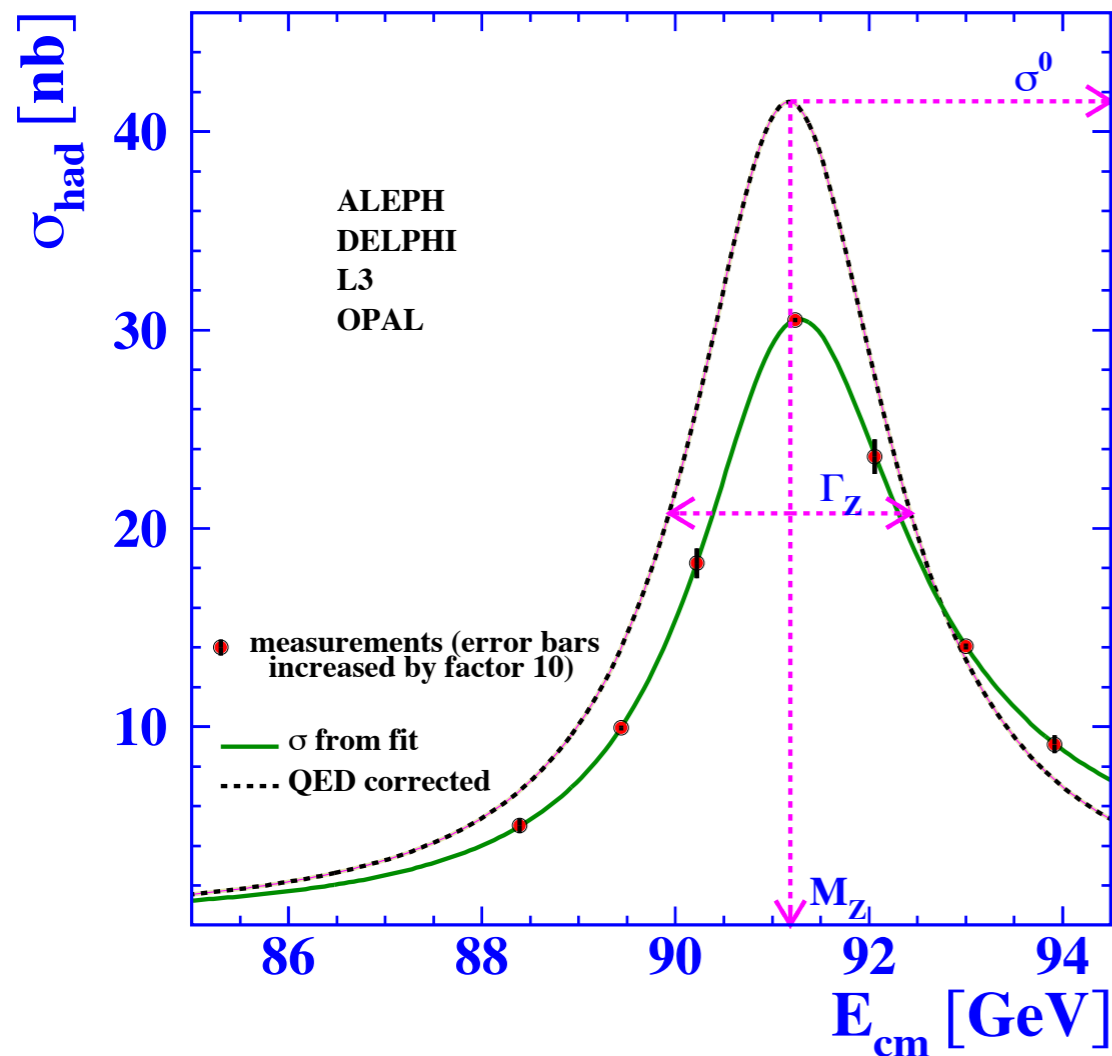
**Matching** to a given model  
at given order in pert. theory

**Constraints/measurements on theories**

# LEP-1 Strategy: on-shell Z decays

[hep-ex/0509008; Bardin, Grunewald, Passarino '99]

The goal was to parametrise on-shell Z decays as much model-independently as possible.



1) Unfold QED (and/or QCD) soft radiation effect

$$\sigma(s) = \int_{4m_f^2/s}^1 dz H_{\text{QED}}^{\text{tot}}(z, s) \sigma_{\text{ew}}(zs).$$

2) Parametrize the shape with some PO defined at amplitude level:

$$m_Z, \Gamma_Z$$

Lineshape

$$\chi(s) = \frac{G_F m_Z^2}{8\pi\sqrt{2}} \frac{s}{s - m_Z^2 + is\Gamma_Z/m_Z}$$

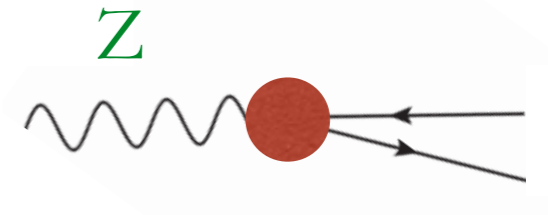
3) Fit the PO from data

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Parametrise the on-shell  $Z \bar{f} f$  vertex as  $\gamma_\mu (\mathcal{G}_V^f + \mathcal{G}_A^f \gamma_5)$



The PO are defined as

$$g_V^f = \text{Re } \mathcal{G}_V^f, \quad g_A^f = \text{Re } \mathcal{G}_A^f$$

To be model-independent it is important to work with on-shell initial and final states.

$$\Gamma_{f\bar{f}} = N_c^f \frac{G_F m_Z^3}{6\sqrt{2}\pi} \left( |\mathcal{G}_{Af}|^2 R_{Af} + |\mathcal{G}_{Vf}|^2 R_{Vf} \right) + \Delta_{\text{ew/QCD}}$$

Radiators: final state radiation

non-factorizable SM corrections, very small.

## PO used at Run 1: the $\kappa$ -framework

At **Run-1**, measurements of Higgs properties were reported in the  $\kappa$ -framework:

Narrow width approximation (& on-shell Higgs):

$$\sigma(ii \rightarrow \mathbf{h} + \mathbf{X}) \times \text{BR}(\mathbf{h} \rightarrow ff) = \sigma_{ii} \frac{\Gamma_{ff}}{\Gamma_{\mathbf{h}}} = \frac{\kappa_{ii}^2 \kappa_{ff}^2}{\kappa_{\mathbf{h}}^2} \sigma_{\text{SM}} \times \text{BR}_{\text{SM}}$$

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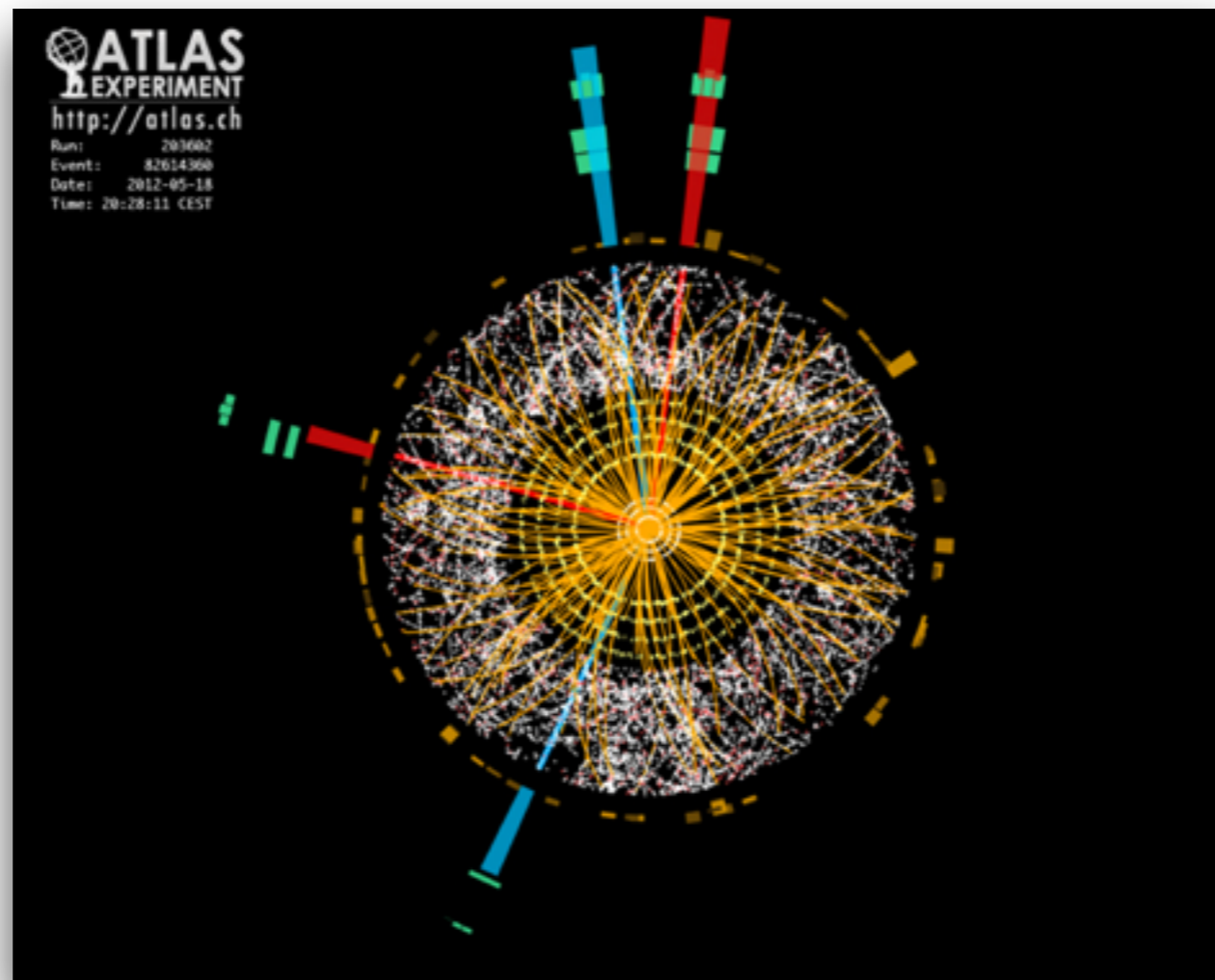
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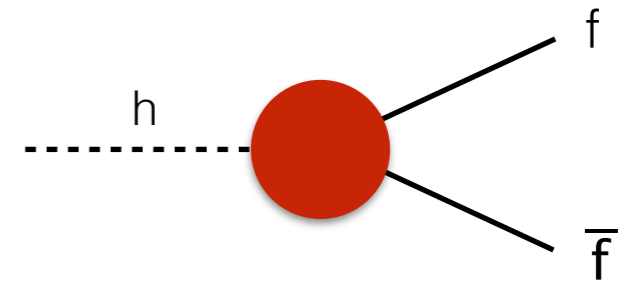
Need to extend the  $\kappa$ -framework retaining all its good properties:

**Higgs pseudo-observables**

# Pseudo observables in Higgs Decays



# Higgs decays to two fermions



The kinematic is fixed.

No polarisation information is retained.

(maybe possible to measure in  $\tau\tau$  channel)

the **total rate** is all that can be extracted from data

“Effective coupling” PO:

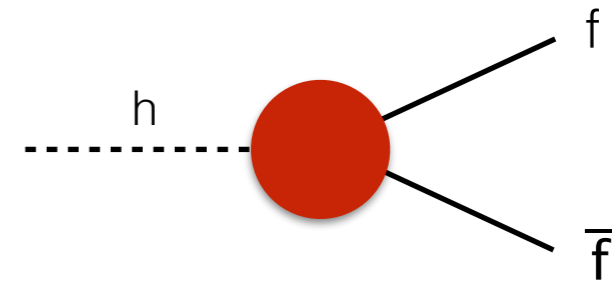
$$\mathcal{A}(h \rightarrow f \bar{f}) = -i \frac{y_{\text{eff}}^{f, \text{SM}}}{\sqrt{2}} \bar{f} (\kappa_f + i \lambda_f^{\text{CP}} \gamma_5) f$$

In the SM  $\kappa_X \rightarrow 1$ ,  $\lambda_X^{\text{CP}} \rightarrow 0$

“Physical” PO:

$$\Gamma(h \rightarrow f \bar{f})_{(\text{incl})} = [\kappa_f^2 + (\lambda_f^{\text{CP}})^2] \Gamma(h \rightarrow f \bar{f})_{(\text{incl})}^{(\text{SM})}$$

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$y_{\text{eff}}^{f,\text{SM}}$

from best SM prediction:

$$\Gamma(h \rightarrow f \bar{f})_{(\text{incl})}^{(\text{SM})} = N_c^f \frac{|y_{\text{eff}}^{f,\text{SM}}|^2}{16\pi} m_H$$

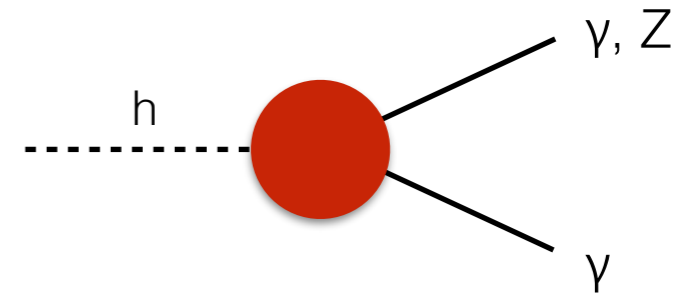


YR2

|                                      | $\bar{b}b$            | $\bar{\tau}\tau$      |
|--------------------------------------|-----------------------|-----------------------|
| $\text{Br}(h \rightarrow f \bar{f})$ | $5.77 \times 10^{-1}$ | $6.32 \times 10^{-2}$ |
| $ y_{\text{eff}}^{f,\text{SM}} $     | $1.77 \times 10^{-2}$ | $1.02 \times 10^{-2}$ |
|                                      | $\bar{c}c$            | $\bar{\mu}\mu$        |
| $\text{Br}(h \rightarrow f \bar{f})$ | $2.91 \times 10^{-2}$ | $2.19 \times 10^{-4}$ |
| $ y_{\text{eff}}^{f,\text{SM}} $     | $3.98 \times 10^{-3}$ | $5.99 \times 10^{-4}$ |

<https://twiki.cern.ch/twiki/bin/view/LHCPhysics/CERNYellowReportPageBR>

# Higgs decays to $\gamma\gamma$ and $Z\gamma$ (on-shell)



“Effective coupling” PO:

$$\mathcal{A} [h \rightarrow \gamma(q, \epsilon)\gamma(q', \epsilon')] = i \frac{2 \epsilon_{\gamma\gamma}^{\text{SM,eff}}}{v_F} \epsilon'_\mu \epsilon_\nu [\kappa_{\gamma\gamma} (g^{\mu\nu} q \cdot q' - q^\mu q'^\nu) + \lambda_{\gamma\gamma}^{\text{CP}} \epsilon^{\mu\nu\rho\sigma} q_\rho q'_\sigma]$$

$$\mathcal{A} [h \rightarrow Z(q, \epsilon)\gamma(q', \epsilon')] = i \frac{2 \epsilon_{Z\gamma}^{\text{SM,eff}}}{v_F} \epsilon'_\mu \epsilon_\nu [\kappa_{Z\gamma} (g^{\mu\nu} q \cdot q' - q^\mu q'^\nu) + \lambda_{Z\gamma}^{\text{CP}} \epsilon^{\mu\nu\rho\sigma} q_\rho q'_\sigma]$$

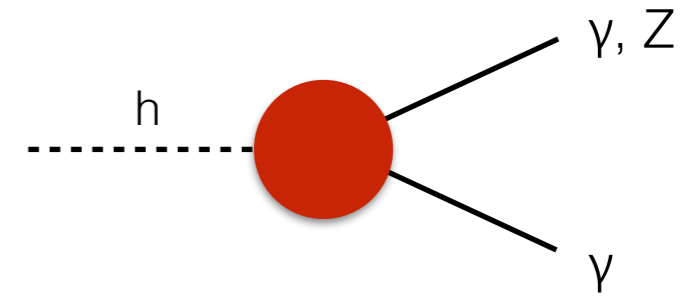
In the SM  $\kappa_X \rightarrow 1, \lambda_X^{\text{CP}} \rightarrow 0$

“Physical” PO:

$$\Gamma(h \rightarrow \gamma\gamma) = [\kappa_{\gamma\gamma}^2 + (\lambda_{\gamma\gamma}^{\text{CP}})^2] \Gamma(h \rightarrow \gamma\gamma)^{(\text{SM})}$$

$$\Gamma(h \rightarrow Z\gamma) = [\kappa_{Z\gamma}^2 + (\lambda_{Z\gamma}^{\text{CP}})^2] \Gamma(h \rightarrow Z\gamma)^{(\text{SM})}$$

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$$\mathcal{A} [h \rightarrow Z(q, \epsilon)\gamma(q', \epsilon')] = i \frac{2 \epsilon_{Z\gamma}^{\text{SM,eff}}}{v_F} \epsilon'_\mu \epsilon_\nu [\kappa_{Z\gamma} (g^{\mu\nu} q \cdot q' - q^\mu q'^\nu) + \lambda_{Z\gamma}^{\text{CP}} \epsilon^{\mu\nu\rho\sigma} q_\rho q'_\sigma]$$

In the SM  $\kappa_X \rightarrow 1, \lambda_X^{\text{CP}} \rightarrow 0$

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$$\Gamma(h \rightarrow Z\gamma) = [\kappa_{Z\gamma}^2 + (\lambda_{Z\gamma}^{\text{CP}})^2] \Gamma(h \rightarrow Z\gamma)^{\text{(SM)}}$$

$\epsilon_X^{\text{SM,eff}}$  from best SM prediction:

$$\Gamma(h \rightarrow \gamma\gamma)^{\text{(SM)}} = \frac{|\epsilon_{\gamma\gamma}^{\text{SM,eff}}|^2}{16\pi} \frac{m_H^3}{v_F^2},$$

$$\Gamma(h \rightarrow Z\gamma)^{\text{(SM)}} = \frac{|\epsilon_{Z\gamma}^{\text{SM,eff}}|^2}{8\pi} \frac{m_H^3}{v^2} \left(1 - \frac{m_Z^2}{m_H^2}\right)^3$$

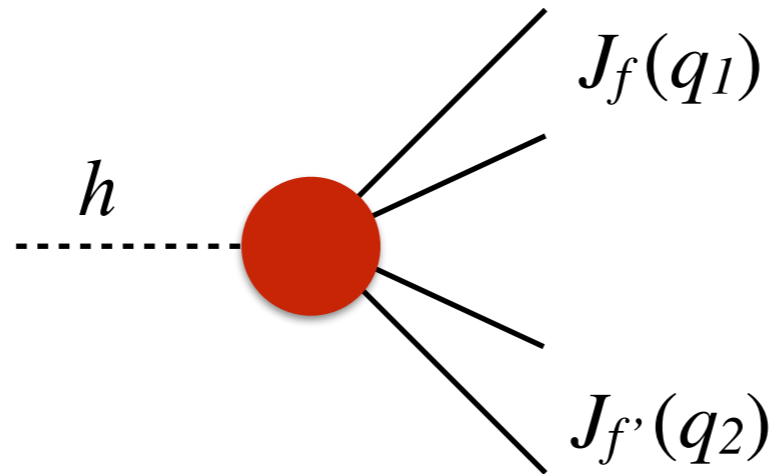


| $VV$                            | $\gamma\gamma$        | $Z\gamma$             |
|---------------------------------|-----------------------|-----------------------|
| $\text{Br}(h \rightarrow VV)$   | $2.28 \times 10^{-3}$ | $1.54 \times 10^{-3}$ |
| $\epsilon_{VV}^{\text{SM,eff}}$ | $3.8 \times 10^{-3}$  | $6.9 \times 10^{-3}$  |

<https://twiki.cern.ch/twiki/bin/view/LHCPhysics/CERNYellowReportPageBR>

# Higgs to 4-fermion decays

Four-body decays  
 $h \rightarrow 4f$



The kinematics is much richer:  
 kinematical distributions.

**Assumption:** Neglect helicity-violating interactions,  
 naturally suppressed by  $m_f$  also in BSM.

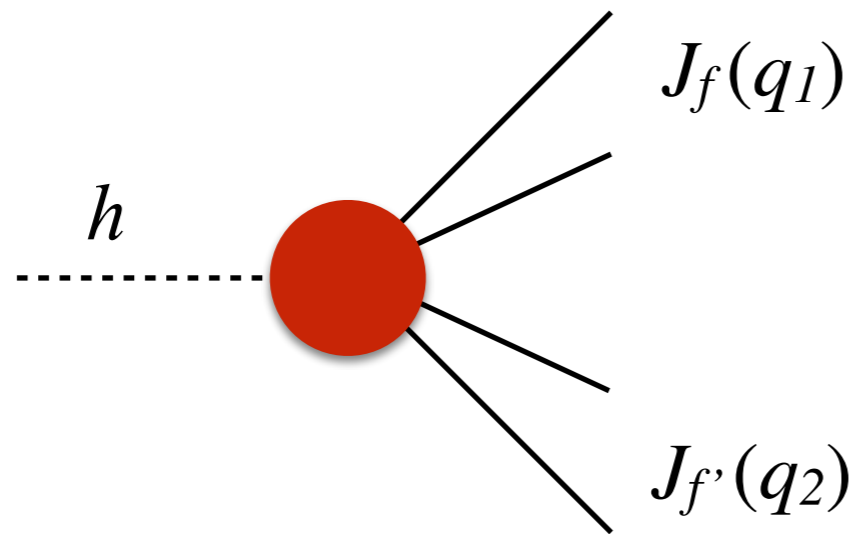
e.g.:  
 $h \rightarrow e_R e_L \mu_L \mu_R \propto y_e y_\mu$

The process is **completely described by this Green function** of **ON-SHELL** states:

$$\langle 0 | \mathcal{T} \{ J_f^\mu(x), J_{f'}^\nu(y), h(0) \} | 0 \rangle, \quad J_f^\mu(x) = \bar{f}(x) \gamma^\mu f(x)$$



# Higgs to 4-fermion decays



$$\langle 0 | \mathcal{T} \{ J_f^\mu(x), J_{f'}^\nu(y), h(0) \} | 0 \rangle$$

Only 3 tensor structures allowed by Lorentz symmetry:

Example:  $h \rightarrow e^+e^- \mu^+\mu^-$

$$\mathcal{A} = i \frac{2m_Z^2}{v_F} (\bar{e}\gamma_\alpha e)(\bar{\mu}\gamma_\beta \mu) \times \left[ F_1^{e\mu}(q_1^2, q_2^2) g^{\alpha\beta} + F_3^{e\mu}(q_1^2, q_2^2) \frac{q_1 \cdot q_2 g^{\alpha\beta} - q_2^\alpha q_1^\beta}{m_Z^2} + F_4^{e\mu}(q_1^2, q_2^2) \frac{\epsilon^{\alpha\beta\rho\sigma} q_{2\rho} q_{1\sigma}}{m_Z^2} \right]$$

*Longitudinal*

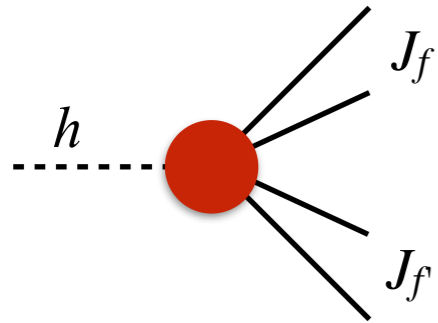
*Transverse*

*CP-odd*

**General approach: measure the double differential distribution in  $(q_1^2, q_2^2)$**

# Higgs to 4-fermion decays

$$\langle 0 | \mathcal{T} \{ J_f^\mu(x), J_{f'}^\nu(y), h(0) \} | 0 \rangle$$



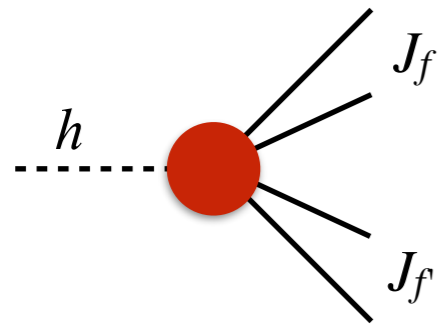
includes

Long-distance (non-local) modes (poles):  
propagation of EW gauge bosons.

Short-distance modes:  
contact terms,  $x$  and/or  $y \rightarrow 0$

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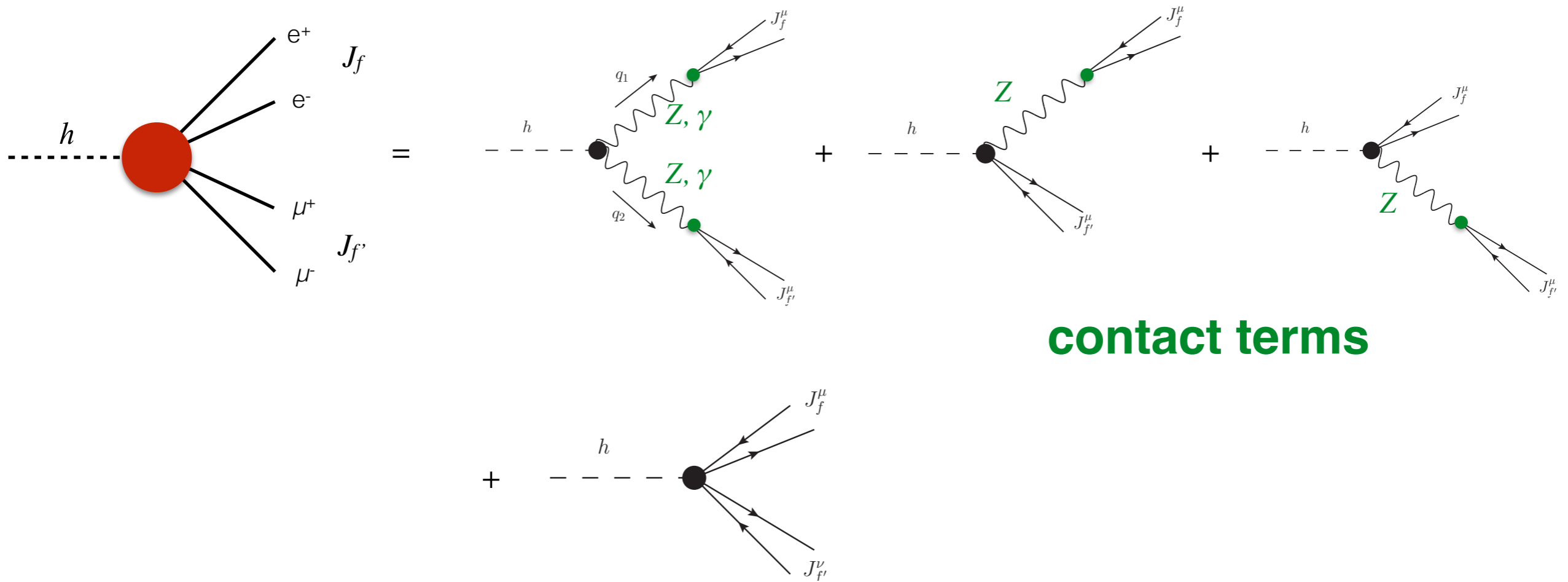


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We expand around the physical poles:



# Higgs to 4-fermion decays

$$\langle 0 | \mathcal{T} \{ J_f^\mu \}$$

**Assumption:**

(To truncate the expansion)

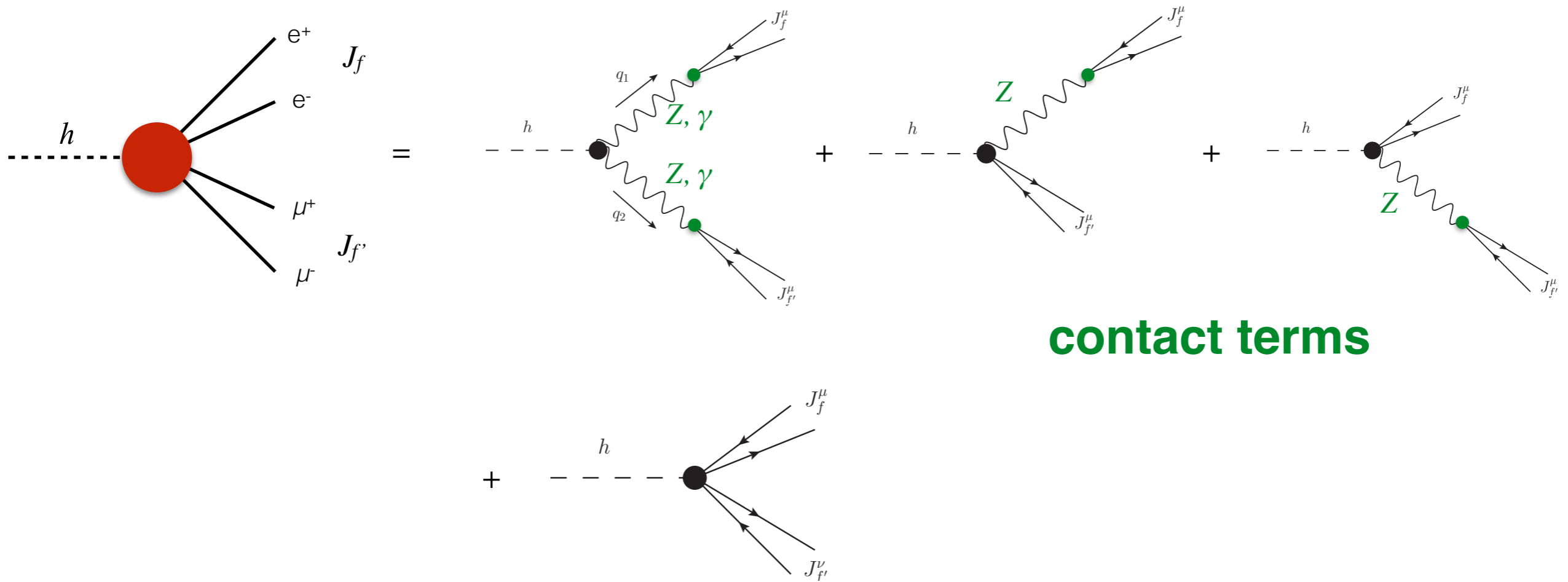
(poles):

No new light state can mediate this amplitude.

New Physics scale  $>$  Higgs mass scale

$h$

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# Higgs to 4-fermion decays

$$\langle 0 | \mathcal{T} \{ J_f^\mu \}$$

**Assumption:**

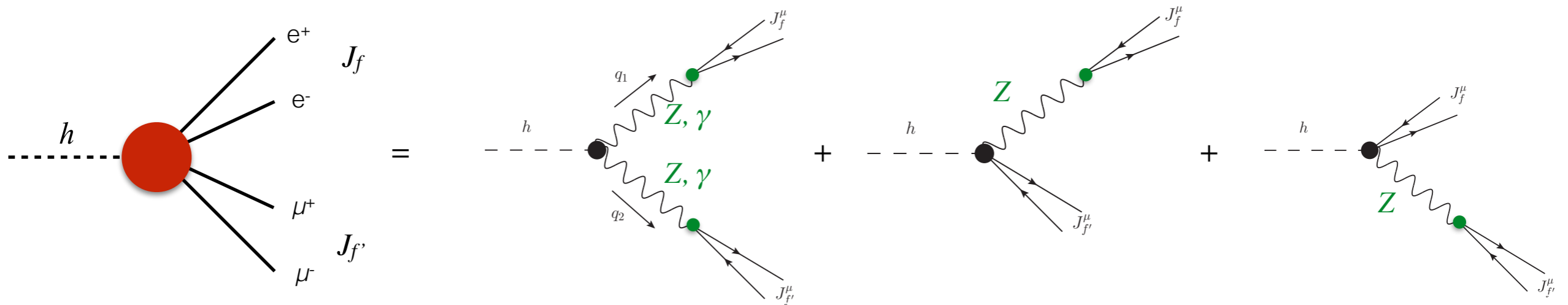
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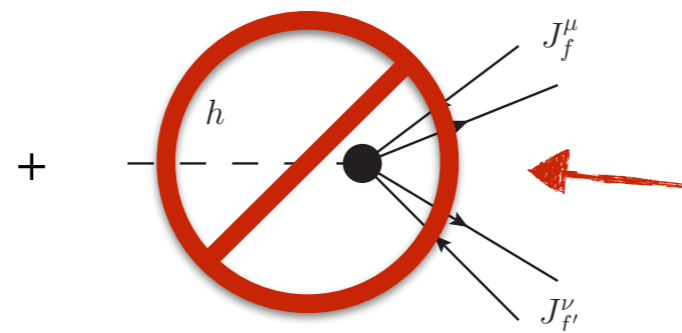
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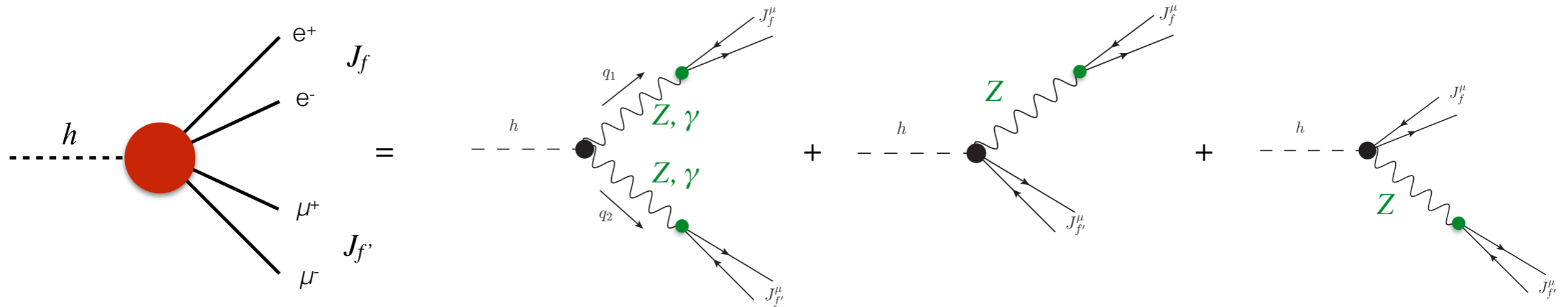
**contact terms**



We neglect completely local terms, corresponding to operators with  $d > 6$ : **EFT assumption.**

$$\mathcal{O}(x) = h(x) \bar{e}(x) \gamma_\mu e(x) \bar{\mu}(x) \gamma^\mu \mu(x)$$

The **Higgs PO** are defined from the **residues** on the **physical poles**.



$$e = e_L, e_R, \quad \mu = \mu_L, \mu_R$$

$$\mathcal{A} = i \frac{2m_Z^2}{v_F} (\bar{e} \gamma_\alpha e) (\bar{\mu} \gamma_\beta \mu) \times \left[ \left( \kappa_{ZZ} \frac{g_Z^e g_Z^\mu}{P_Z(q_1^2) P_Z(q_2^2)} + \frac{\epsilon_{Ze}}{m_Z^2} \frac{g_Z^\mu}{P_Z(q_2^2)} + \frac{\epsilon_{Z\mu}}{m_Z^2} \frac{g_Z^e}{P_Z(q_1^2)} + \Delta_1^{\text{SM}}(q_1^2, q_2^2) \right) g^{\alpha\beta} + \right.$$

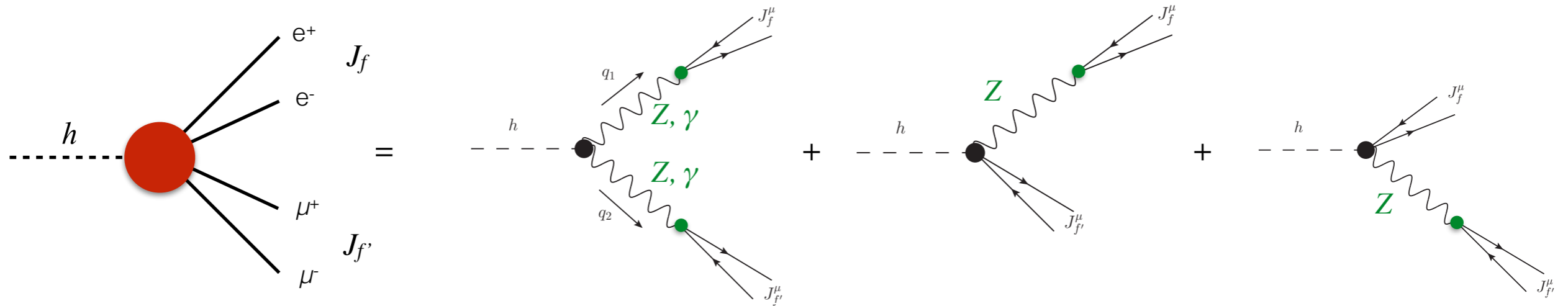
In the SM  $\kappa_X \rightarrow 1, \epsilon_X \rightarrow 0$

$$P_Z(q^2) = q^2 - m_Z^2 + im_Z \Gamma_Z$$

$$\epsilon_{\gamma\gamma}^{\text{SM-1L}} \simeq 3.8 \times 10^{-3},$$

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$$\left. + \left( \epsilon_{ZZ} \frac{g_Z^e g_Z^\mu}{P_Z(q_1^2) P_Z(q_2^2)} + \kappa_{Z\gamma} \epsilon_{Z\gamma}^{\text{SM-1L}} \left( \frac{e Q_\mu g_Z^e}{q_2^2 P_Z(q_1^2)} + \frac{e Q_e g_Z^\mu}{q_1^2 P_Z(q_2^2)} \right) + \kappa_{\gamma\gamma} \epsilon_{\gamma\gamma}^{\text{SM-1L}} \frac{e^2 Q_e Q_\mu}{q_1^2 q_2^2} + \Delta_3^{\text{SM}}(q_1^2, q_2^2) \right) \times \right.$$

$$\left. \times \frac{q_1 \cdot q_2 g^{\alpha\beta} - q_2^\alpha q_1^\beta}{m_Z^2} + \right.$$

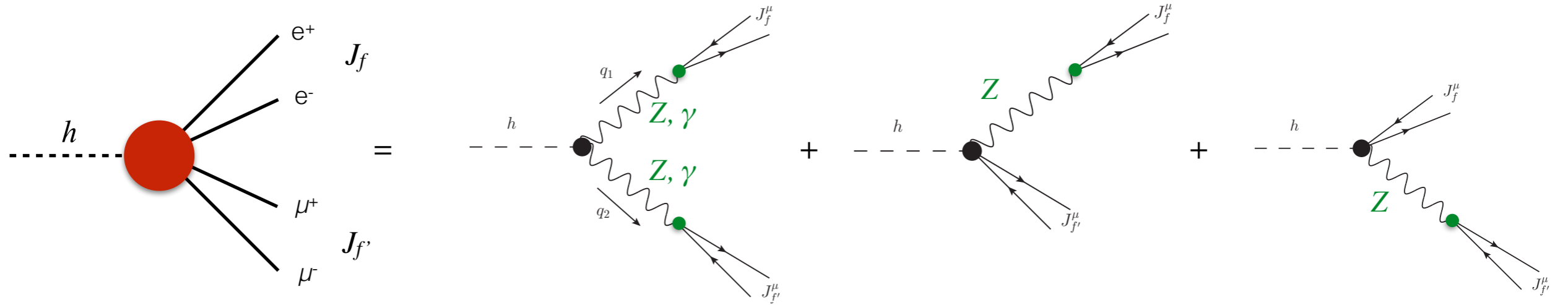
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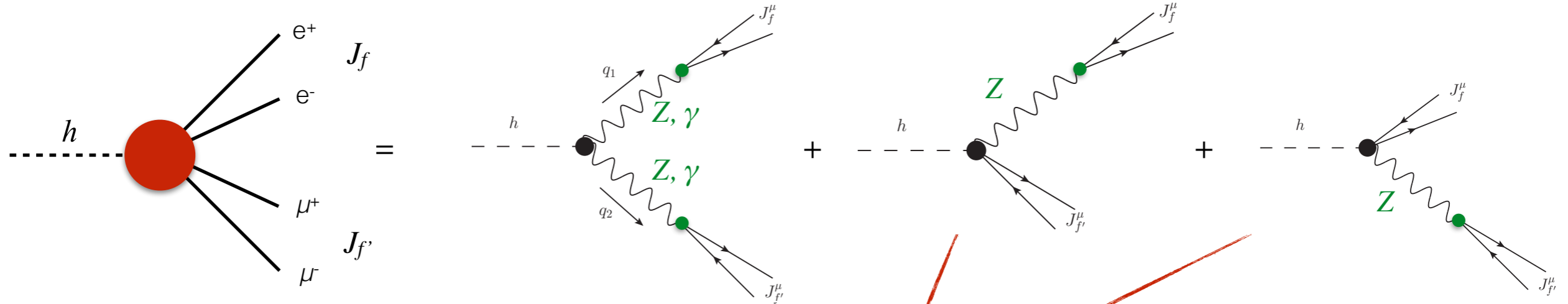
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$$e = e_L, e_R, \quad \mu = \mu_L, \mu_R$$

**contact terms**  
only source of  
flavor dependence

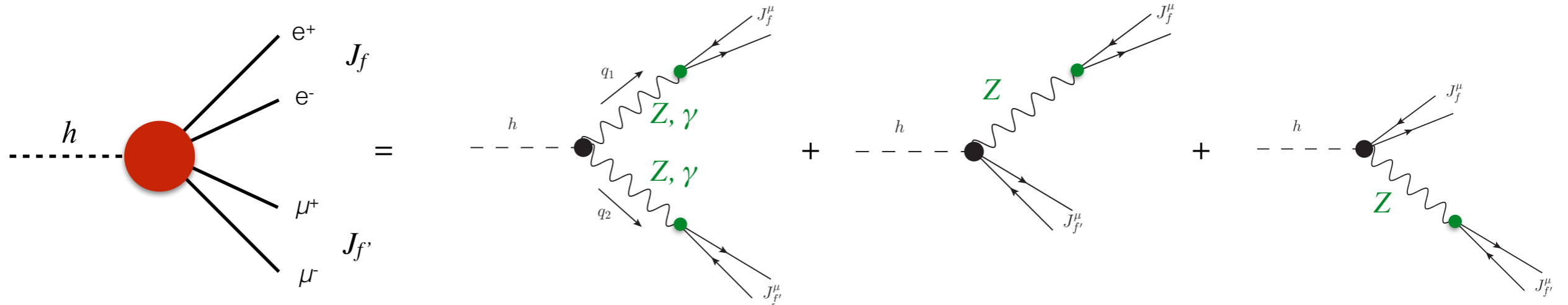
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The **Higgs PO** are defined from the **residues** on the **physical poles**.



$e = e_L, e_R, \quad \mu = \mu_L, \mu_R$

**Z-pole PO**

**non-local NLO SM contribution**

(very small)

As measured at LEP-I

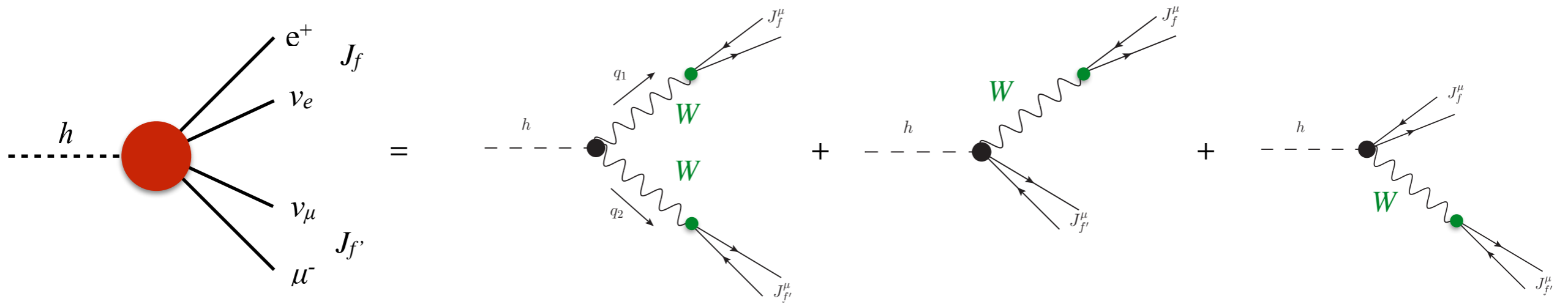
$$\begin{aligned}
 \mathcal{A} = & i \frac{2m_Z^2}{v_F} (\bar{e} \gamma_\alpha e) (\bar{\mu} \gamma_\beta \mu) \times \\
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 & + \left( \epsilon_{ZZ} \frac{g_Z^e g_Z^\mu}{P_Z(q_1^2) P_Z(q_2^2)} + \kappa_{Z\gamma} \epsilon_{Z\gamma}^{\text{SM-1L}} \left( \frac{e Q_\mu g_Z^e}{q_2^2 P_Z(q_1^2)} + \frac{e Q_e g_Z^\mu}{q_1^2 P_Z(q_2^2)} \right) + \kappa_{\gamma\gamma} \epsilon_{\gamma\gamma}^{\text{SM-1L}} \frac{e^2 Q_e Q_\mu}{q_1^2 q_2^2} + \Delta_3^{\text{SM}}(q_1^2, q_2^2) \right) \times \\
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 & \left. + \left( \epsilon_{ZZ}^{\text{CP}} \frac{g_Z^e g_Z^\mu}{P_Z(q_1^2) P_Z(q_2^2)} + \epsilon_{Z\gamma}^{\text{CP}} \left( \frac{e Q_\mu g_Z^e}{q_2^2 P_Z(q_1^2)} + \frac{e Q_e g_Z^\mu}{q_1^2 P_Z(q_2^2)} \right) + \epsilon_{\gamma\gamma}^{\text{CP}} \frac{e^2 Q_e Q_\mu}{q_1^2 q_2^2} \right) \frac{\epsilon^{\alpha\beta\rho\sigma} q_{2\rho} q_{1\sigma}}{m_Z^2} \right]
 \end{aligned}$$

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 \epsilon_{\gamma\gamma}^{\text{SM-1L}} & \simeq 3.8 \times 10^{-3}, \\
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 \end{aligned}$$

# Charged current decays



The same approach can be extended to charged current decays

Only c.c.:  $h \rightarrow \bar{\nu}_e e \bar{\mu} \nu_\mu$

Interference  
of c.c. and n.c.:  $h \rightarrow e^+ e^- \nu \bar{\nu}$   
 $h \rightarrow \mu^+ \mu^- \nu \bar{\nu}$

$$\begin{aligned}
 \mathcal{A} = & i \frac{2m_W^2}{v_F} (\bar{e}_L \gamma_\alpha \nu_e) (\bar{\nu}_\mu \gamma_\beta \mu_L) \times \\
 & \left[ \left( \kappa_{WW} \frac{(g_W^e)^* g_W^\mu}{P_W(q_1^2) P_W(q_2^2)} + \frac{(\epsilon_{W e_L})^*}{m_W^2} \frac{g_W^\mu}{P_W(q_2^2)} + \frac{\epsilon_{W \mu_L}}{m_Z^2} \frac{(g_W^e)^*}{P_W(q_1^2)} \right) g^{\alpha\beta} + \right. \\
 & \left. + \epsilon_{WW} \frac{(g_W^e)^* g_W^\mu}{P_W(q_1^2) P_W(q_2^2)} \times \frac{q_1 \cdot q_2 g^{\alpha\beta} - q_2^\alpha q_1^\beta}{m_W^2} + \epsilon_{WW}^{\text{CP}} \frac{(g_W^e)^* g_W^\mu}{P_W(q_1^2) P_W(q_2^2)} \frac{\epsilon^{\alpha\beta\rho\sigma} q_{2\rho} q_{1\sigma}}{m_W^2} \right]
 \end{aligned}$$

# Parameter counting and symmetry assumptions

## Neutral current

$$h \rightarrow e^+e^-\mu^+\mu^-$$

$$h \rightarrow \mu^+\mu^-\mu^+\mu^-$$

$$h \rightarrow e^+e^-e^+e^-$$

$$h \rightarrow \gamma e^+e^-$$

$$h \rightarrow \gamma \mu^+\mu^-$$

$$h \rightarrow \gamma\gamma$$

$$\kappa_{ZZ}, \kappa_{Z\gamma}, \kappa_{\gamma\gamma}, \epsilon_{ZZ},$$

$$\epsilon_{Z\gamma}^{CP}, \epsilon_{\gamma\gamma}^{CP}, \epsilon_{ZZ}^{CP},$$

$$\epsilon_{Ze_L}, \epsilon_{Ze_R}, \epsilon_{Z\mu_L}, \epsilon_{Z\mu_R}$$

**11**

Charged  
current

$$h \rightarrow e^+\mu^-\nu\nu$$

$$h \rightarrow e^-\mu^+\nu\nu$$

$$\kappa_{WW}, \epsilon_{WW}, \epsilon_{WW}^{CP},$$

$$\epsilon_{We}, \epsilon_{W\mu}, \text{ (complex)}$$

**7**

N. & C.

interference

$$h \rightarrow e^+e^-\nu\nu$$

$$h \rightarrow \mu^+\mu^-\nu\nu$$

others +

$$\epsilon_{Z\nu_e}, \epsilon_{Z\nu_\mu}$$

**2**

Symmetries impose relations among these observables.

# Parameter counting and symmetry assumptions

## Neutral current

$$h \rightarrow e^+e^-\mu^+\mu^-$$

$$h \rightarrow \mu^+\mu^-\mu^+\mu^-$$

$$h \rightarrow e^+e^-e^+e^-$$

$$h \rightarrow \gamma e^+e^-$$

$$h \rightarrow \gamma \mu^+\mu^-$$

$$h \rightarrow \gamma\gamma$$

$$\kappa_{ZZ}, \kappa_{Z\gamma}, \kappa_{\gamma\gamma}, \epsilon_{ZZ},$$

$$\epsilon_{Z\gamma}^{CP}, \epsilon_{\gamma\gamma}^{CP}, \epsilon_{ZZ}^{CP},$$

$$\epsilon_{Ze_L}, \epsilon_{Ze_R}, \epsilon_{Z\mu_L}, \epsilon_{Z\mu_R}$$

**11**

|                    |                                |   |
|--------------------|--------------------------------|---|
| Charged<br>current | $h \rightarrow e^+\mu^-\nu\nu$ | $\kappa_{WW}, \epsilon_{WW}, \epsilon_{WW}^{CP},$ |
|                    | $h \rightarrow e^-\mu^+\nu\nu$ | $\epsilon_{We}, \epsilon_{W\mu},$ (complex)       |

**7**

|                         |                                  |  |
|-------------------------|----------------------------------|--|
| N. & C.<br>interference | $h \rightarrow e^+e^-\nu\nu$     | others +<br>$\epsilon_{Z\nu_e}, \epsilon_{Z\nu_\mu}$ |
|                         | $h \rightarrow \mu^-\mu^+\nu\nu$ |  |

**2**

Symmetries impose relations among these observables.

## Flavor universality

$$\epsilon_{Ze_L} = \epsilon_{Z\mu_L},$$

$$\epsilon_{Ze_R} = \epsilon_{Z\mu_R},$$

$$\epsilon_{Z\nu_e} = \epsilon_{Z\nu_\mu},$$

$$\epsilon_{We_L} = \epsilon_{W\mu_L}.$$

# Parameter counting and symmetry assumptions

## Neutral current

$$h \rightarrow e^+e^-\mu^+\mu^-$$

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$$\kappa_{ZZ}, \kappa_{Z\gamma}, \kappa_{\gamma\gamma}, \epsilon_{ZZ},$$

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$$\epsilon_{We_L} = \epsilon_{W\mu_L}$$

CP Invariance

$$\epsilon_{ZZ}^{CP} = \epsilon_{Z\gamma}^{CP} = \epsilon_{\gamma\gamma}^{CP} = \epsilon_{WW}^{CP} = \text{Im}\epsilon_{We_L} = \text{Im}\epsilon_{W\mu_L} = 0$$

# Parameter counting and symmetry assumptions

## Neutral current

- $h \rightarrow e^+e^-\mu^+\mu^-$
- $h \rightarrow \mu^+\mu^-\mu^+\mu^-$
- $h \rightarrow e^+e^-e^+e^-$
- $h \rightarrow \gamma e^+e^-$
- $h \rightarrow \gamma\mu^+\mu^-$
- $h \rightarrow \gamma\gamma$

$$\kappa_{ZZ}, \kappa_{Z\gamma}, \kappa_{\gamma\gamma}, \epsilon_{ZZ},$$

$$\epsilon_{Z\gamma}^{CP}, \epsilon_{\gamma\gamma}^{CP}, \epsilon_{ZZ}^{CP},$$

$$\epsilon_{Ze_L}, \epsilon_{Ze_R}, \epsilon_{Z\mu_L}, \epsilon_{Z\mu_R}$$

**11**

- Charged current  $h \rightarrow e^+\mu^-\nu\nu$   $\kappa_{WW}, \epsilon_{WW}, \epsilon_{WW}^{CP}$ ,  
 current  $h \rightarrow e^-\mu^+\nu\nu$   $\epsilon_{We}, \epsilon_{W\mu}$ , (complex)

**7**

- N. & C. interference  $h \rightarrow e^+e^-\nu\nu$  others +  
 $h \rightarrow \mu^+\mu^-\nu\nu$   $\epsilon_{Z\nu_e}, \epsilon_{Z\nu_\mu}$  **2**

Symmetries impose relations among these observables.

## Flavor universality

$$\epsilon_{Ze_L} = \epsilon_{Z\mu_L}$$

$$\epsilon_{Ze_R} = \epsilon_{Z\mu_R}$$

$$\epsilon_{Z\nu_e} = \epsilon_{Z\nu_\mu}$$

$$\epsilon_{We_L} = \epsilon_{W\mu_L}$$

## CP Invariance

$$\epsilon_{ZZ}^{CP} = \epsilon_{Z\gamma}^{CP} = \epsilon_{\gamma\gamma}^{CP} = \epsilon_{WW}^{CP}$$

## Custodial symmetry

$$\star \epsilon_{WW} = c_w^2 \epsilon_{ZZ} + 2c_w s_w \epsilon_{Z\gamma} + s_w^2 \epsilon_{\gamma\gamma},$$

$$\star \epsilon_{WW}^{CP} = c_w^2 \epsilon_{ZZ}^{CP} + 2c_w s_w \epsilon_{Z\gamma}^{CP} + s_w^2 \epsilon_{\gamma\gamma}^{CP},$$

$$\kappa_{WW} - \kappa_{ZZ} = -\frac{2}{g} \left( \sqrt{2} \epsilon_{We_L^i} + 2c_w \epsilon_{Ze_L^i} \right),$$

$$\star \epsilon_{We_L^i} = \frac{c_w}{\sqrt{2}} (\epsilon_{Z\nu_L^i} - \epsilon_{Ze_L^i}),$$

★ Accidentally true also in the linear EFT.

# Parameter counting and symmetry assumptions

## Neutral current

$h \rightarrow e^+e^-\mu^+\mu^-$   
 $h \rightarrow \mu^+\mu^-\mu^+\mu^-$   
 $h \rightarrow e^+e^-\mu^+\mu^-$   
 $h \rightarrow \gamma e^+e^-$   
 $h \rightarrow \gamma \mu^+\mu^-$   
 $h \rightarrow \gamma\gamma$

$\kappa_{ZZ}, \kappa_{Z\gamma}, \kappa_{\gamma\gamma}, \epsilon_{ZZ}$ ,

$\epsilon_{Z\gamma}^{CP}, \epsilon_{\gamma\gamma}^{CP}, \epsilon_{ZZ}^{CP}$ ,

$\epsilon_{Ze_L}, \epsilon_{Ze_R}, \epsilon_{Z\mu_L}, \epsilon_{Z\mu_R}$

**11**

Charged current  $h \rightarrow e^+\mu^-\nu\nu$   $\kappa_{WW}, \epsilon_{WW}, \epsilon_{WW}^{CP}$ ,  
 current  $h \rightarrow e^-\mu^+\nu\nu$   $\epsilon_{We}, \epsilon_{W\mu}$ , (complex)

**7**

N. & C. interference  $h \rightarrow e^+e^-\nu\nu$  others +  
 $h \rightarrow \mu^+\mu^-\nu\nu$   $\epsilon_{Z\nu_e}, \epsilon_{Z\nu_\mu}$  **2**

Symmetries in **20** (general case)  $\longrightarrow$  **7** (max symm.)

## Flavor universality

$$\epsilon_{Ze_L} = \epsilon_{Z\mu_L}$$

$$\epsilon_{Ze_R} = \epsilon_{Z\mu_R}$$

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## CP Invariance

$$\epsilon_{ZZ}^{CP} = \epsilon_{Z\gamma}^{CP} = \epsilon_{\gamma\gamma}^{CP} = \epsilon_{WW}^{CP}$$

## Custodial symmetry

$$\star \epsilon_{WW} = c_w^2 \epsilon_{ZZ} + 2c_w s_w \epsilon_{Z\gamma} + s_w^2 \epsilon_{\gamma\gamma},$$

$$\star \epsilon_{WW}^{CP} = c_w^2 \epsilon_{ZZ}^{CP} + 2c_w s_w \epsilon_{Z\gamma}^{CP} + s_w^2 \epsilon_{\gamma\gamma}^{CP},$$

$$\kappa_{WW} - \kappa_{ZZ} = -\frac{2}{g} \left( \sqrt{2} \epsilon_{We_L^i} + 2c_w \epsilon_{Ze_L^i} \right),$$

$$\star \epsilon_{We_L^i} = \frac{c_w}{\sqrt{2}} (\epsilon_{Z\nu_L^i} - \epsilon_{Ze_L^i}),$$

$\star$  Accidentally true also in the linear EFT.



# Parameter counting and symmetry assumptions

Neutral current

- $h \rightarrow e^+e^-\mu^+\mu^-$
- $h \rightarrow \mu^+\mu^-\mu^+\mu^-$
- $h \rightarrow e^+e^-e^+e^-$
- $h \rightarrow \gamma e^+e^-$
- $h \rightarrow \gamma \mu^+\mu^-$
- $h \rightarrow \gamma\gamma$

Charged  $h \rightarrow e^+\mu^-\nu_e\nu_\mu$  (CP, complex)

Possibility to test such hypotheses from Higgs data only.

Contact terms are extremely important for this goal.

2

Symmetries in

20 (general case)



7 (max symm.)

Flavor universality

- $\epsilon_{Ze_L} = \epsilon_{Z\mu_L}$
- $\epsilon_{Ze_R} = \epsilon_{Z\mu_R}$
- $\epsilon_{Z\nu_e} = \epsilon_{Z\nu_\mu}$
- $\epsilon_{We_L} = \epsilon_{W\mu_L}$

CP Invariant

$$\epsilon_{ZZ}^{CP} = \epsilon_{Z\gamma}^{CP} = \epsilon_{\gamma\gamma}^{CP} = \epsilon_{WW}^{CP}$$

Custodial symmetry

- ★  $\epsilon_{WW} = c_w^2 \epsilon_{ZZ} + 2c_w s_w \epsilon_{Z\gamma} + s_w^2 \epsilon_{\gamma\gamma}$ ,
- ★  $\epsilon_{WW}^{CP} = c_w^2 \epsilon_{ZZ}^{CP} + 2c_w s_w \epsilon_{Z\gamma}^{CP} + s_w^2 \epsilon_{\gamma\gamma}^{CP}$ ,
- $\kappa_{WW} - \kappa_{ZZ} = -\frac{2}{g} \left( \sqrt{2} \epsilon_{We_L^i} + 2c_w \epsilon_{Ze_L^i} \right)$ ,
- ★  $\epsilon_{We_L^i} = \frac{c_w}{\sqrt{2}} (\epsilon_{Z\nu_L^i} - \epsilon_{Ze_L^i})$ ,

★ Accidentally true also in the linear EFT.

# Prospects in $h \rightarrow 4\ell$

[Work in progress]

At HL-LHC (2037) we will have  $\sim 8000$  events in  $h \rightarrow 4\ell$

| ATLAS Selected signal event rates |     |     |    |     |      |
|-----------------------------------|-----|-----|----|-----|------|
|                                   | ttH | ZH  | WH | VBF | ggH  |
| 3000fb <sup>-1</sup>              | 35  | 5.7 | 67 | 97  | 3800 |

[From Aleandro Nisati's [talk at LHCP 2015](#)]

few % precision in  $h \rightarrow \gamma\gamma$   
 $\sim 10\%$  precision in  $h \rightarrow Z\gamma$

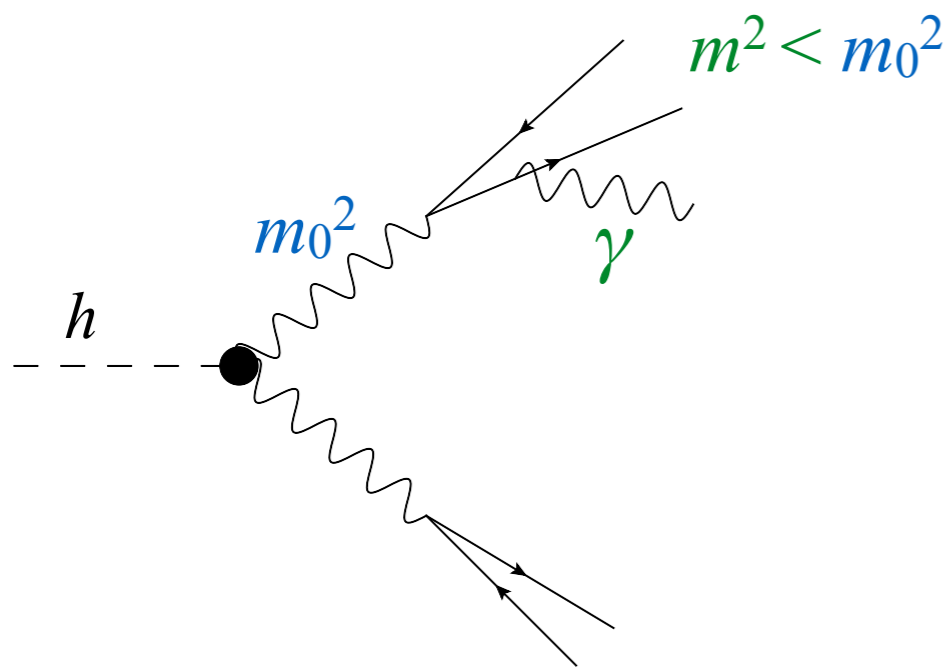


They already  
fix 4 PO to be really small.

A precise 11 parameter global fit is very reasonable.

# Radiative Corrections

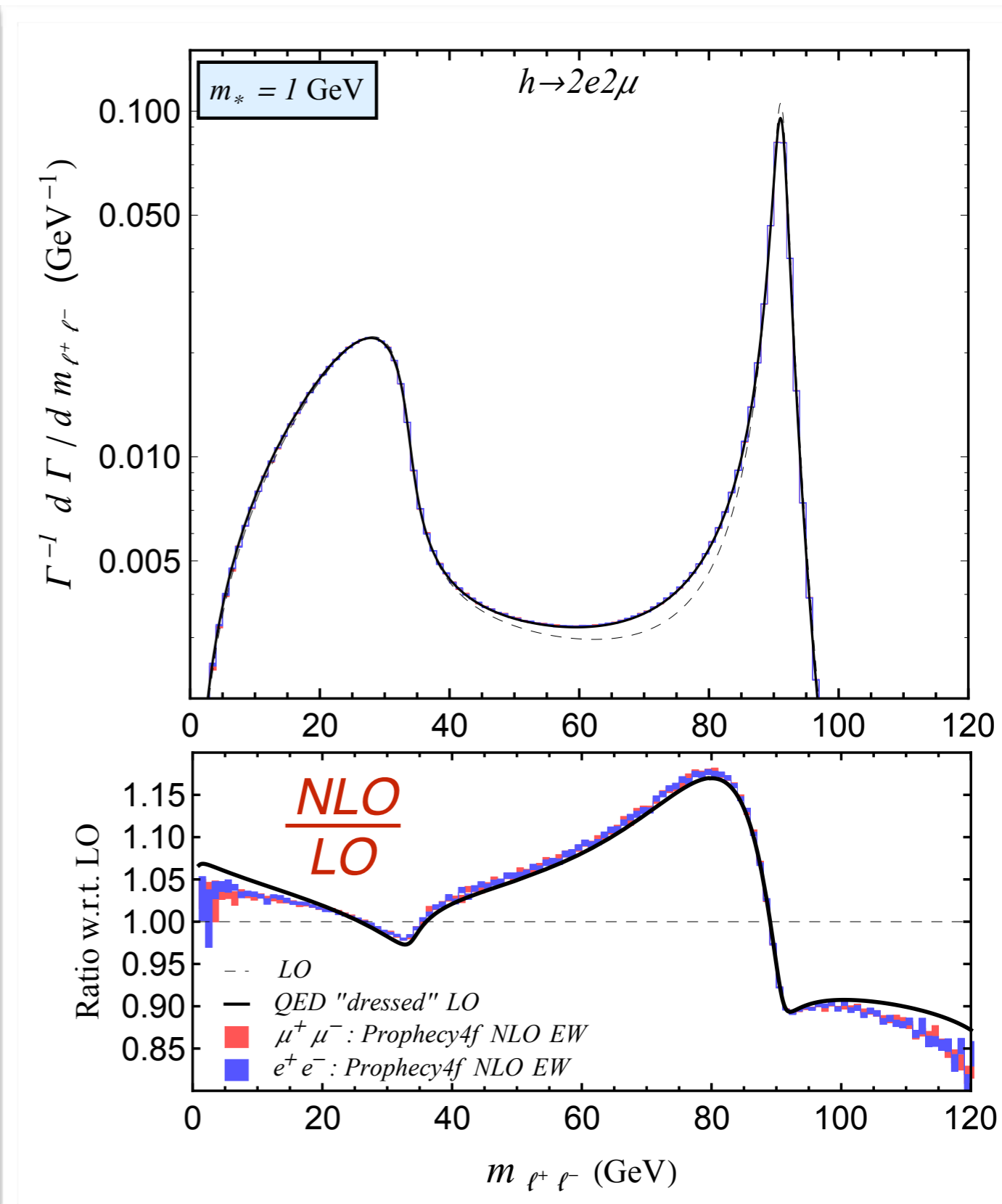
The most important radiative corrections are given by **soft QED radiation** effects since they **distort the spectrum**.



Effect described by **simple and universal radiator functions**.

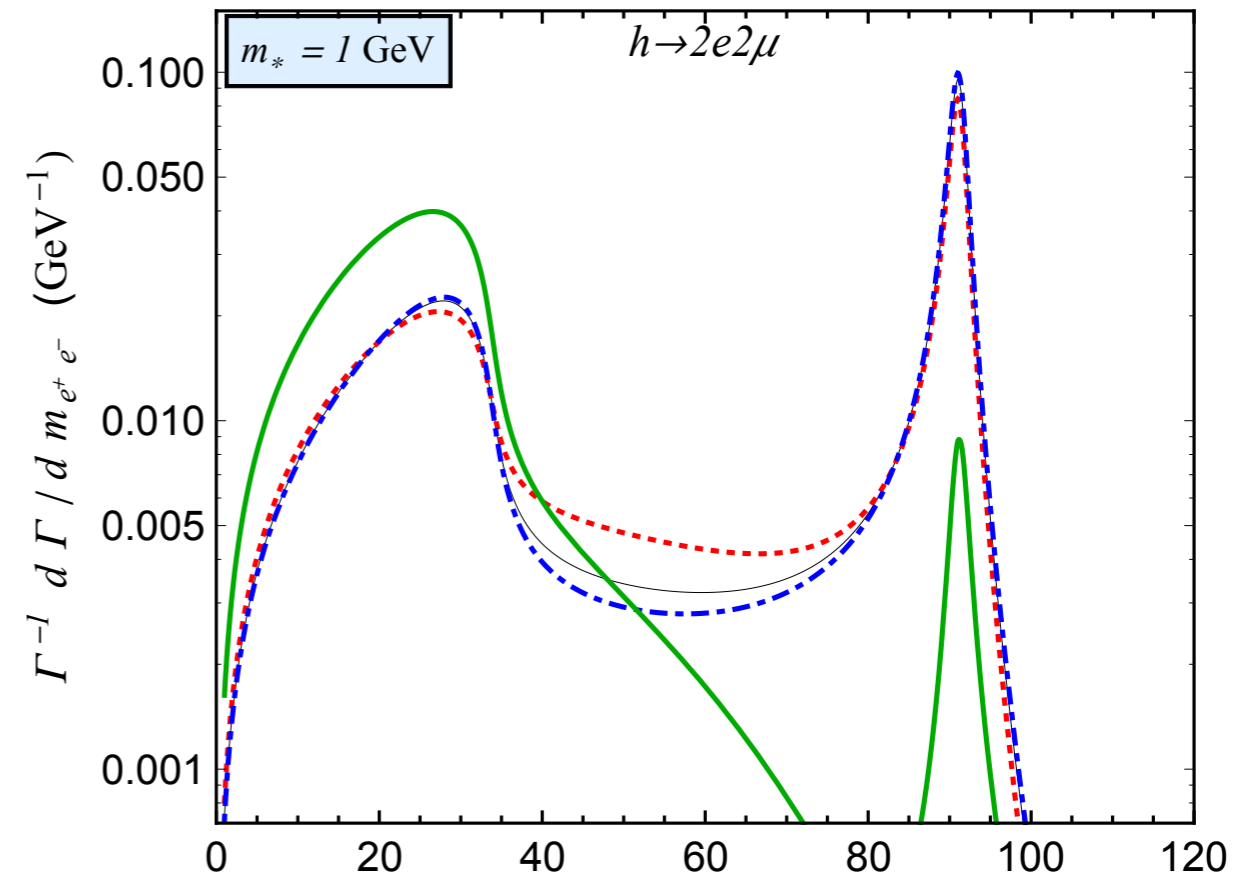
**~15% effect!**

Other NLO corrections are small:  $\approx 1\%$

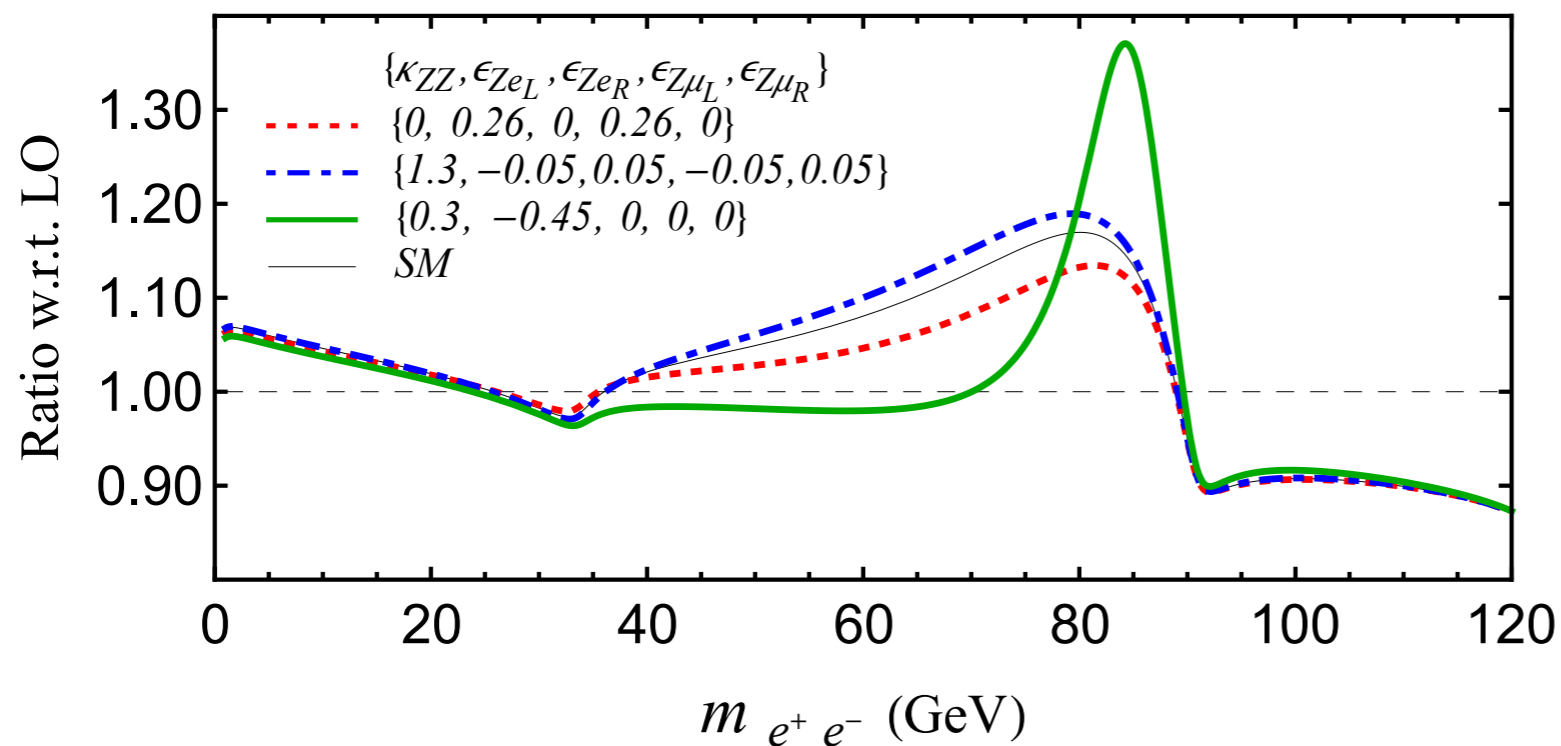


# Radiative Corrections

Taking this effect into account is **necessary to extract the PO** from data.



All these benchmark points give a SM-like total rate.



Showering algorithms (e.g. PHOTOS or PYTHIA) correctly describe these corrections.

# Tools: *HiggsPO*

In collaboration with Admir Greljo and Gino Isidori



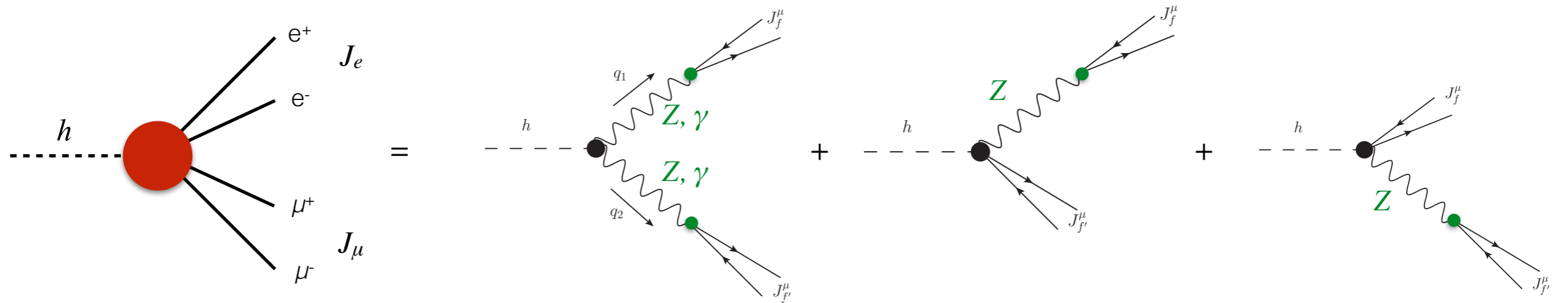
[www.physik.uzh.ch/data/HiggsPO](http://www.physik.uzh.ch/data/HiggsPO)

A **Universal FeynRules Output** model for  
generating **Higgs decays** with **MG5\_aMC@NLO**.

To be used to generate the **on-shell Higgs decay amplitudes** described before.

(use tree-level Feynman rules to generate the amplitude we need)

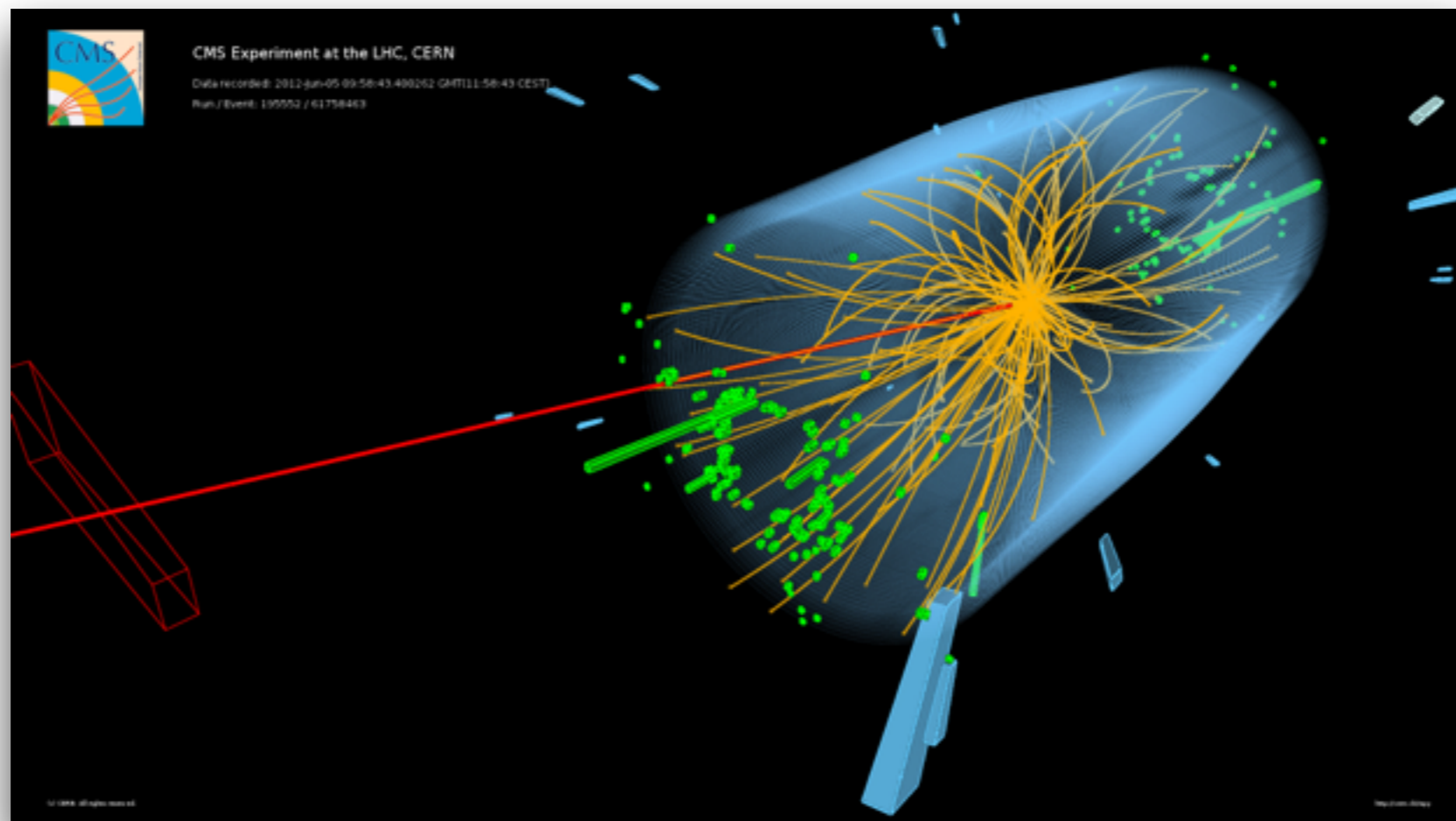
Extensively **validated** by comparing to our analytic results and other codes  
(Higgs Characterization, MEKD).



*To summarize.* **Higgs PO in decay**

- Related to **physical distributions**, measurable experimentally.
- Defined from the **residues of the Green function on its poles**.  
(valid at all orders in perturbation theory)
- Can be used to **test symmetries** and/or dynamics of the NP sector.
- **QED radiation** corrections are easily implemented.
- Implemented a **Montecarlo tool** for event generation.

# Pseudo observables in Electroweak Higgs Production



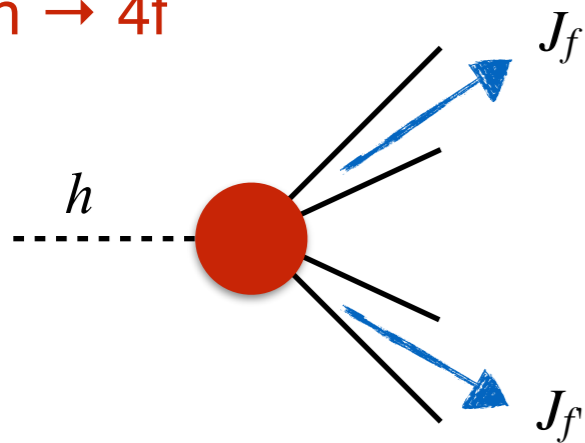
# PO in EW Higgs Production

[Work in progress with Admir, Gino and Jonas]

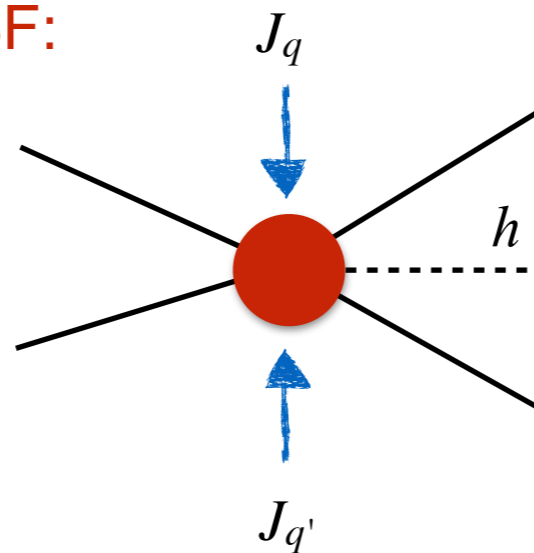
$$\langle 0 | \mathcal{T} \{ J_f^\mu(x), J_{f'}^\nu(y), h(0) \} | 0 \rangle$$

By crossing symmetry, the **same correlation function** (in a different kinematical region and with different fermionic currents) enters also in **EW Higgs production**.

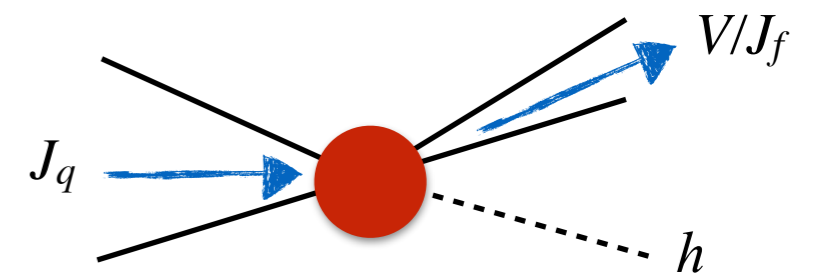
$h \rightarrow 4f$



VBF:

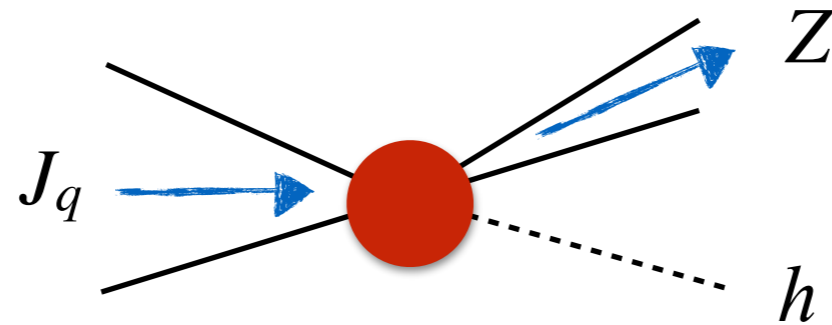


V h:





# Associate Zh production



The amplitude is the same as for the decays:

$$\mathcal{A}(q_i(p_1)\bar{q}_i(p_2) \rightarrow h(p)Z(k)) = i\frac{2m_W^2}{v}\bar{q}_i(p_2)\gamma_\nu q_i(p_1)\epsilon_\mu^{Z*}(k) \left[ \left( \kappa_{ZZ} \frac{g_{Zq_i}}{P_Z(q^2)} + \frac{\epsilon_{Zq_i}}{m_Z^2} \right) g^{\mu\nu} + \left( \epsilon_{ZZ} \frac{g_{Zq_i}}{P_Z(q^2)} + \epsilon_{Z\gamma} \frac{eQ_q}{q^2} \right) \frac{-(q \cdot k)g^{\mu\nu} + q^\mu k^\nu}{m_Z^2} + \left( \tilde{\epsilon}_{ZZ} \frac{g_{Zq_i}}{P_Z(q^2)} + \tilde{\epsilon}_{Z\gamma} \frac{eQ_q}{q^2} \right) \frac{-\epsilon^{\mu\nu\alpha\beta} q_\alpha k_\beta}{m_Z^2} \right]$$

Only **quark contact terms** are not probed in  $h \rightarrow 4\ell$  decays.

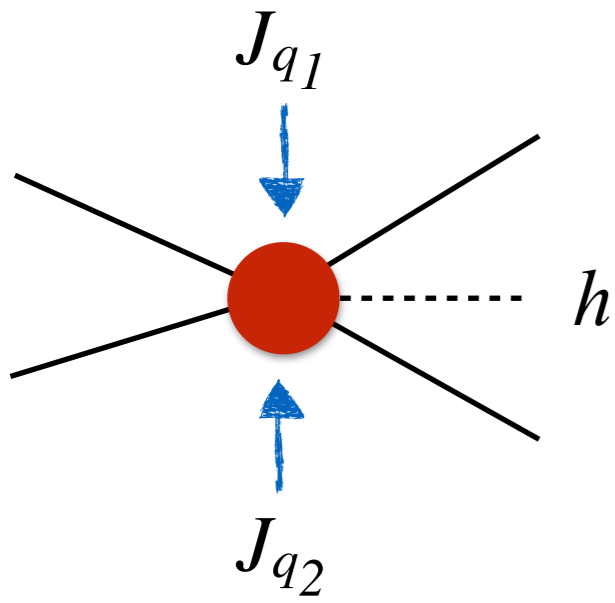
Form factor,  
mom. expansion validity

only 1 observable:

$$q^2 = (p_h + k_Z)^2$$

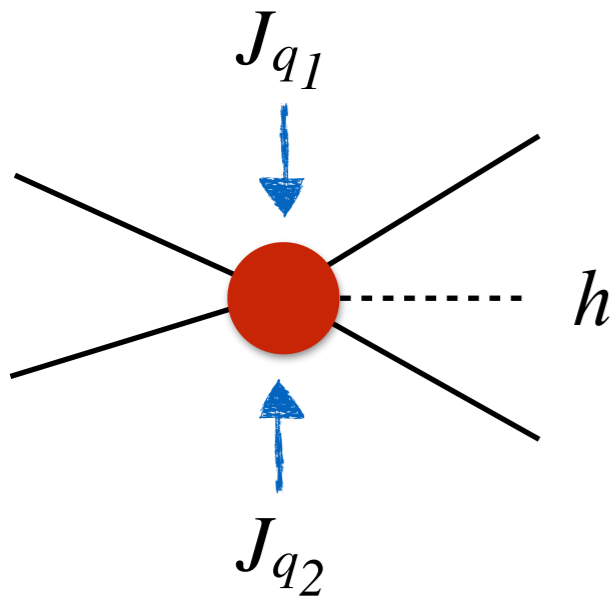
## VBF Higgs production

Again, same amplitude as decays.



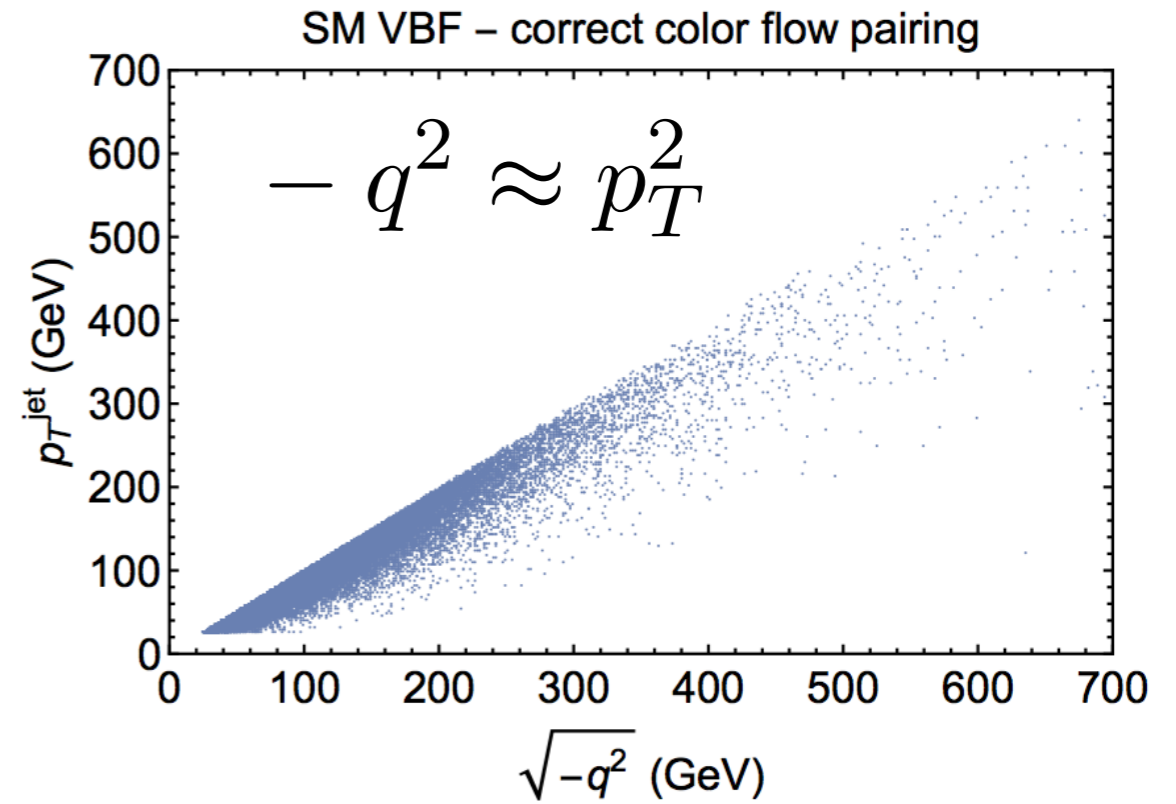
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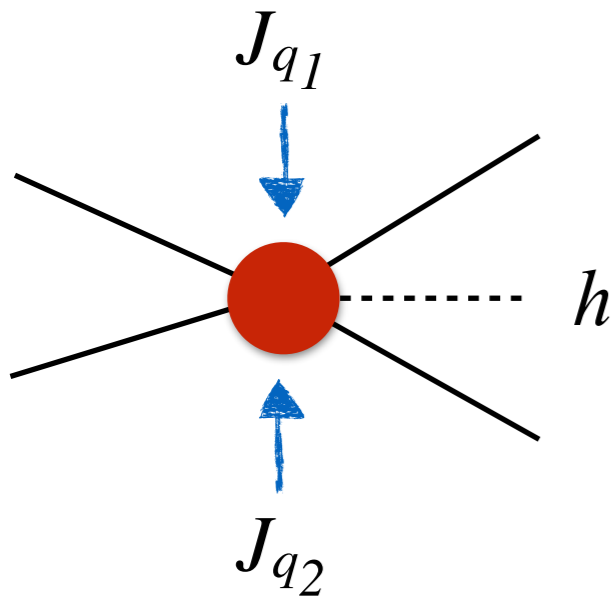
Initial state quarks are not accessible, so is  $q^2$ .  
(unless Higgs is reconstructed)

$p_T$  of the jets is a good proxy for the  $q^2$ .



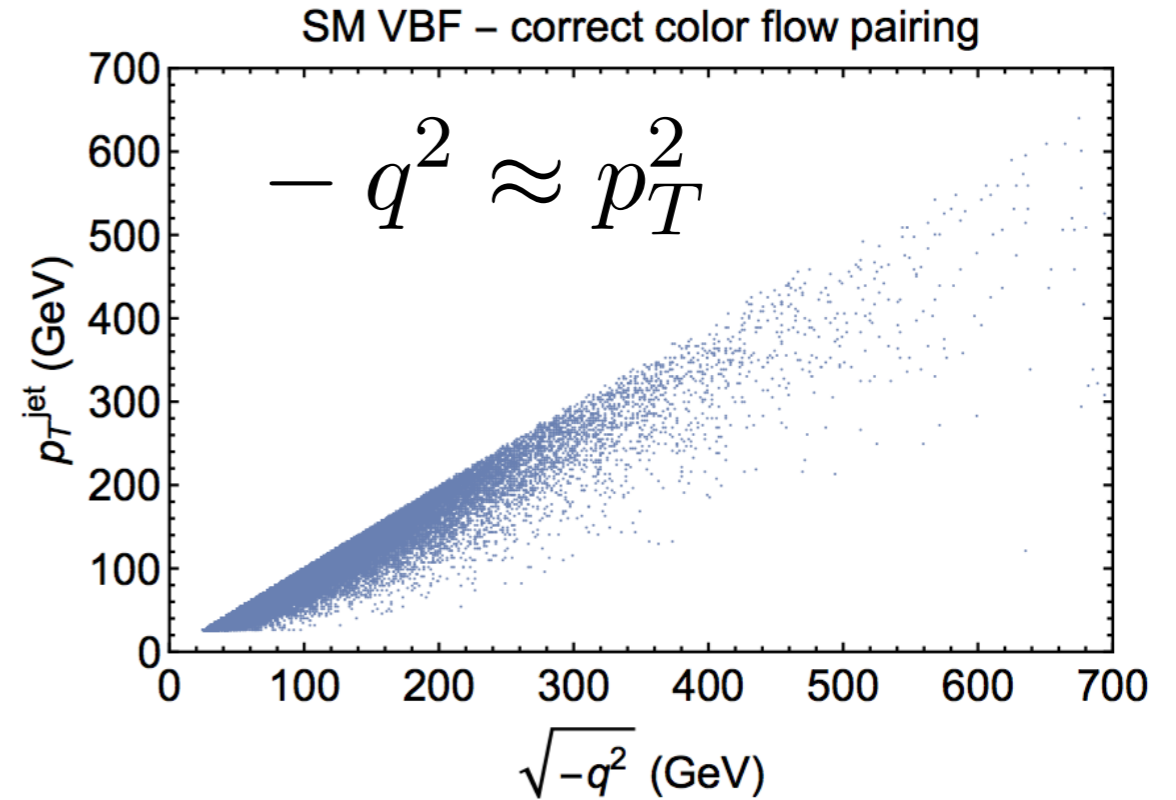
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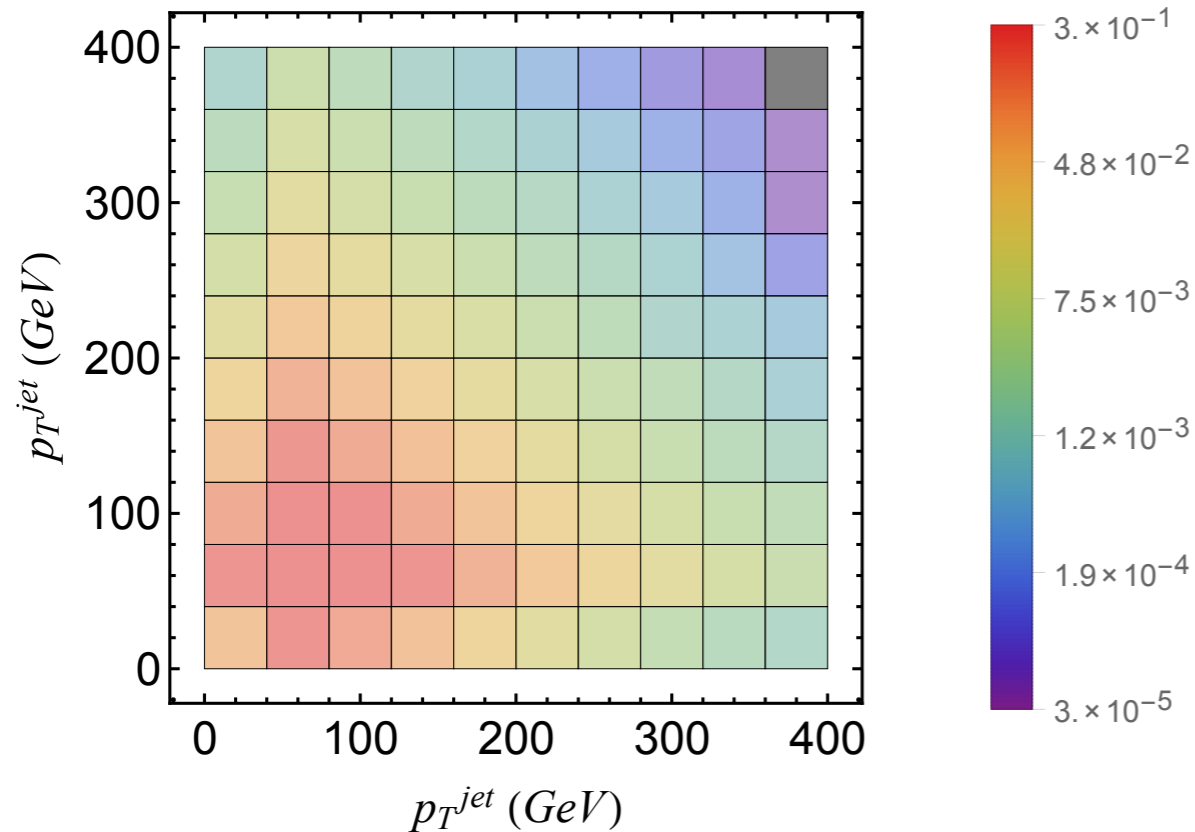


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Higgs VBF in the SM



$$F(q_1^2, q_2^2) \rightarrow \tilde{F}(p_{T1}^2, p_{T2}^2)$$

**General approach: measure the double differential distribution in  $(p_{T1}^2, p_{T2}^2)$**

With 3000 fb<sup>-1</sup>: ~ 2000 events in VBF



**precision physics!**

## 2000 events in VBF Higgs production

Flavor-independent PO probed in  $h \rightarrow 4\ell$  decay.  Focus on **quark contact terms**.

For simplicity let's assume **Minimal Flavor Violation**. Consider **7 PO**:

$$\kappa_{ZZ} , \quad \kappa_{WW} , \quad \epsilon_{Zu_L} , \quad \epsilon_{Zu_R} , \quad \epsilon_{Zd_L} , \quad \epsilon_{Zd_R} , \quad \epsilon_{Wu_L}$$

Do a fit of the **2D  $p_T$  distribution**, up to **600 GeV**.  **Momentum expansion validity.**

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Do a fit of the **2D  $p_T$  distribution**, up to **600 GeV**.  **Momentum expansion validity.**

Very preliminary result. Only at parton level:

$$\begin{pmatrix} \kappa_{ZZ} \\ \kappa_{WW} \\ \epsilon_{Zu_L} \\ \epsilon_{Zu_R} \\ \epsilon_{Zd_L} \\ \epsilon_{Zd_R} \\ \epsilon_{Wu_L} \end{pmatrix} : \quad \sigma = \begin{pmatrix} 0.46 \\ 0.17 \\ 0.015 \\ 0.023 \\ 0.021 \\ 0.031 \\ 0.004 \end{pmatrix}$$

Assuming expected 2000 events in the SM.

$$\rho = \begin{pmatrix} 1. & -0.98 & -0.04 & -0.18 & -0.31 & -0.25 & -0.04 \\ -0.98 & 1. & -0.03 & 0.14 & 0.25 & 0.18 & 0.1 \\ -0.04 & -0.03 & 1. & 0.22 & 0.55 & -0.13 & -0.33 \\ -0.18 & 0.14 & 0.22 & 1. & -0.22 & 0.03 & 0.14 \\ -0.31 & 0.25 & 0.55 & -0.22 & 1. & 0.12 & 0.22 \\ -0.25 & 0.18 & -0.13 & 0.03 & 0.12 & 1. & -0.29 \\ -0.04 & 0.1 & -0.33 & 0.14 & 0.22 & -0.29 & 1. \end{pmatrix}$$

LHC will be able to **measure all the contact terms with percent accuracy!**

Same conclusion also if no information on the total rate is retained.

**Pseudo observables**  
**and**  
**the SM Effective Theory**



# The Linear SM Effective Field Theory

Integrate out the heavy BSM dof.

Low energy theory specified by Symmetries & Field content

Assuming  $h(125)$  is a  $SU(2)_L$  doublet  
(linear EFT)

$$\varphi = \begin{pmatrix} \varphi^+ \\ \varphi^0 \end{pmatrix} = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v + h(x) \end{pmatrix}$$

and

Scale of New Physics is high

$$\Lambda_{NP} \gg m_h$$



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and

$$\Lambda_{NP} \gg m_h$$

Scale of New Physics is high

Assuming L and B conservation

$$\mathcal{L} = \mathcal{L}^{SM} + \sum_i \frac{c_i}{\Lambda^2} \mathcal{O}_i^{d=6} + (\text{dim} > 6)$$

Standard Model  
Lagrangian ( $d \leq 4$ )

Leading deformations of the SM

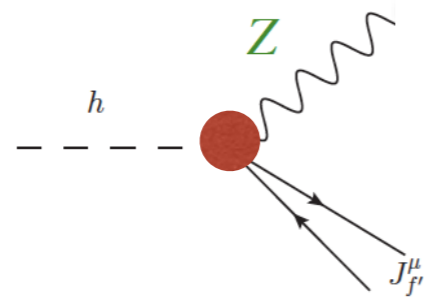
59 independent dim-6 operators if flavour universality.  
2499 parameters for a generic flavour structure.

[Grzadkowski et al. 1008.4884, Alonso et al. 1312.2014]

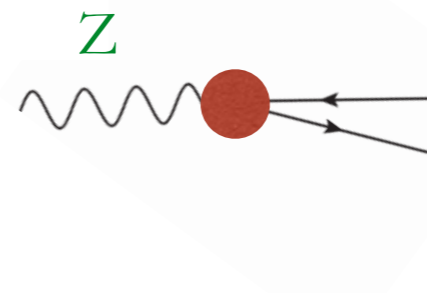
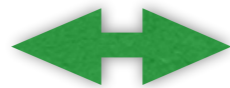
# The power of the EFT: relating different observables

The same operator can contribute to different processes.

For example: 
$$O_{Hf} = i(H^\dagger \overleftrightarrow{D}_\mu H) \bar{f} \gamma^\mu f = -\frac{1}{2} \sqrt{g^2 + g'^2} Z_\mu (v + h)^2 \bar{f} \gamma^\mu f$$



Higgs decay & production

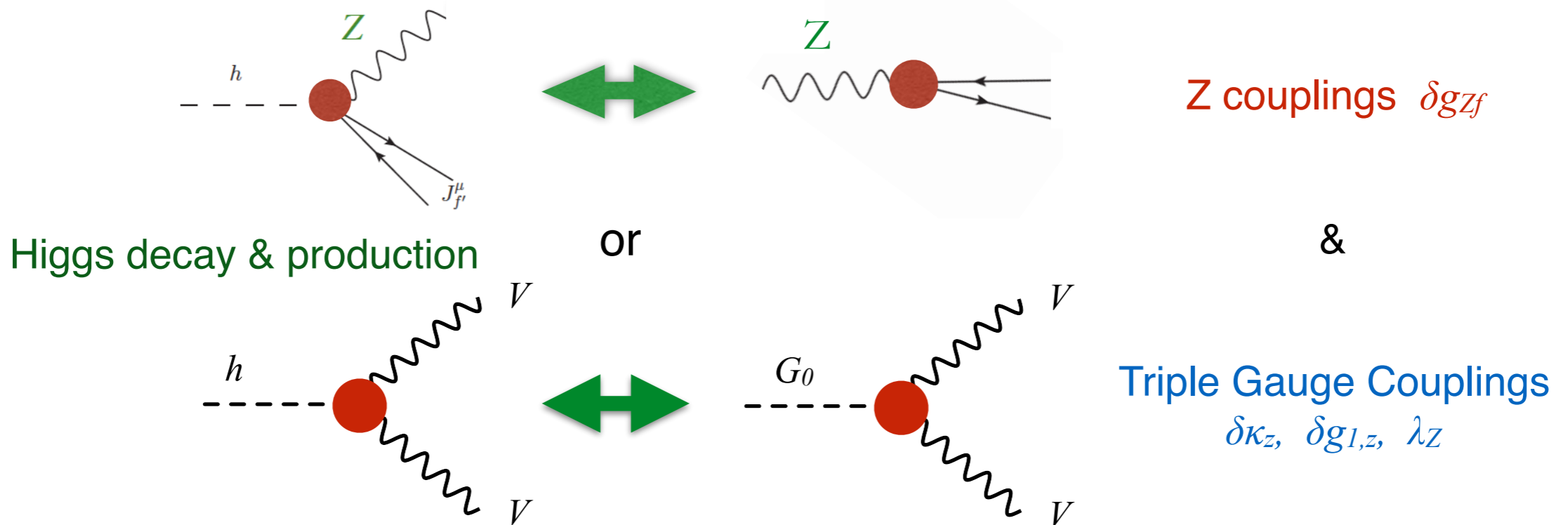


Z couplings  $\delta g_{zf}$

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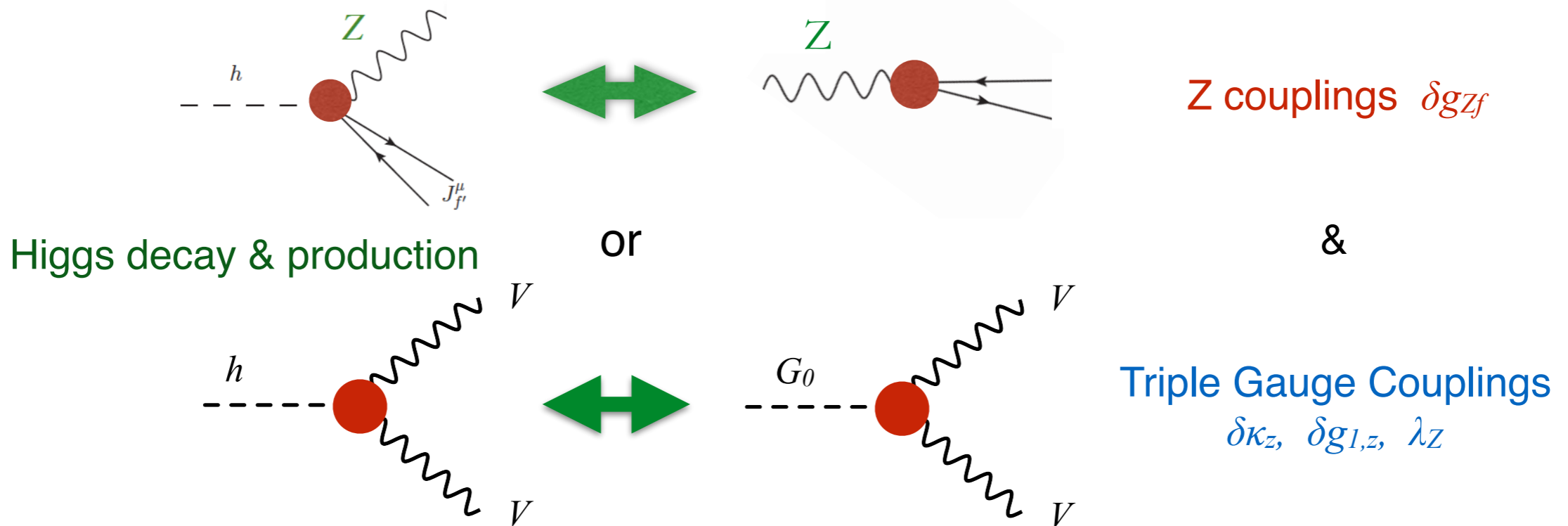
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- ★ Use LEP 1 and LEP 2 data to obtain bounds on some Higgs PO.
- ★ Combine LEP data with Higgs data to derive stronger constraints for the EFT.

# The power of the EFT: relating different observables

Let us impose the strong **LEP I constraints** ( $\approx 1\%$ ).

[Pomarol Riva 2013; Efrati et al. 2015; Berthier, Trott 2015]

Assuming **MFV**, only **10 independent combinations** of coefficients contribute at tree-level to **Higgs** and **LEP II (WW)** observables.

[Corbett et al. 2013; J. Elias-Miro et al. 2013;  
Pomarol Riva 2013; Gupta et al 2014; Falkowski 2015]

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Global fit in the '**Higgs basis**' [LHCHXSWG 2015]

[Falkowski, Gonzalez-Alonso, Greljo, D.M. 1508.00581]

$\delta c_z, c_{\gamma\gamma}, c_{z\gamma}, c_{gg}, \delta y_u, \delta y_d, \delta y_e, \delta g_{1,z}, \delta \kappa_\gamma, \lambda_z.$

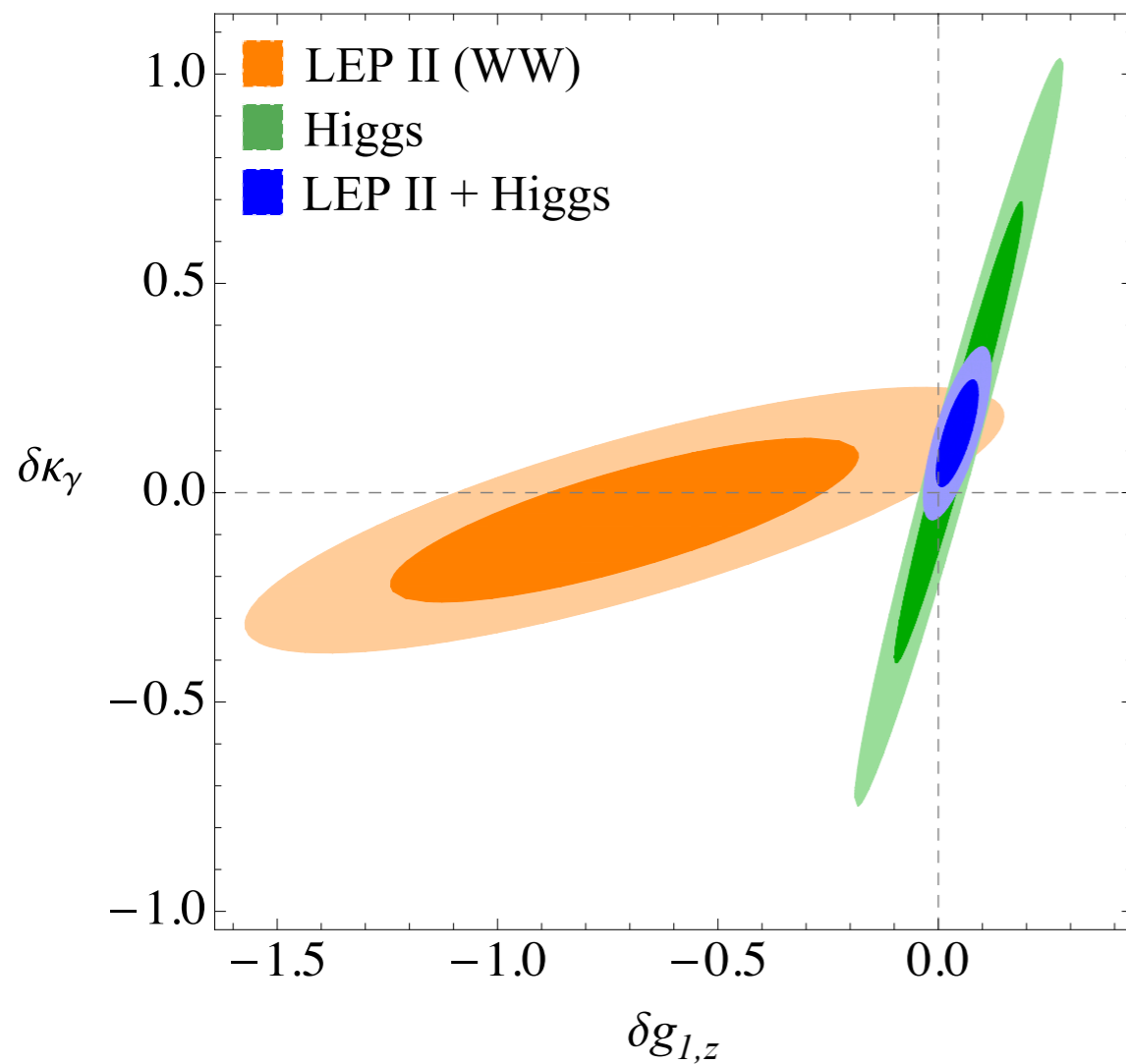
**Higgs**

**TGC**

# The power of the EFT: relating different observables

## Constraints on TGCs

All other coefficients have been marginalised.



LEP II data alone suffers from a **flat direction** in the TGC fit. [Falkowski, Riva 1411.0669]

+

Higgs data (mainly via VH and VBF production) is sensitive to a different direction.

[Falkowski 1505.00046]

=

Together they provide **strong and robust constraints on the TGC**.

# Constraints on the Higgs PO in the linear EFT

We match the Higgs PO to the SM EFT at LO: relations with LEP observables.

e.g  $h \rightarrow 4\ell$ :

$$\epsilon_{Zf} = \frac{2m_Z}{v} \left( \delta g^{Zf} - (c_\theta^2 T_f^3 + s_\theta^2 Y_f) \mathbf{1}_3 \delta g_{1,z} + t_\theta^2 Y_f \mathbf{1}_3 \delta \kappa_\gamma \right)$$

$$\delta \epsilon_{ZZ} = \delta \epsilon_{\gamma\gamma} + \frac{2}{t_{2\theta}} \delta \epsilon_{Z\gamma} - \frac{1}{c_\theta^2} \delta \kappa_\gamma$$

[Gonzalez-Alonso, Greljo, Isidori, D.M. 1504.04018]

**LEP-I:**  $\delta g^{Z\ell} \lesssim 10^{-2}$  [Efrati, Falkowski, Soreq 2015]

Naively  $\sim 10^{-3}$  bounds, however the theoretical error is of  $\sim 1\%$ .

[Berthier, Trott 2015]

No qualitative influence for Higgs physics at present precision.

**From LHC:**  $\delta \epsilon_{\gamma\gamma} \lesssim 10^{-3}$   
 $\delta \epsilon_{Z\gamma} \lesssim 10^{-2}$

The less constrained coefficients are the TGC.

We use our combined LEP II + Higgs global fit to derive constraints on the Higgs PO.



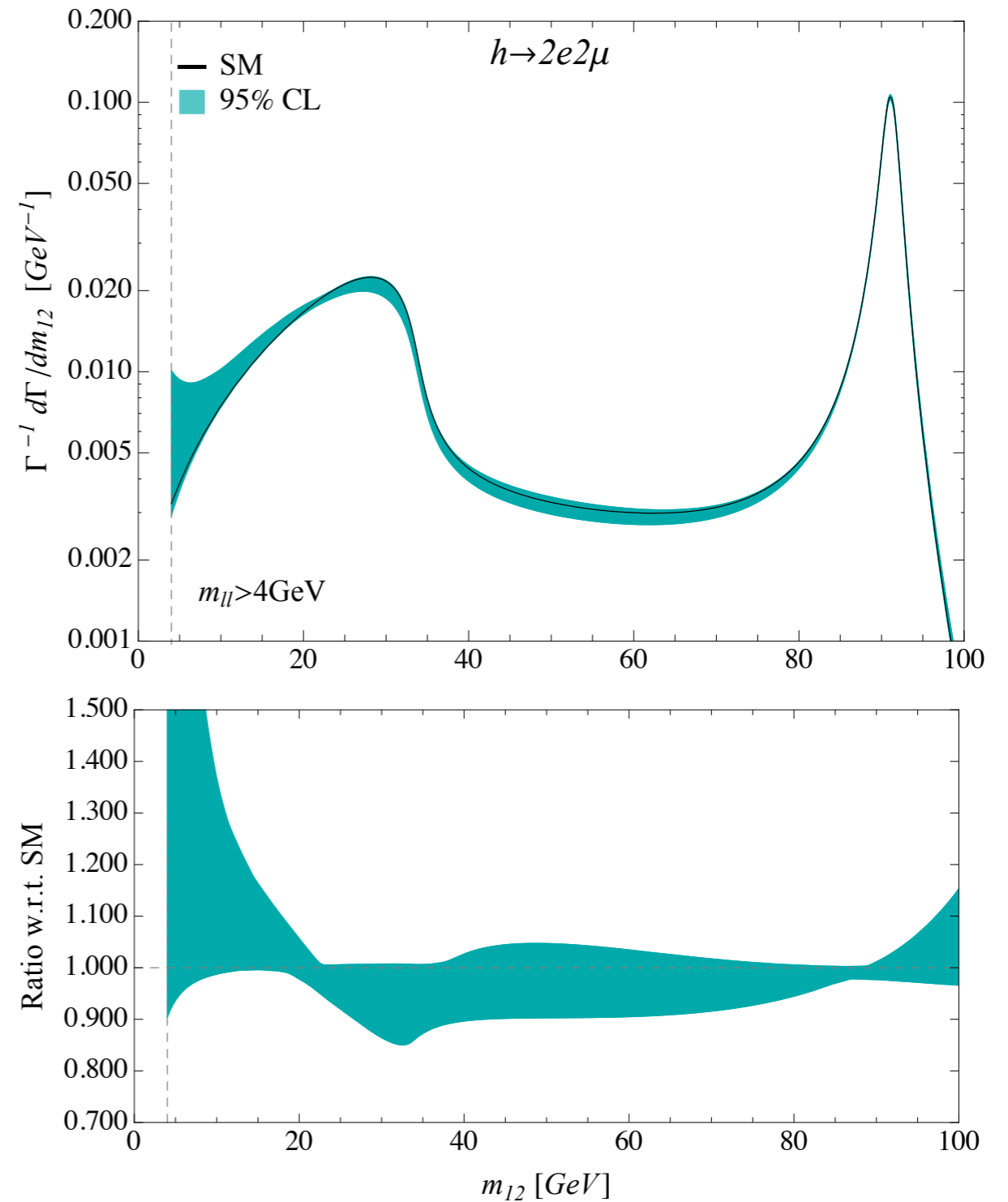
# Predictions for $h \rightarrow 4\ell$ in the linear EFT

5 independent PO only, in the linear EFT.

$$\begin{pmatrix} \kappa_{ZZ} \\ \epsilon_{Zl_L} \\ \epsilon_{Zl_R} \\ \kappa_{Z\gamma} \\ \kappa_{\gamma\gamma} \end{pmatrix} = \begin{pmatrix} 0.85 \pm 0.17 \\ -0.0001 \pm 0.0078 \\ -0.025 \pm 0.015 \\ 0.96 \pm 1.6 \\ 0.88 \pm 0.19 \end{pmatrix},$$

$$\rho = \begin{pmatrix} 1 & .72 & .60 & .19 & .83 \\ \cdot & 1 & .35 & -.16 & .62 \\ \cdot & \cdot & 1 & .02 & .47 \\ \cdot & \cdot & \cdot & 1 & .20 \\ \cdot & \cdot & \cdot & \cdot & 1 \end{pmatrix}.$$

From these bounds we can extract precise predictions for Higgs data, such as **di-lepton invariant mass spectra**.

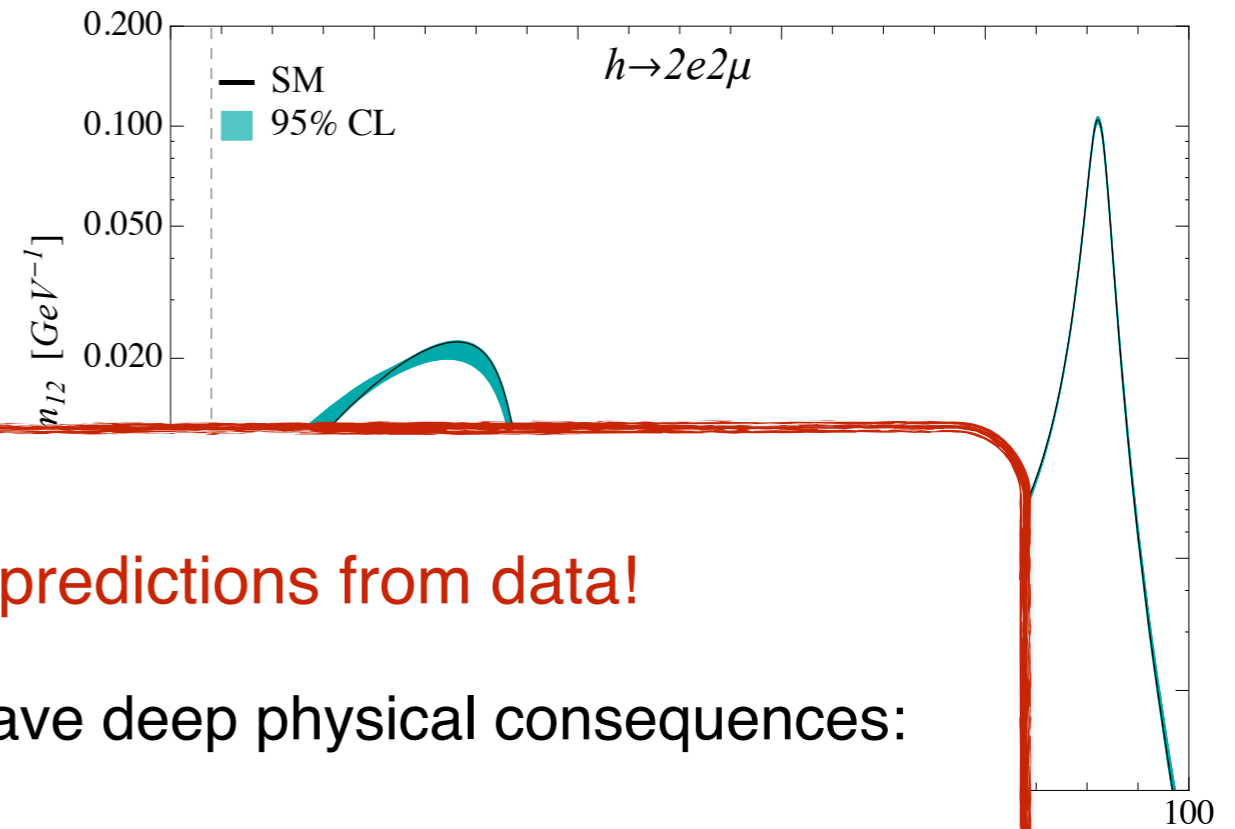


Small deviations allowed in the shape.

# Predictions for $h \rightarrow 4\ell$ in the linear EFT

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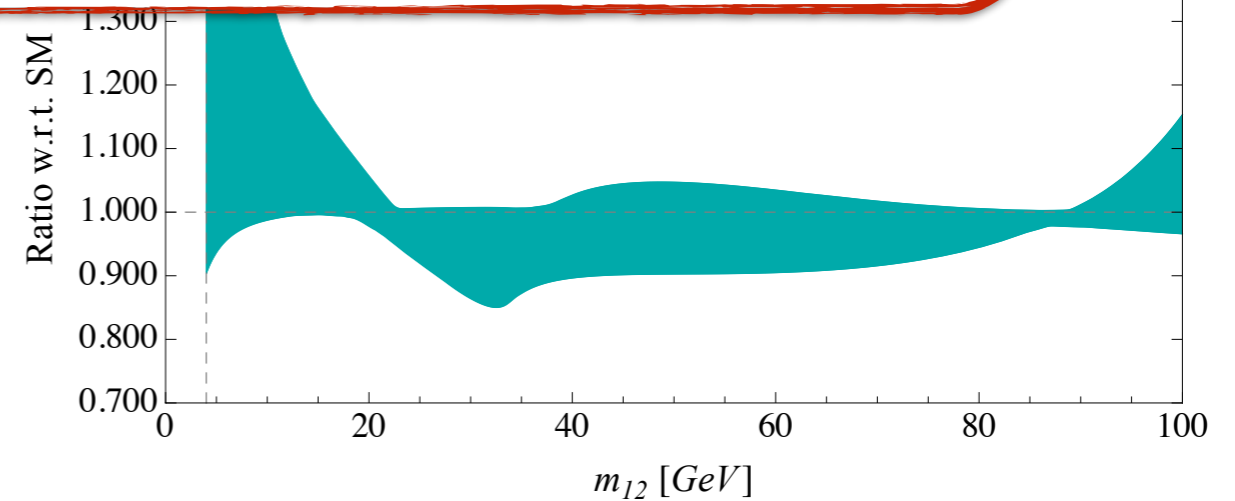


Crucial to test these predictions from data!

Any measured deviation would have deep physical consequences:

non-linear realization of EW symmetry, flavor non-universality, ...

From these bounds we can extract precise predictions for Higgs data, such as di-lepton invariant mass spectra.



Small deviations allowed in the shape.

# Conclusions

## Higgs PO

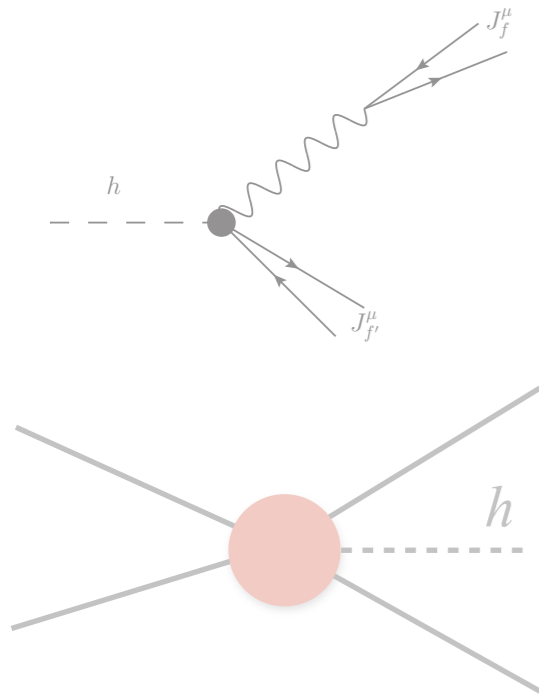
- **general framework** to describe on-shell Higgs properties: **decay** and **production**.
- defined from **physical properties** of the Green functions
- **easy to match** to specific scenarios: **test hypotheses**.
- clear implementation of **QED soft radiation** (leading NLO effect)

Implemented in FeynRules/UFO model:

[www.physik.uzh.ch/data/HiggsPO/](http://www.physik.uzh.ch/data/HiggsPO/)

The **linear EFT** provides relations among **Higgs and non-Higgs** processes:

- **combine LEP and Higgs** data to derive stronger constraints
  - derive **predictions for  $h \rightarrow 4\ell$  processes**
- Testing these predictions: **important test for the linear EFT**.



# Backup

# “Physical” PO in $h \rightarrow 4\ell$

**Goal:** provide a simple interpretation for the PO.

$$\mathcal{A} = i \frac{2m_Z^2}{v_F} (\bar{e}\gamma_\alpha e)(\bar{\mu}\gamma_\beta \mu) \times$$

$$\left[ \left( \kappa_{ZZ} \frac{g_Z^e g_Z^\mu}{P_Z(q_1^2) P_Z(q_2^2)} + \frac{\epsilon_{Ze}}{m_Z^2} \frac{g_Z^\mu}{P_Z(q_2^2)} + \frac{\epsilon_{Z\mu}}{m_Z^2} \frac{g_Z^e}{P_Z(q_1^2)} \right) g^{\alpha\beta} + \right.$$

$$+ \left( \epsilon_{ZZ} \frac{g_Z^e g_Z^\mu}{P_Z(q_1^2) P_Z(q_2^2)} + \kappa_{Z\gamma}^{\text{SM,eff}} \epsilon_{Z\gamma} \left( \frac{eQ_\mu g_Z^e}{q_2^2 P_Z(q_1^2)} + \frac{eQ_e g_Z^\mu}{q_1^2 P_Z(q_2^2)} \right) + \kappa_{\gamma\gamma}^{\text{SM,eff}} \frac{e^2 Q_e Q_\mu}{q_1^2 q_2^2} \right) \frac{q_1 \cdot q_2 g^{\alpha\beta} - q_2^\alpha q_1^\beta}{m_Z^2} +$$

$$\left. + \left( \epsilon_{ZZ}^{\text{CP}} \frac{g_Z^e g_Z^\mu}{P_Z(q_1^2) P_Z(q_2^2)} + \lambda_{Z\gamma}^{\text{CP}} \epsilon_{Z\gamma}^{\text{SM,eff}} \left( \frac{eQ_\mu g_Z^e}{q_2^2 P_Z(q_1^2)} + \frac{eQ_e g_Z^\mu}{q_1^2 P_Z(q_2^2)} \right) + \lambda_{\gamma\gamma}^{\text{CP}} \epsilon_{\gamma\gamma}^{\text{SM,eff}} \frac{e^2 Q_e Q_\mu}{q_1^2 q_2^2} \right) \frac{\epsilon^{\alpha\beta\rho\sigma} q_{2\rho} q_{1\sigma}}{m_Z^2} \right]$$

$$\Gamma(h \rightarrow Z\gamma)$$

$$\Gamma(h \rightarrow \gamma\gamma)$$

# “Physical” PO in $h \rightarrow 4\ell$

**Goal:** provide a simple interpretation for the PO.

$$\mathcal{A} = i \frac{2m_Z^2}{v_F} (\bar{e}\gamma_\alpha e)(\bar{\mu}\gamma_\beta \mu) \times$$

$$\left[ \left( \kappa_{ZZ} \frac{g_Z^e g_Z^\mu}{P_Z(q_1^2) P_Z(q_2^2)} + \frac{\epsilon_{Ze} g_Z^\mu}{m_Z^2 P_Z(q_2^2)} + \frac{\epsilon_{Z\mu} g_Z^e}{m_Z^2 P_Z(q_1^2)} \right) g^{\alpha\beta} + \right.$$

$$+ \left( \epsilon_{ZZ} \frac{g_Z^e g_Z^\mu}{P_Z(q_1^2) P_Z(q_2^2)} + \kappa_{Z\gamma}^{\text{SM,eff}} \left( \frac{eQ_\mu g_Z^e}{q_2^2 P_Z(q_1^2)} + \frac{eQ_e g_Z^\mu}{q_1^2 P_Z(q_2^2)} \right) + \kappa_{\gamma\gamma}^{\text{SM,eff}} \frac{e^2 Q_e Q_\mu}{q_1^2 q_2^2} \right) \frac{q_1 \cdot q_2 g^{\alpha\beta} - q_2^\alpha q_1^\beta}{m_Z^2} +$$

$$\left. + \left( \epsilon_{ZZ}^{\text{CP}} \frac{g_Z^e g_Z^\mu}{P_Z(q_1^2) P_Z(q_2^2)} + \lambda_{Z\gamma}^{\text{CP,SM,eff}} \left( \frac{eQ_\mu g_Z^e}{q_2^2 P_Z(q_1^2)} + \frac{eQ_e g_Z^\mu}{q_1^2 P_Z(q_2^2)} \right) + \lambda_{\gamma\gamma}^{\text{CP,SM,eff}} \frac{e^2 Q_e Q_\mu}{q_1^2 q_2^2} \right) \frac{\epsilon^{\alpha\beta\rho\sigma} q_{2\rho} q_{1\sigma}}{m_Z^2} \right]$$

Single Z-pole.

Decay width if only the contact term is present:

$$\Gamma(h \rightarrow Z\ell^+\ell^-) = 0.0366 |\epsilon_{Z\ell}|^2 \text{ MeV}$$

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$$\left[ \left( \kappa_{ZZ} \frac{g_Z^e g_Z^\mu}{P_Z(q_1^2) P_Z(q_2^2)} + \frac{\epsilon_{Ze}}{m_Z^2} \frac{g_Z^\mu}{P_Z(q_2^2)} + \frac{\epsilon_{Z\mu}}{m_Z^2} \frac{g_Z^e}{P_Z(q_1^2)} \right) g^{\alpha\beta} + \right.$$

$$+ \left( \epsilon_{ZZ} \frac{g_Z^e g_Z^\mu}{P_Z(q_1^2) P_Z(q_2^2)} + \kappa_{Z\gamma}^{\text{SM,eff}} \left( \frac{eQ_\mu g_Z^e}{q_2^2 P_Z(q_1^2)} + \frac{eQ_e g_Z^\mu}{q_1^2 P_Z(q_2^2)} \right) + \kappa_{\gamma\gamma}^{\text{SM,eff}} \frac{e^2 Q_e Q_\mu}{q_1^2 q_2^2} \right) \frac{q_1 \cdot q_2 g^{\alpha\beta} - q_2^\alpha q_1^\beta}{m_Z^2} +$$

$$\left. + \left( \epsilon_{ZZ}^{\text{CP}} \frac{g_Z^e g_Z^\mu}{P_Z(q_1^2) P_Z(q_2^2)} + \lambda_{Z\gamma}^{\text{CP}} \epsilon_{Z\gamma}^{\text{SM,eff}} \left( \frac{eQ_\mu g_Z^e}{q_2^2 P_Z(q_1^2)} + \frac{eQ_e g_Z^\mu}{q_1^2 P_Z(q_2^2)} \right) + \lambda_{\gamma\gamma}^{\text{CP}} \epsilon_{\gamma\gamma}^{\text{SM,eff}} \frac{e^2 Q_e Q_\mu}{q_1^2 q_2^2} \right) \frac{\epsilon^{\alpha\beta\rho\sigma} q_{2\rho} q_{1\sigma}}{m_Z^2} \right]$$

Double Z-pole.  $h \rightarrow ZZ$  not accessible kinematically.

We define the physical PO from  $h \rightarrow 2e2\mu$ :

$$\Gamma(h \rightarrow Z_L Z_L) \equiv \frac{\Gamma(h \rightarrow 2e2\mu) [\kappa_{ZZ}]}{\mathcal{B}(Z \rightarrow 2e) \mathcal{B}(Z \rightarrow 2\mu)} = 0.209 |\kappa_{ZZ}|^2 \text{ MeV}$$

$$\Gamma(h \rightarrow Z_T Z_T) \equiv \frac{\Gamma(h \rightarrow 2e2\mu) [\epsilon_{ZZ}]}{\mathcal{B}(Z \rightarrow 2e) \mathcal{B}(Z \rightarrow 2\mu)} = 0.0189 |\epsilon_{ZZ}|^2 \text{ MeV}$$

$$\Gamma^{\text{CPV}}(h \rightarrow Z_T Z_T) \equiv \frac{\Gamma(h \rightarrow 2e2\mu) [\epsilon_{ZZ}^{\text{CP}}]}{\mathcal{B}(Z \rightarrow 2e) \mathcal{B}(Z \rightarrow 2\mu)} = 0.00799 |\epsilon_{ZZ}^{\text{CP}}|^2 \text{ MeV}$$

# NLO effects in production

## QCD

As for the decay, the most important effect can be described by [soft QCD radiation](#).

Complete NLO QCD corrections, for generic PO, can be implemented in automatic tools for event generation. *Work in progress.*

[see also Maltoni, Mawatari, Zaro 1311.1829]

[NNLO corrections also dominated by real radiation effects:  
Cacciari, Dreyer, Karlberg, Salam, Zanderighi 1506.02660]

## EW

Electroweak corrections can be divided in:

- **Local contributions.** Such terms are parametrised as SM contributions to the PO  
(e.g.  $\epsilon^{SM}_{Z\gamma,\gamma\gamma}$ )
- **Non-local terms.** Unlike decay, in VBF such terms could be relevant. Would need a dedicated study.



# Precision on signal strength

| channel      | Prec. (%) 100 fb <sup>-1</sup> | Prec. (%) 300 fb <sup>-1</sup> |    | Prec. (%) 3000 fb <sup>-1</sup> |    |
|--------------|--------------------------------|--------------------------------|----|---------------------------------|----|
| ttH H→γγ     | ~65                            | 38                             | 36 | 17                              | 12 |
| ttH H→ZZ*→4l | ~85                            | 49                             | 48 | 20                              | 16 |
| VBF H→γγ     | ~80                            | 47                             | 43 | 22                              | 15 |
| VBF H→ZZ*→4l | ~60                            | 36                             | 33 | 21                              | 16 |
| H→μμ         | ~70                            | 39                             | 38 | 16                              | 12 |
| H→ττ         | ~18                            | 14                             | 8  | 8                               | 5  |
| H→bb         | ~20                            | 14                             | 11 | 7                               | 5  |
| H→γγ         | ~15                            | 12                             | 6  | 8                               | 4  |
| H→4l         | ~15                            | 11                             | 7  | 9                               | 4  |
| H→4l         | ~15                            | 11                             | 7  | 7                               | 4  |

↑ My personal estimates

**ATLAS:** experimental & theory uncertainties; **only exp. uncertainty**

**CMS:** current exp.l & theory uncertainties; **exp. uncertainty**  $\propto 1/\sqrt{L}$  and  $\frac{1}{2}$  theory unc.

ATLAS assumed luminosity uncertainty: 3%