# The $\{m_h, m_t\}$ plane: Standard Model criticality vs. high-scale SUSY





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### Motivations

In recent years, the study of Standard Model (SM) behaviour under the Renormalization Group Equation (RGE) flow has revealed an interesting peculiarity: the measured values of Higgs and Top masses lie in the narrow SM metastability region (the region where electroweak vacuum is unstable) but sufficiently long-lived compared to the age of the Universe, and the SM can be considered a viable theory up to the Planck scale). This work shows that also within the Minimal Supersymmetric Standard Model (MSSM), studied with an analogous philosophy, the measured values of  $m_h$  and  $m_t$  reveal interesting features. These features are somehow equally surprising and perhaps with more fertile implications.

# 1. Novelty of the work

## 2. Details of the performed analysis

Former works have focused their attention on single requirements (such as quartic Higgs coupling matching or gauge coupling unification) using as variables the SUSY scale  $m_s$  and/or the Higgs mass  $m_h$ , but rarely the Top mass  $m_t$ , despite many valid motivations for doing so.

Here we have **analysed the MSSM** for different plausible SUSY-breaking scales ( $m_S = 2$ , 5, 100, 1000 TeV), using the { $m_h, m_t$ } plane perspective, looking for viable configurations with simultaneous:

- gauge coupling unification
- satisfactory quartic Higgs coupling ( $\lambda$ ) matching
- natural parameters configuration at the GUT scale
- Radiatively realised ElectroWeak Symmetry Breakdown (REWSB)



# 3. Results in a low-scale SUSY scenario

**Results** for  $m_S = 5$  TeV:



- Many factors contribute to the final shape:
- I. For higher  $m_t$ ,  $\lambda(m_s)$  becomes negative
- II. For higher  $m_t$ ,  $y_t(\mu)$  develop a Landau pole before *m<sub>GUT</sub>*

# 4. Changing the analysis parameters

By modifying the analysis parameters and observing the effects, we get a deeper understanding of the physics that originates the borders:

#### Enlarged natural range at $m_{GUT}$



#### Reduced $\lambda$ -matching tolerance



III. For higher  $m_h$ ,  $\lambda(m_s)$  becomes too big IV. For lower  $m_t$  / higher  $m_h$ , EWSB and  $\lambda(m_s)$  matching are incompatible V. For lower  $m_t$ , EWSB cannot be

radiatively induced

VI. For  $m_S = 5$  TeV, the measured  $\{m_h, m_t\}$  values are allowed by a naïve analysis, but excluded by our more sophisticated analysis.

# 5. Comparison for different SUSY scales

By comparing the results for different SUSY scales we can better appreciate the peculiar position of the SM in the space of possible vacua.



- I.  $m_S > 2$  TeV, due to direct searches bounds
  - $m_S < 10^6 \,\text{GeV}$ , otherwise gauge coupling unification is spoiled
- II. For high  $m_t$ ,  $d\lambda(\mu)/d\mu < 0$ . Thus, for higher

### 6. Conclusions

This analysis has two important novelties:

- $m_t$  is a scanned input parameter (as  $m_h$ )
- we introduce **a Radiative EWSB** condition



 $m_S$  we have lower  $\lambda(m_S)$ , causing the observed shift to the right

- III. For low  $m_t$ ,  $d\lambda(\mu)/d\mu > 0$ . Thus, for higher  $m_S$  we have higher  $\lambda(m_S)$ , causing the observed shift to the left
- IV. For higher  $m_S$  we have lower  $y_t(m_S)$ . This makes REWSB harder to achieve
- V. The measured  $\{m_h, m_t\}$  values are found in a remarkably narrow window of the parameter space where all the imposed conditions are met for a large range of  $m_S$ values



We obtain new and interesting results:

- we reduce the allowed window for SUSY models in the  $\{m_h, m_t\}$ plane, also as a **consequence of** the **REWSB** condition.

- remarkably, the measured values still lies in the allowed window, which is **narrow in both** *m<sub>h</sub>* and *m*<sub>t</sub> directions.

It can be appreciated that this coincidence is perhaps as strong and surprising as for the SM vacuum metastability.