

# Flavour Anomalies: stepping stones to New Physics?



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## **stepping stone**

*/ˈstɛpɪŋ stəʊn/*

*noun*

*plural noun: stepping stones*

a raised stone used singly or in a series as a place on which to step when crossing a stream or muddy area.

- an action or event that helps one to make progress towards a specified goal.

*U. Zurich - 12/10/2021*

The ***Standard Model of particle physics*** describes a huge variety of phenomena in a unified and simple theory.

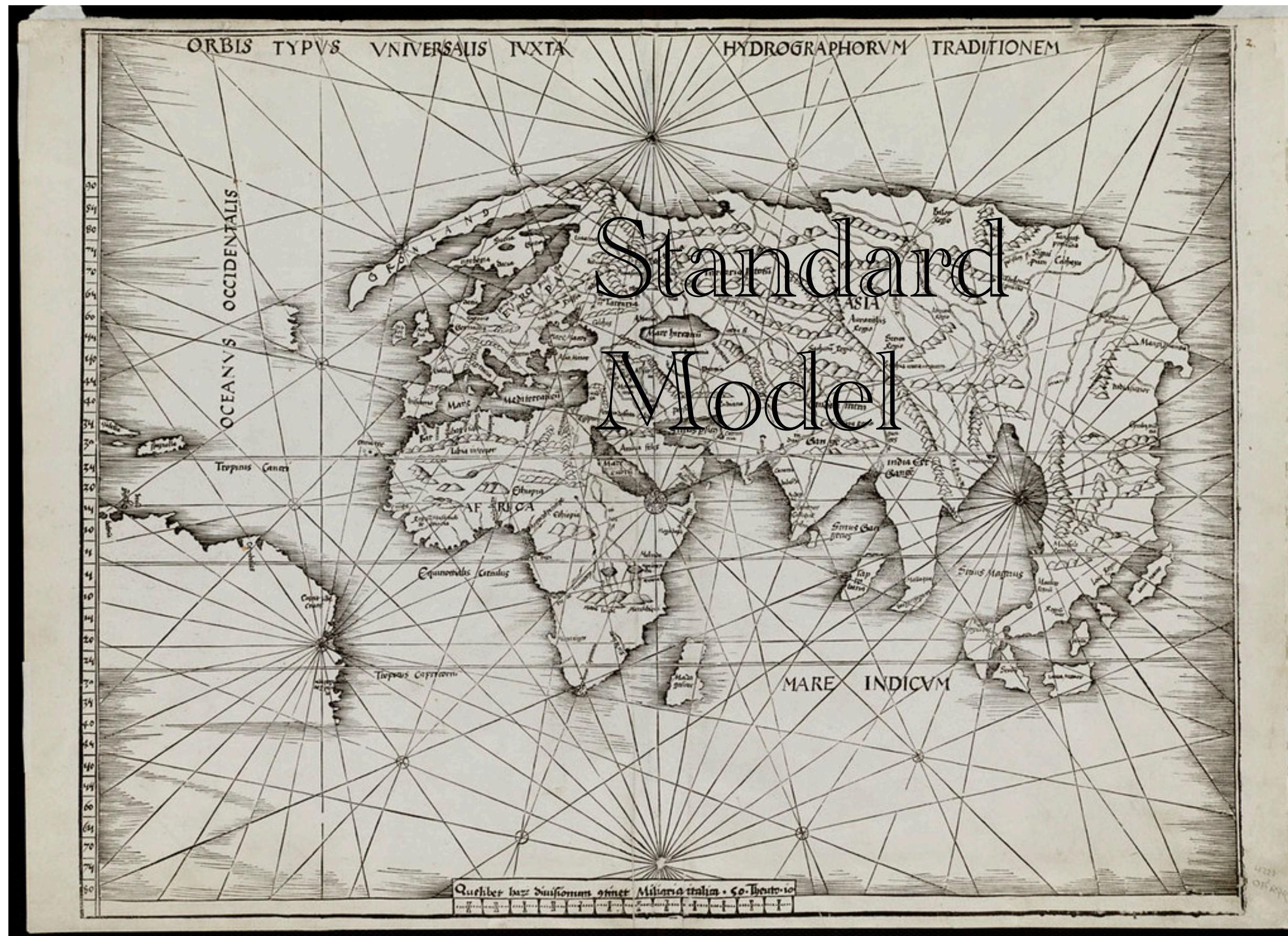
However, we know it **must be extended** at some energy scales:

- neutrino masses
- astrophysical/cosmological obs.

(dark matter, dark energy, baryonic asymmetry, inflation)

Our desire for *simplicity* and a sense of *beauty* also motivates extensions of the SM for other reasons:

- hierarchy problem of the EW scale (and CC)
- understanding the hierarchies in fermion masses and mixings
- unification of gauge interactions and fermion representations
- understanding the smallness of CP-violation in strong interactions



Many experiments are exploring the *terra incognita* in all possible directions, but we still don't have a confirmed discovery of a new land.



... every once in a while, possible land is sighted.



Some of these *anomalies* might just be mirages, however some could also be the first genuine hints of a New Land.

It is important to take each into consideration, in order to understand how realistic it could be and to point out the searches in promising directions

# A selection of “anomalies” from the SM \*

\* not including cosmological anomalies from the  $\Lambda$ CDM

## Flavour Anomalies

This talk



$$b \rightarrow s \ell \ell$$

$$pp \rightarrow e^+ e^-$$

$$\gamma\gamma @ 750 \text{ 151 GeV}$$

$$R(D^{(*)})$$

Standard Model

$$(g-2)_\mu$$

Neutrino anomalies:  
LSND, Miniboone, reactor, Gallium  
5MeV "bump"

$$(g-2)_e$$

Cabibbo Angle

Atomki: 17 MeV excess in  $^8\text{Be}$  decays

No viable NP

~~$$B_q \rightarrow D_q^{(*)+} \pi^- (K^-)$$~~

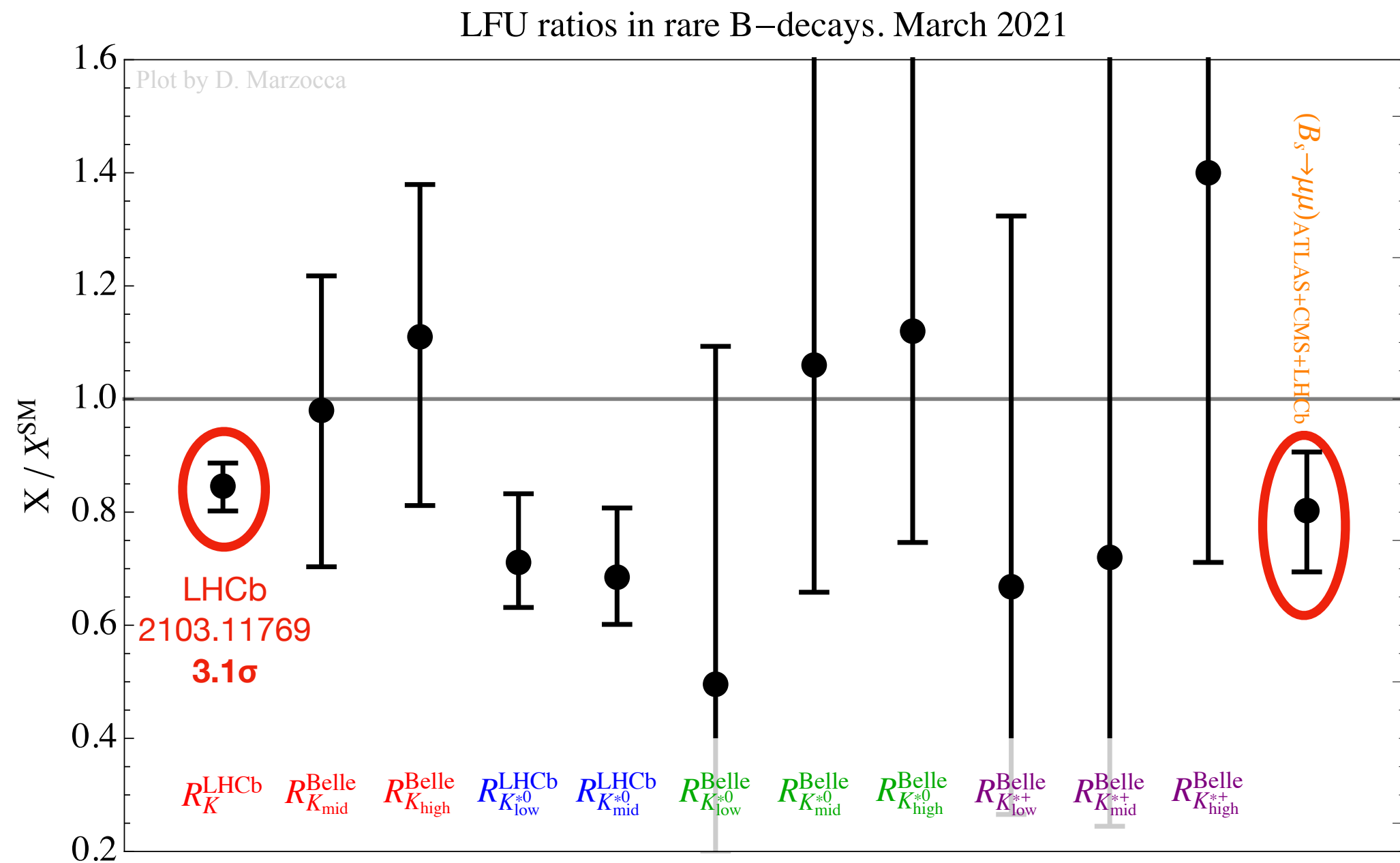
Bordone, Greljo, DM [2103.10332]

~~$$B_{d,s} \rightarrow K^{*0} \bar{K}^{*0}$$~~

Alguerò et al. [2011.07867]

# $R_K$ and the other $b \rightarrow s \mu^+ \mu^-$ probes

Compilation of “clean” observables

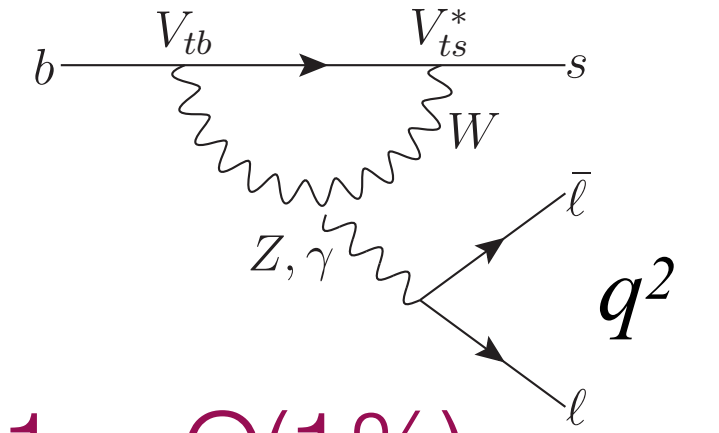


Also the leptonic decay  $B_s \rightarrow \mu^+ \mu^-$  can be predicted precisely in the SM, and is measured by ATLAS, CMS, and LHCb.

It shows a consistent reduction w.r.t. the SM.

Lepton Flavour Universality (LFU) ratios

$$R_H \equiv \frac{\int_{q^2_{\min}}^{q^2_{\max}} \frac{d\mathcal{B}(B \rightarrow H \mu^+ \mu^-)}{dq^2} dq^2}{\int_{q^2_{\min}}^{q^2_{\max}} \frac{d\mathcal{B}(B \rightarrow H e^+ e^-)}{dq^2} dq^2}$$

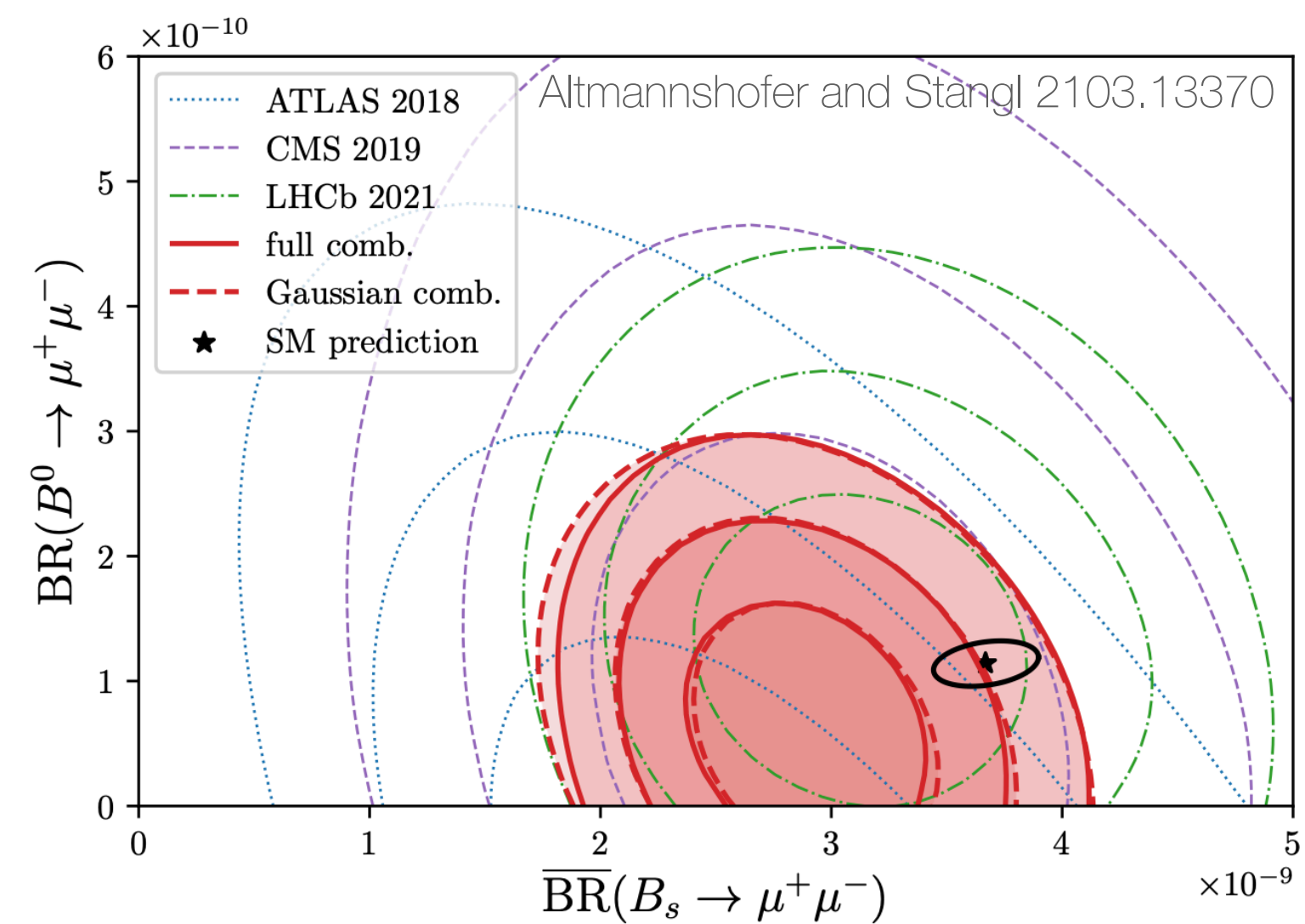


SM  $= 1 \pm O(1\%)$   
for  $q^2 \gtrsim 1 \text{ GeV}^2$   
Bordone, Isidori, Pattori [1605.07633]

E.g. the most recent one from LHCb [2103.11769]

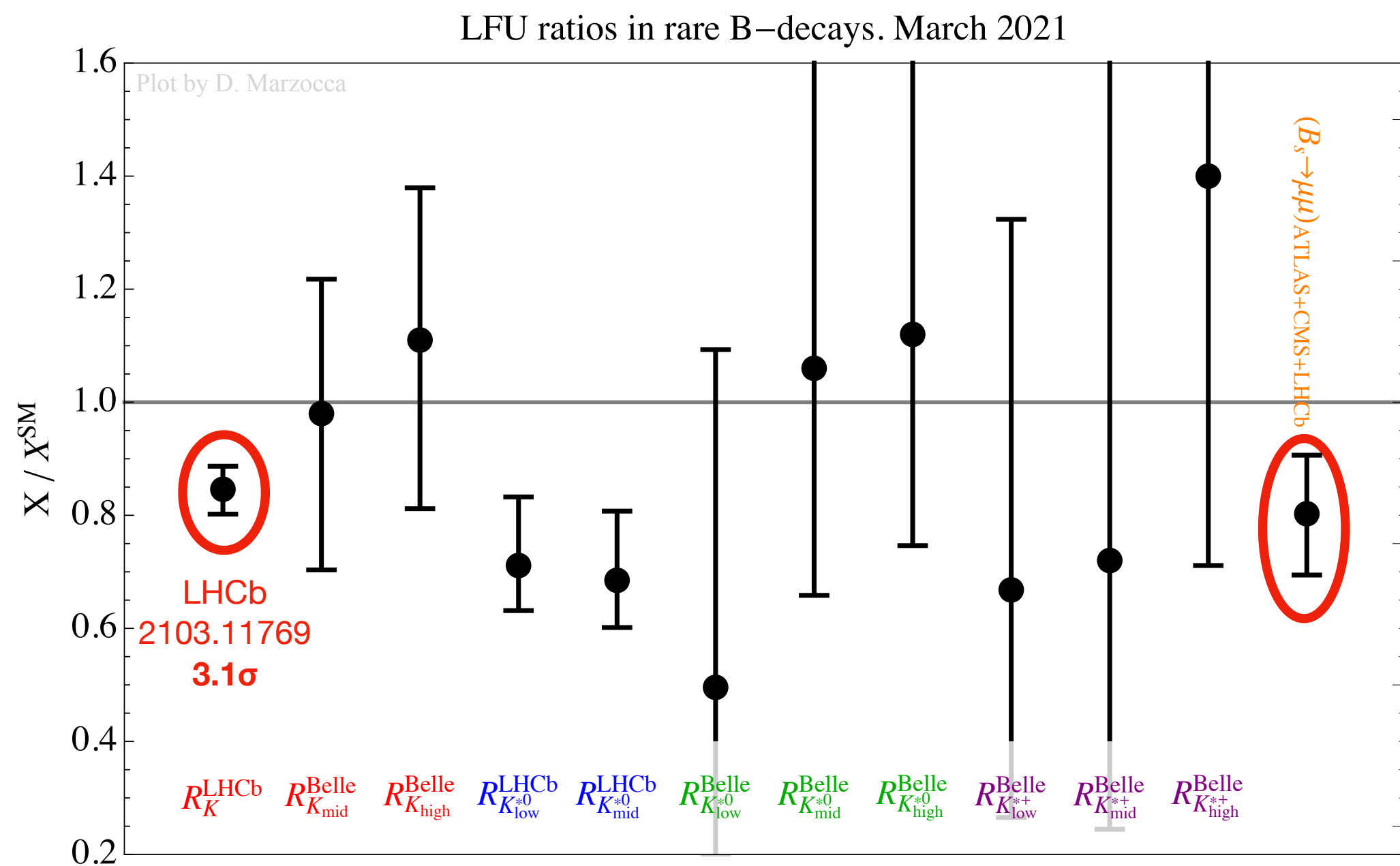
$$R_K(1.1 < q^2 < 6.0 \text{ GeV}^2/c^4) = 0.846^{+0.042}_{-0.039} {}^{+0.013}_{-0.012}$$

$3.1\sigma$

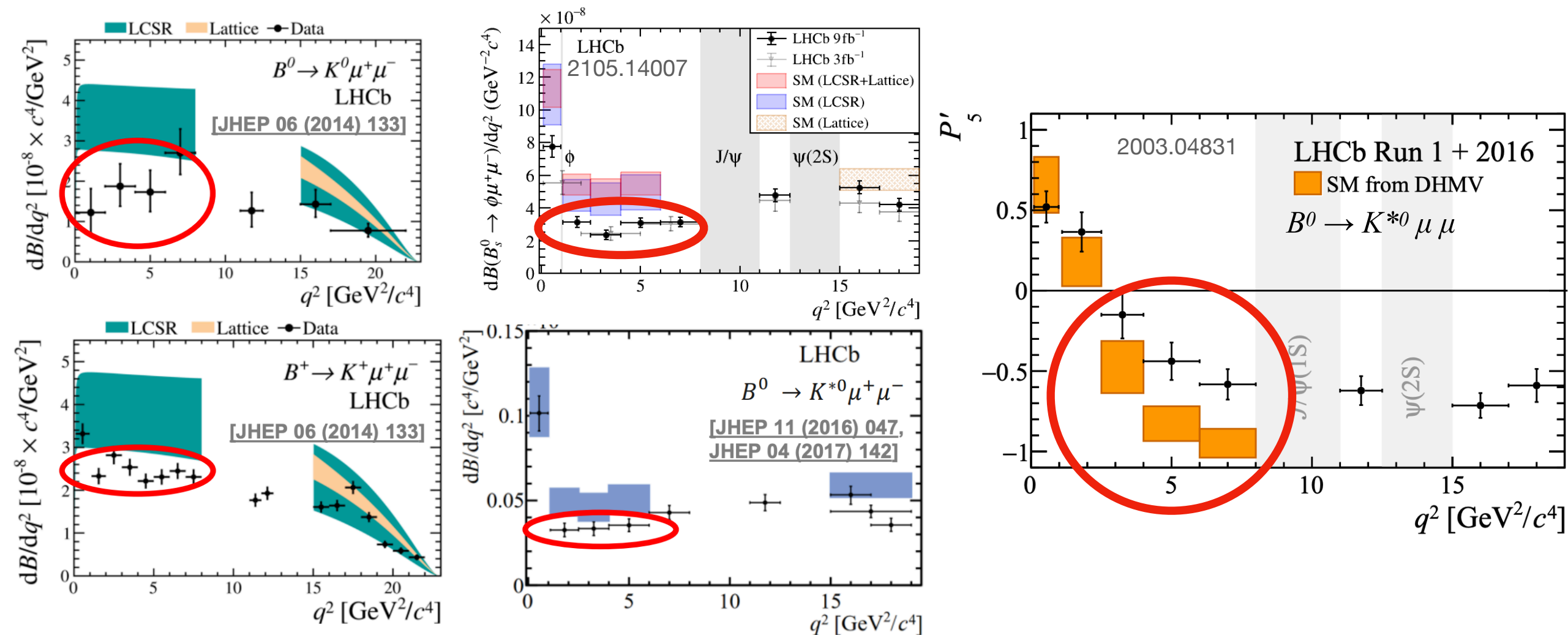


# $R_K$ and the other $b \rightarrow s \mu^+ \mu^-$ probes

Compilation of “clean” observables



Angular observables and Br's



Specific NP hypothesis, with less conservative estimates of SM uncertainties show significances in the 5.9 - 7 $\sigma$  range.

Altmannshofer and Staub [2103.13370], Algueró et al. [2104.08921], Geng et al. [2103.12738]

The global significance of the **New Physics hypothesis** in  $b \rightarrow s \mu^+ \mu^-$  (very conservative SM uncertainties estimate) is:

**3.9 $\sigma$**

Lancierini, Isidori, Owen, Serra [2104.05631]

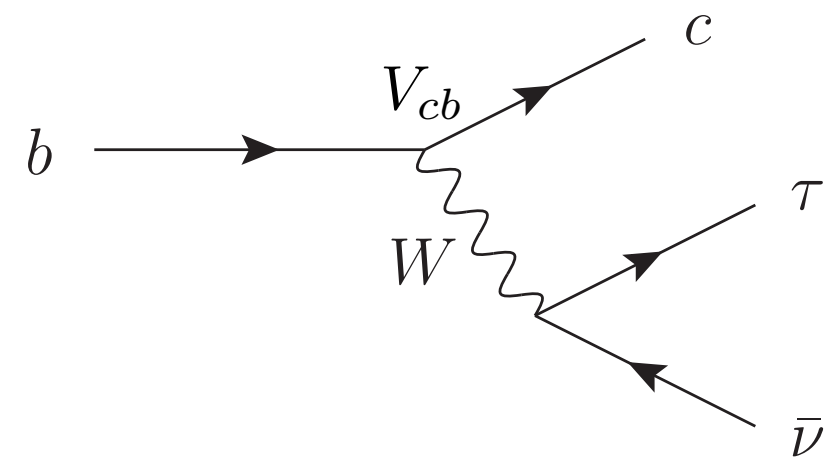
Very good fit to all these deviations with:

$$\mathcal{L}_{\text{LCFT}} = C_{S_{bc\mu\mu}} (\bar{s}_L \gamma_\mu b_L) (\bar{\mu}_L \gamma^\mu \mu_L)$$

$$C_{S_{bc\mu\mu}} \approx (37 \text{ TeV})^{-2}$$

# Charged-current B-anomalies

$b \rightarrow c \tau \nu$  vs.  $b \rightarrow c \ell \nu$



$$R(D^{(*)}) \equiv \frac{\mathcal{B}(B^0 \rightarrow D^{(*)+} \tau \nu)}{\mathcal{B}(B^0 \rightarrow D^{(*)+} \ell \nu)}, \quad \ell = \mu, e$$

$\sim 14\%$  enhancement from the SM

$\sim 3\sigma$  from the SM ( $3.7\sigma$  when combined)

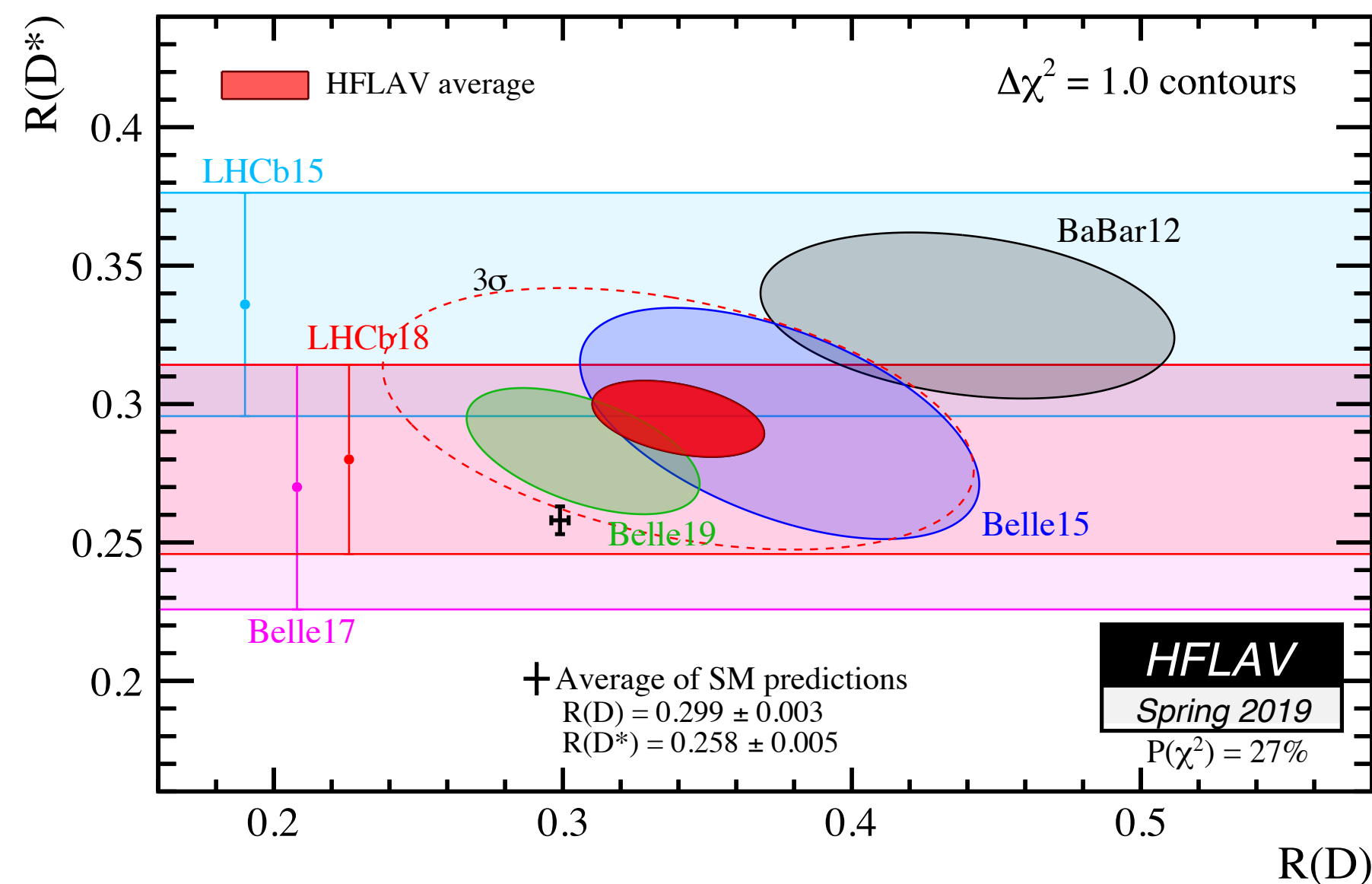
While  $\mu/e$  universality well tested

$$R(D)^{\mu/e} = 0.995 \pm 0.045$$

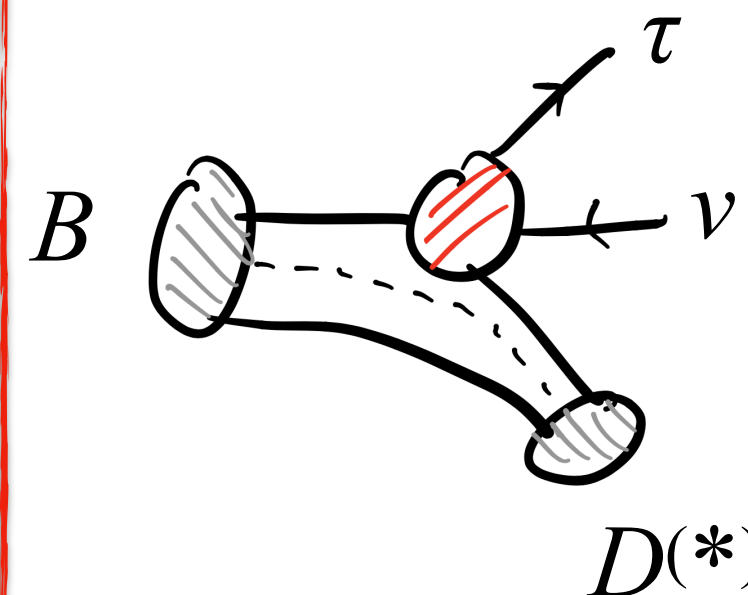
Belle - [1510.03657]

**Tree-level** SM process with  $V_{cb}$  suppression.

All measurements since 2012 consistently above the SM predictions



New Physics interpretations (LEFT):



$$\mathcal{O}_{V_L} = (\bar{c} \gamma_\mu P_L b) (\bar{\tau} \gamma^\mu P_L \nu)$$

and/or

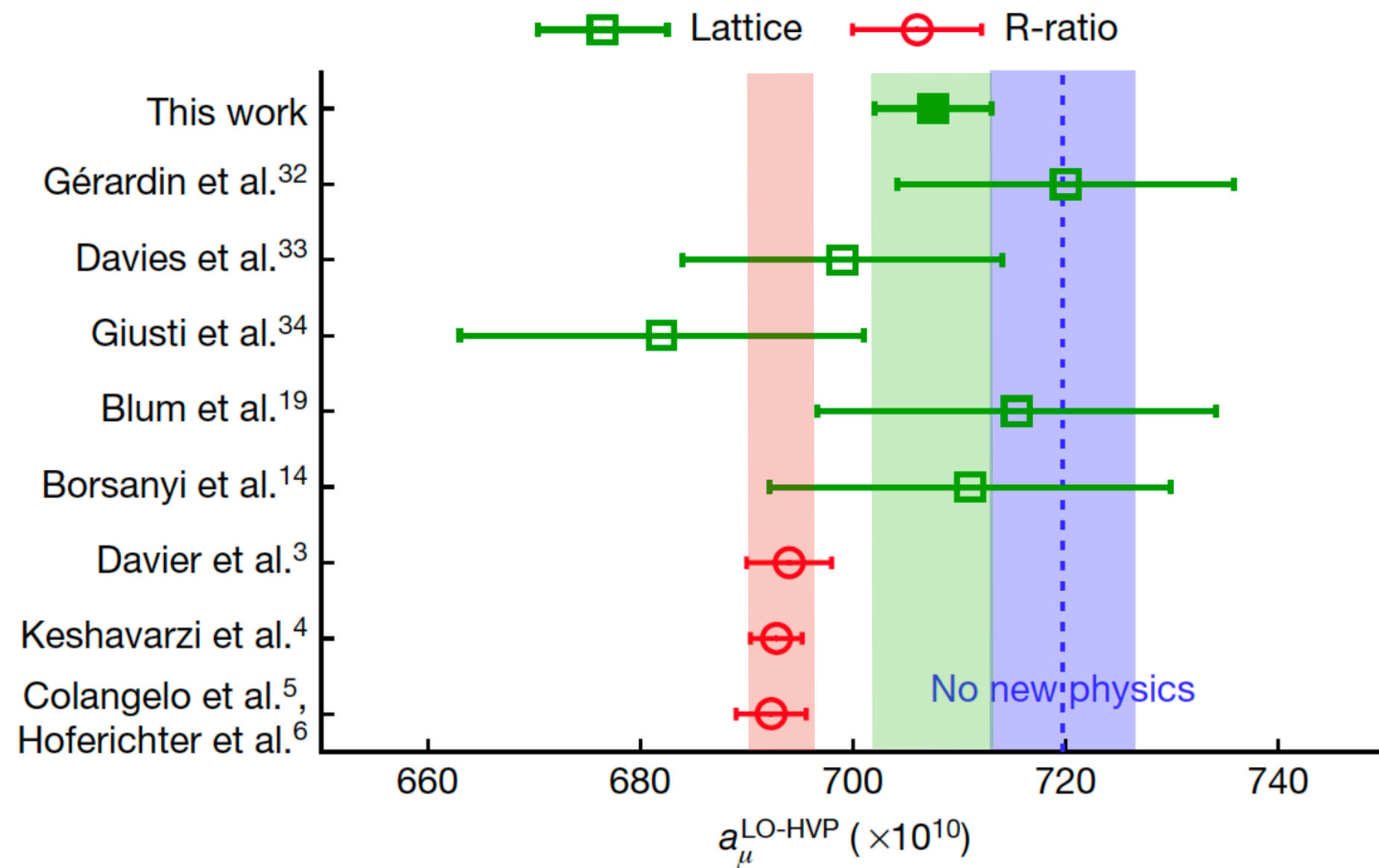
$$\mathcal{O}_{S_L} = (\bar{c} P_L b) (\bar{\tau} P_L \nu),$$

$$\mathcal{O}_T = (\bar{c} \sigma^{\mu\nu} P_L b) (\bar{\tau} \sigma_{\mu\nu} P_L \nu)$$

With a **New Physics scale** of

$$C_{cb\tau\nu} \sim (4 \text{ TeV})^{-2}$$

# Muon g-2



$$a_\mu^{\text{exp}} = (11659\mathbf{2061} \pm \mathbf{41}) \times 10^{-11} \text{ FNAL '21 + BNL '04}$$

$$a_\mu^{\text{THin}} = (11659\mathbf{1810} \pm \mathbf{43}) \times 10^{-11} \text{ TH initiative WP 2006.04822}$$

$$a_\mu^{\text{BMW}} = (11659\mathbf{1954} \pm \mathbf{55}) \times 10^{-11} \text{ Borsanyi et al. Nature 2021, 2002.12347}$$

**4.2σ** or **1.6σ** ??

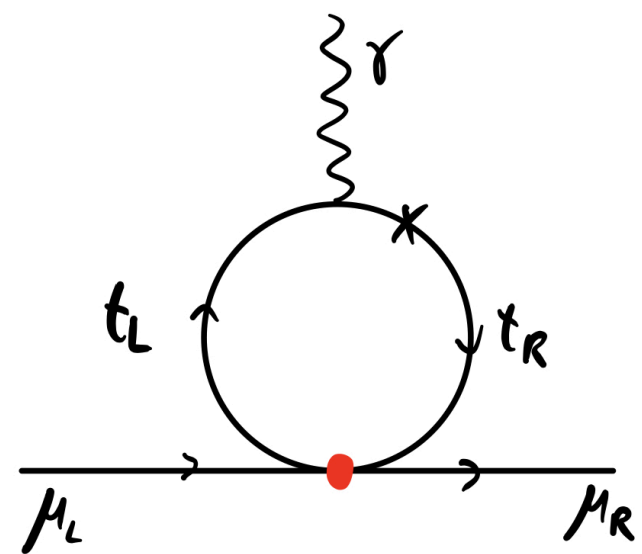
Let us entertain the possibility that the 4.2σ deviation is real.

**New physics** contribution arises via the **dipole operator**:

$$\Delta a_\mu = \frac{4W_f}{e} \text{Re} [L_{e\gamma}(W_f)]_{\mu\mu}$$

$$[O_{e\gamma}]_{\alpha\beta} = \bar{e}_L^\alpha \sigma^{\mu\nu} e_R^\beta F_{\mu\nu}$$

NP is enhanced if the chirality flip happens in an internal line with a heavy fermion, as the top quark:



semileptonic tensor  
dim-6 operator  
with top quark

$$C_{lequ}^{(3)} = (\bar{l}_L \sigma^{\mu\nu} e_R) (\bar{q}_L \sigma^{\mu\nu} u_R)$$

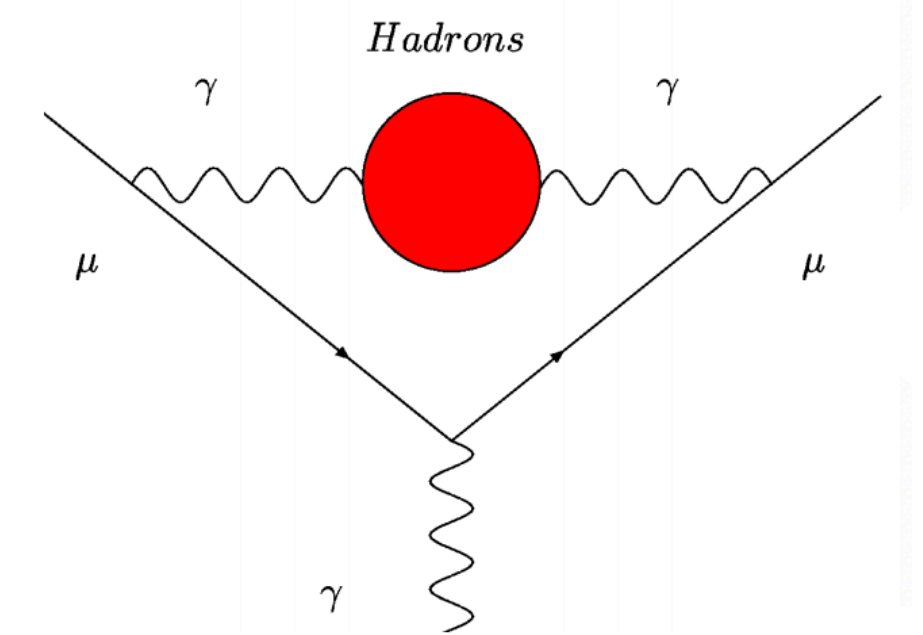
To fit the deviation (I put  $\Lambda=2\text{TeV}$  in the log):

$$C_{lequ}^{(3)}(2\text{TeV}) \approx - \frac{1}{(83\text{TeV})^2}$$

**The same structure of operator can also help in R(D<sup>\*</sup>): possible connection?**

$$[L_{e\gamma}(W_{EW})]_{\mu\mu} = - \frac{e N_c W_t}{6\pi^2} [C_{lequ}^{(3)}(\Lambda)]_{\mu\mu tt} \log \frac{\Lambda^2}{W_t^2}$$

Main Th. uncertainty in HVP LO contribution:





# Cabibbo Angle Anomaly

SGPR 1807.10197,  
Belfatto, Beradze, Berezhiani 1906.02714,  
Grossmann, Passermar, Schacht 1911.07821

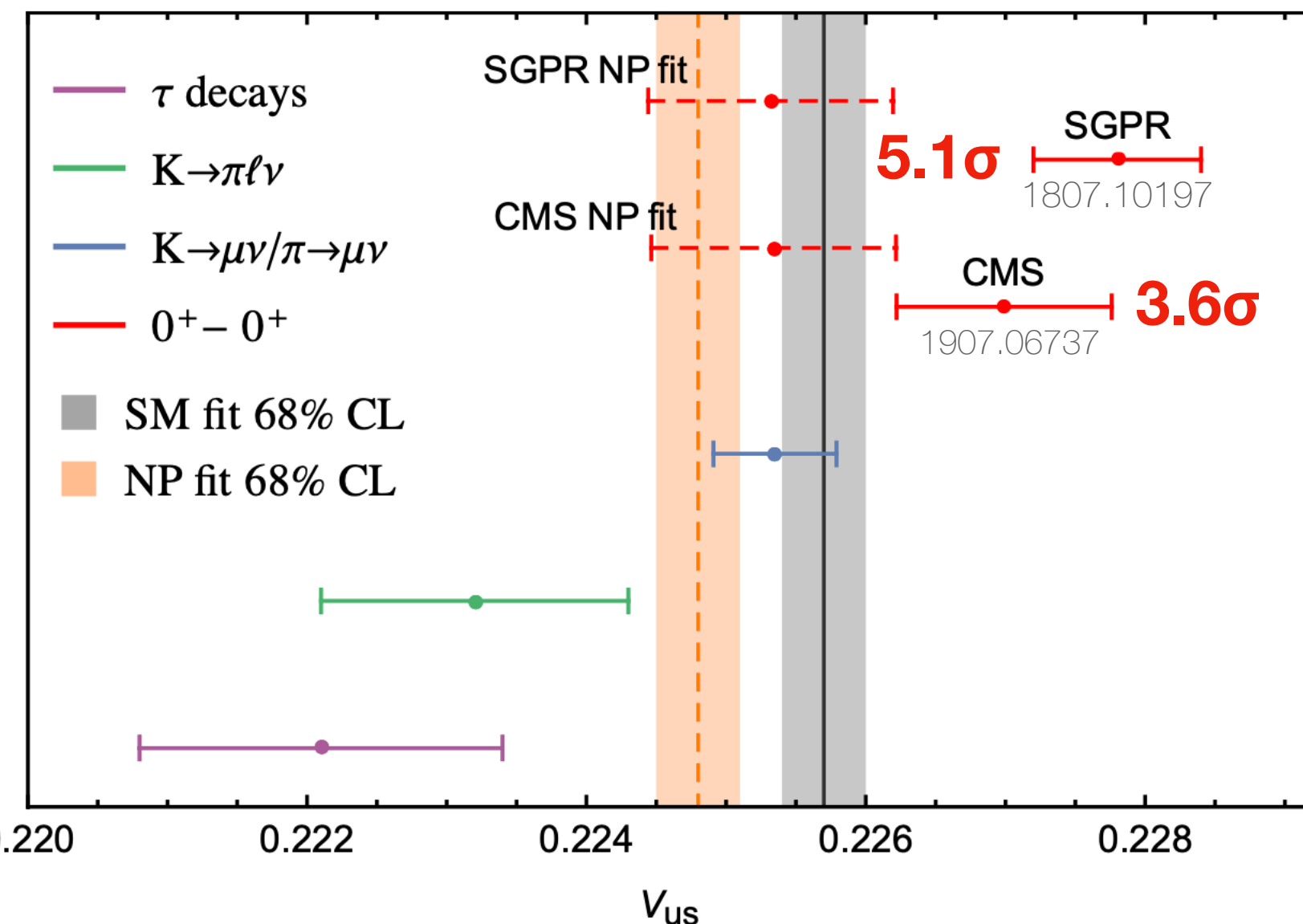
Unitarity of the first row of the CKM matrix:  $|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1$

Neglecting the very small  $V_{ub}$ :  $V_{ud}^2 + V_{us}^2 = 1$

Assuming unitarity, we can extract the Cabibbo angle from:

- $V_{ud}$ : superallowed  $0^+ \rightarrow 0^+$   $\beta$ -decays. SGPR 1807.10197, CMS 1907.06737
- $V_{us}$ : semileptonic  $K\ell 3$  decays.
- $|V_{us}|/|V_{ud}|$ :  $(K \rightarrow \mu\nu) / (\pi \rightarrow \mu\nu)$ .
- $\tau$  decays

The effect is *very small*: **(few)  $\times 10^{-3}$**  of the SM, but **SM is large**: tree x Cabibbo.



Coutinho, Crivellin, Manzari 1912.08823

Possible New Physics: *deviation in the muon decay*: mismatch from  $G_F$  and  $G_\mu$

$$G_\mu = G_F (1 + \delta_\mu)$$

This modifies the  $|V_{us}| = 0.22333(60) \times (1 + \delta_\mu)$

decays as:

1906.02714

$$|V_{us}/V_{ud}| = 0.23130(50)$$

$$|V_{ud}| = 0.97370(14) \times (1 + \delta_\mu)$$

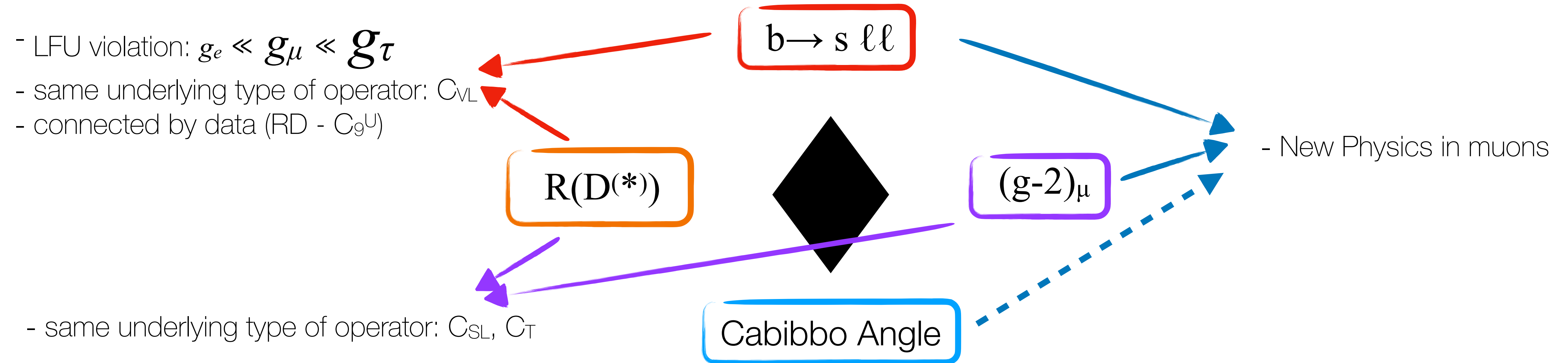
Enhancement  $\sim 20!$

$$|V_{us}| = |V_{us}^{(0)}| \left( 1 - \frac{|V_{ud}^{(0)}|^2}{|V_{us}^{(0)}|^2} \delta_\mu \right)$$

Including the **EW fit constraints**:  $\delta(\mu \rightarrow e\nu\nu) = 0.00065(15)$

Belfatto, Beradze, Berezhiani 1906.02714,  
Crivellin, Kirk, Manzari, Panizzi 2012.09845, 2102.02825

# Combined explanations: why?



IF all turn out to be due to NP, a **combined explanation** could be an **elegant** and **economical** way to explain the data.

Combined explanations are typically **more constrained by data**, can provide **sharper predictions**.

# Combined interpretation of $R_K$ , $R(D^{(*)})$ , $(g-2)_\mu$

We must **start with R(D<sup>\*</sup>)**: lowest NP scale → most stringent requirements

Tree-level mediators of:

$$\mathcal{O}_{VL} = (\bar{c}\gamma_\mu P_L b)(\bar{\tau}\gamma^\mu P_L \nu)$$

and/or

$$\mathcal{O}_{SL} = (\bar{c}P_L b)(\bar{\tau}P_L \nu),$$

$$\mathcal{O}_T = (\bar{c}\sigma^{\mu\nu} P_L b)(\bar{\tau}\sigma_{\mu\nu} P_L \nu)$$

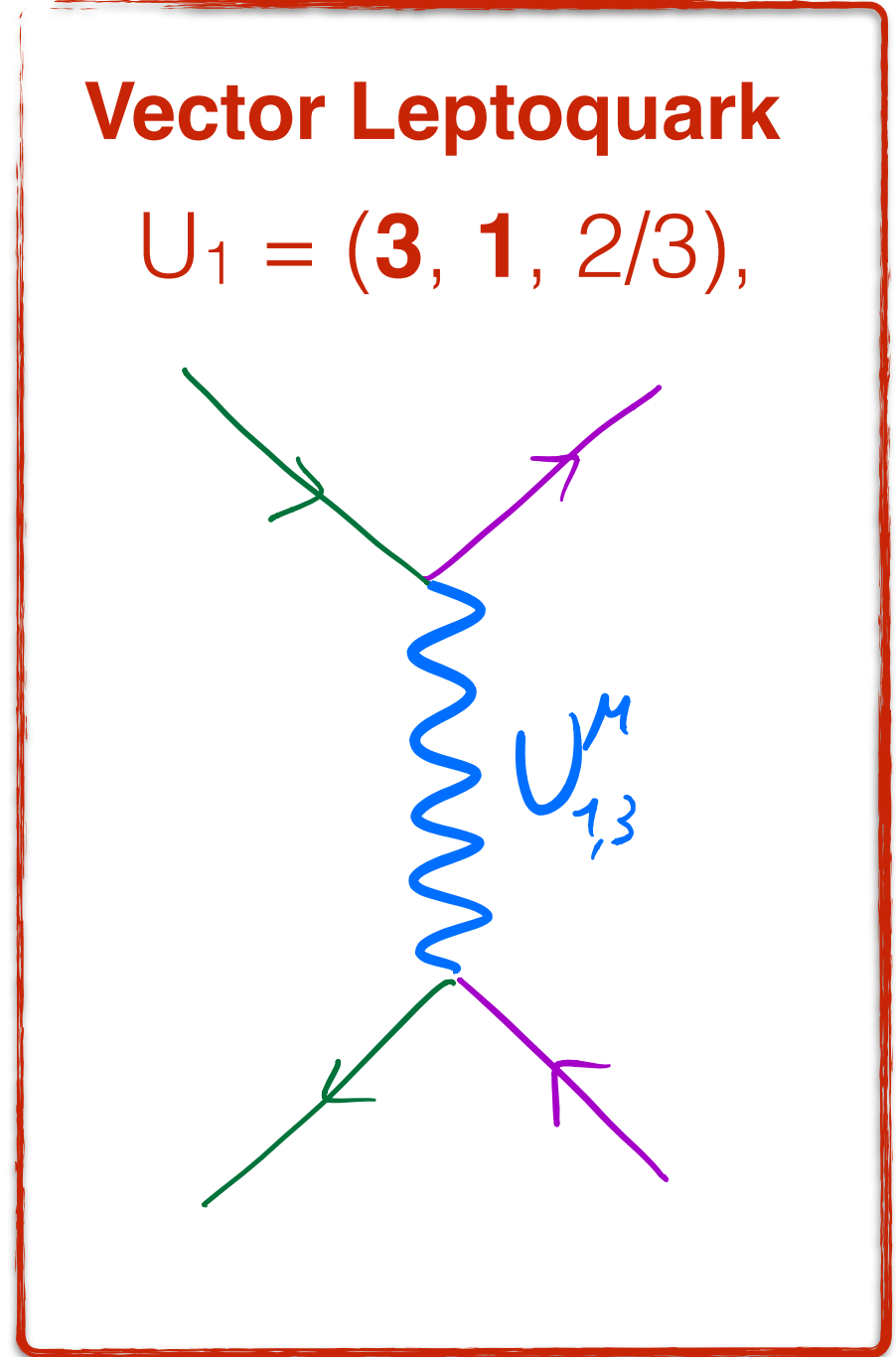
Needs to escape the constraints from:

Meson mixing

$$B \rightarrow K^{(*)} w$$

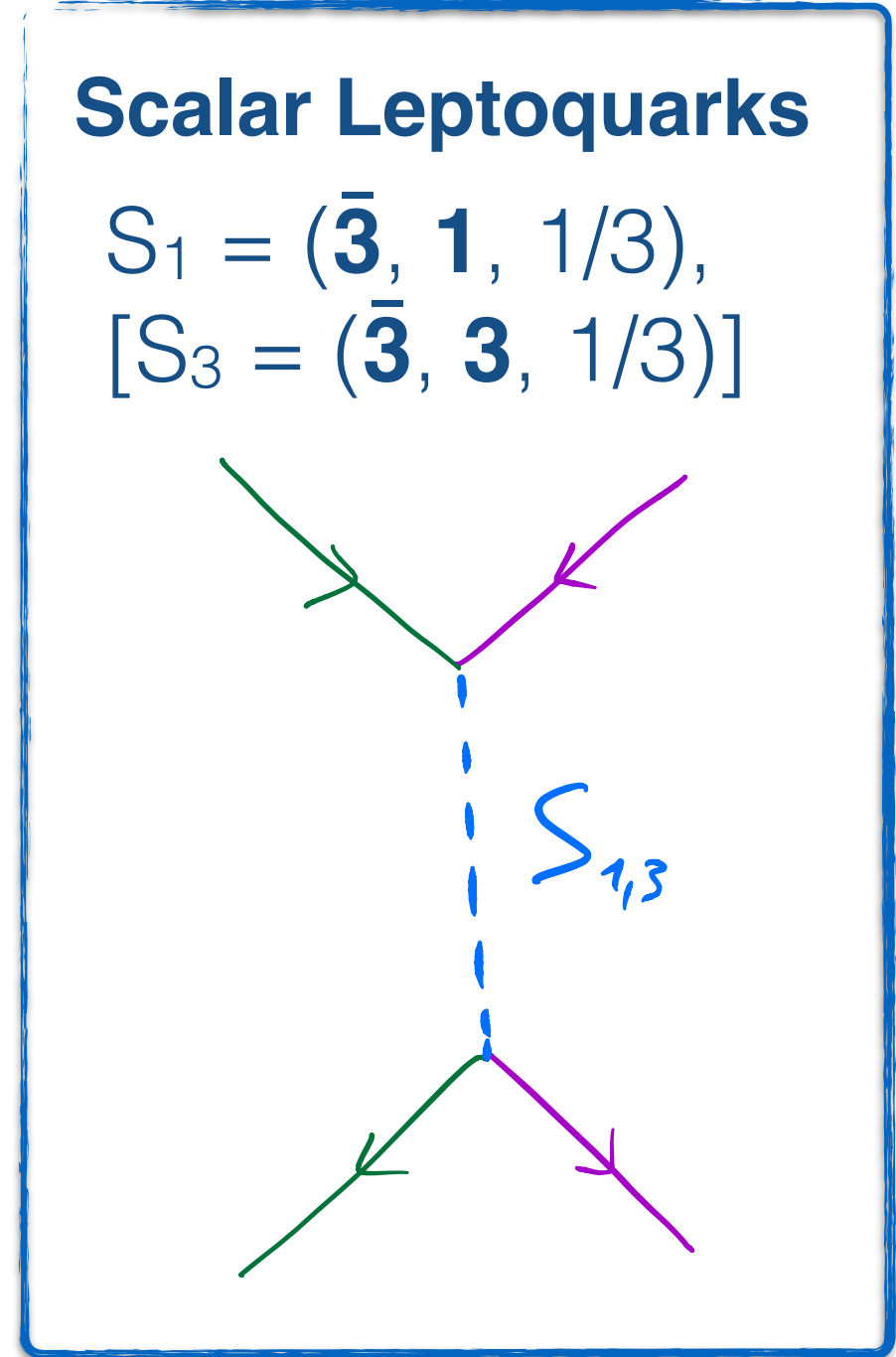
$$Z \rightarrow \tau \tau$$

$$pp \rightarrow \tau \tau$$



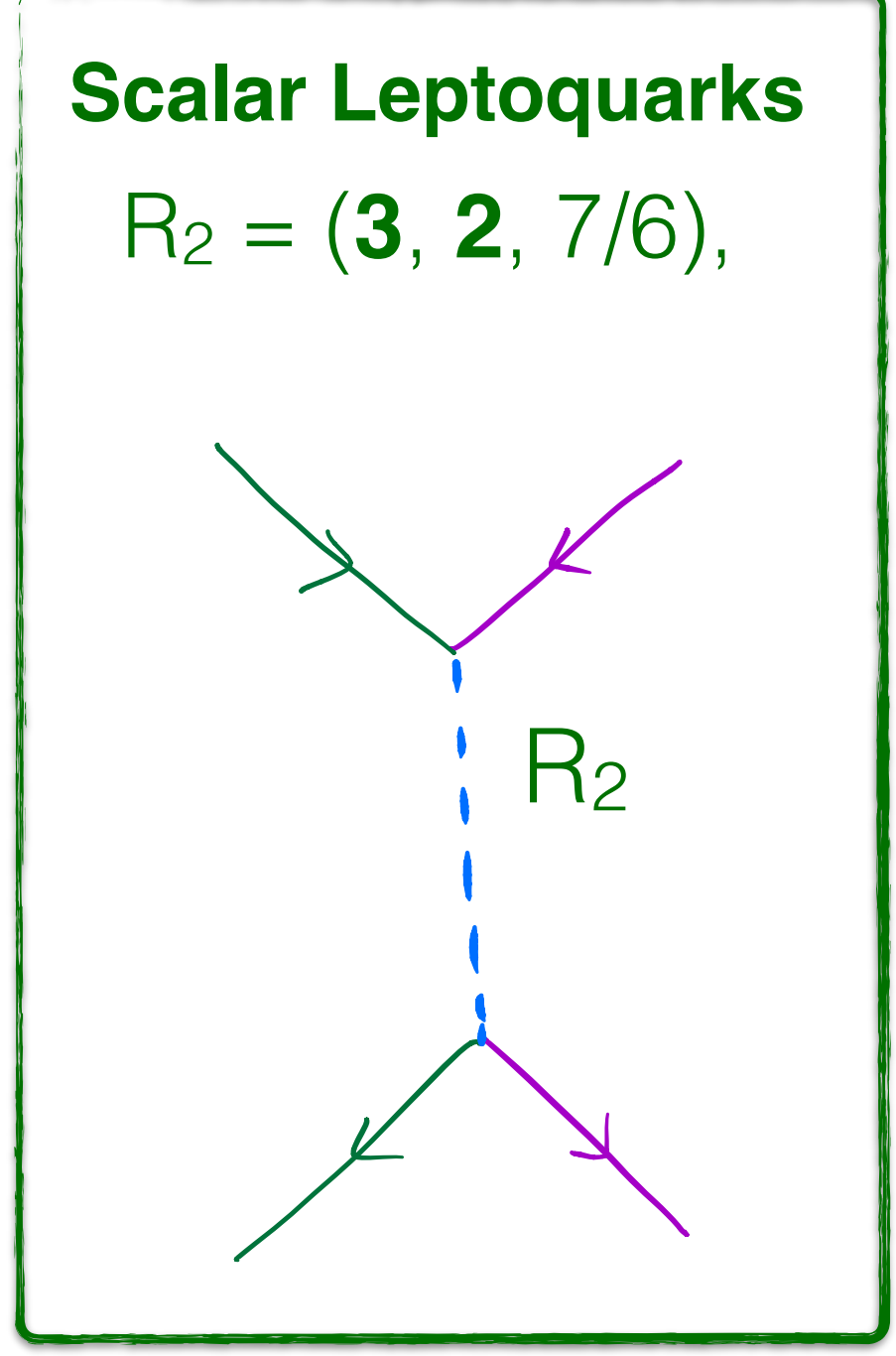
Barbieri et al 1512.01560; Buttazzo, Greljo, Isidori, DM 1706.07808; Di Luzio et al 1708.08450; Bordone et al. 1712.01368; Calibbi et al. '17; Blanke, Crivellin '18; Cornella et al 2103.16558; Angelescu et al 1808.08179

**C<sub>VL</sub>**



Crivellin et al. 1703.09226; Buttazzo, Greljo, Isidori, DM 1706.07808; D.M. 1803.10972; Arnan et al 1901.06315; Bigaran et al. 1906.01870; Crivellin et al. 1912.04224; Saad 2005.04352; V. Gherardi, E. Venturini, D.M. 2003.12525, 2008.09548; Bordone, Catà, Feldmann, Mandal 2010.03297; Crivellin et al. 2010.06593, 2101.07811; ETC...

**(C<sub>SL</sub>, C<sub>T</sub>)**



Becirevic et al. 1806.05689; Becirevic, Suresari 1704.05835; Popov et al. 1905.06339; Angelescu et al. 2103.12504; ETC...

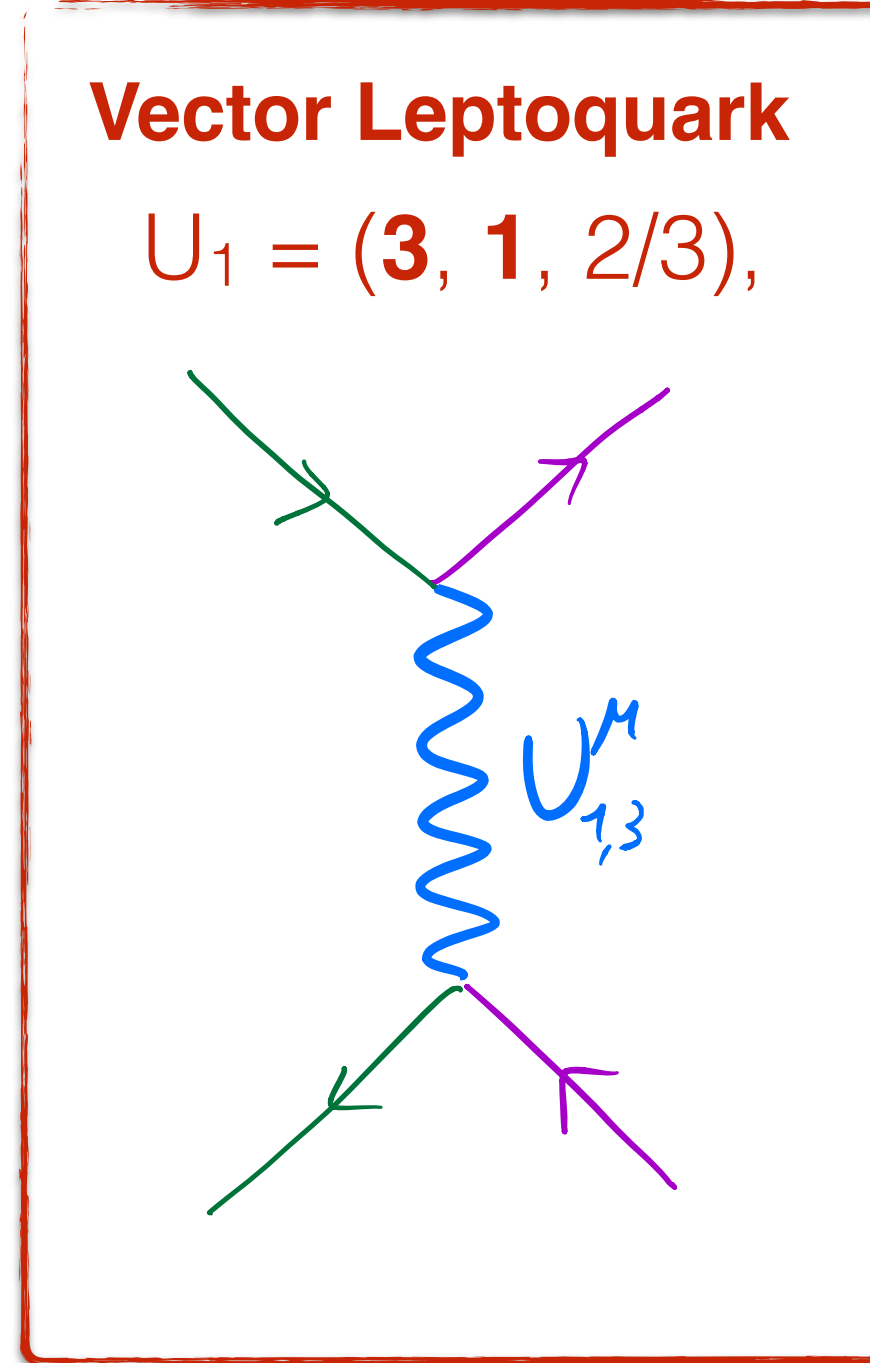
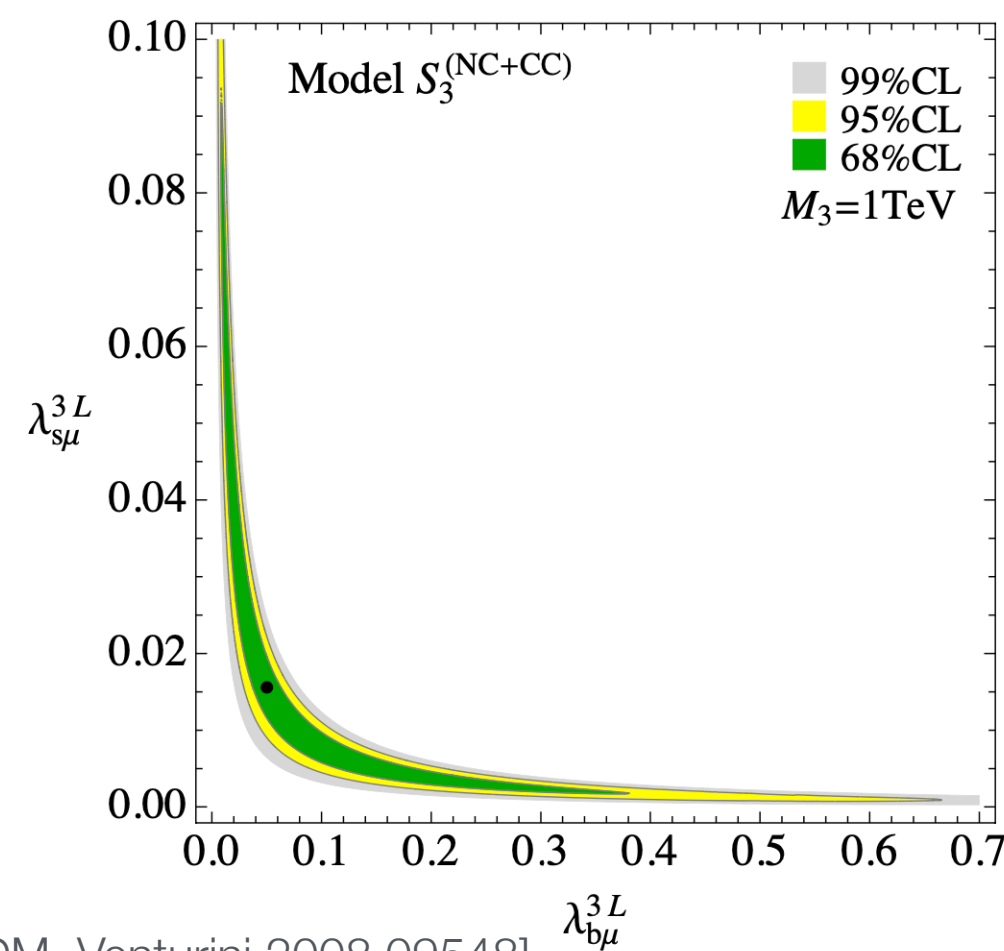
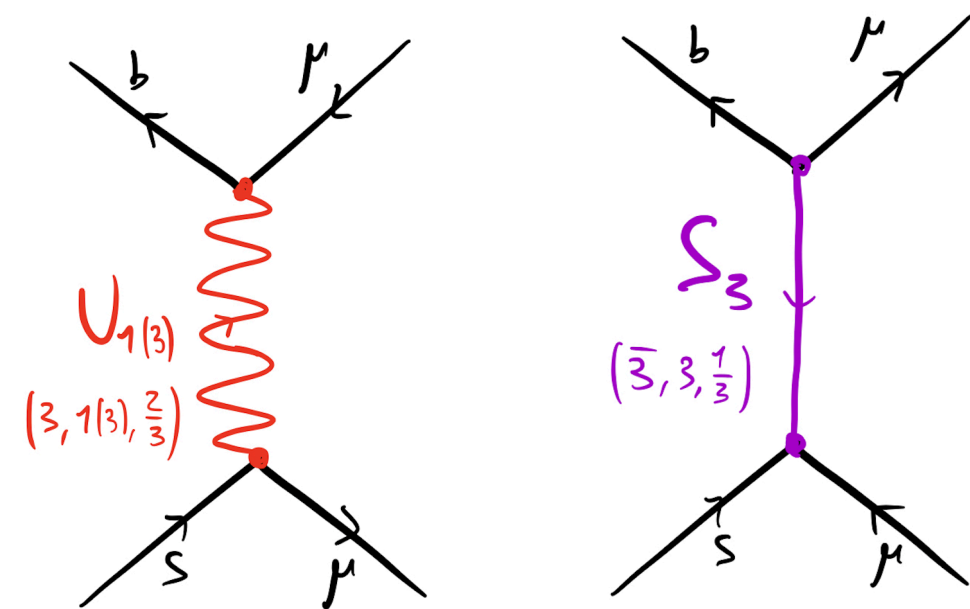
mild tension with  $Bc \rightarrow \tau \nu$  and on the verge of exclusion from mono- $\tau$  at LHC

What about **R(K<sup>\*</sup>)**?

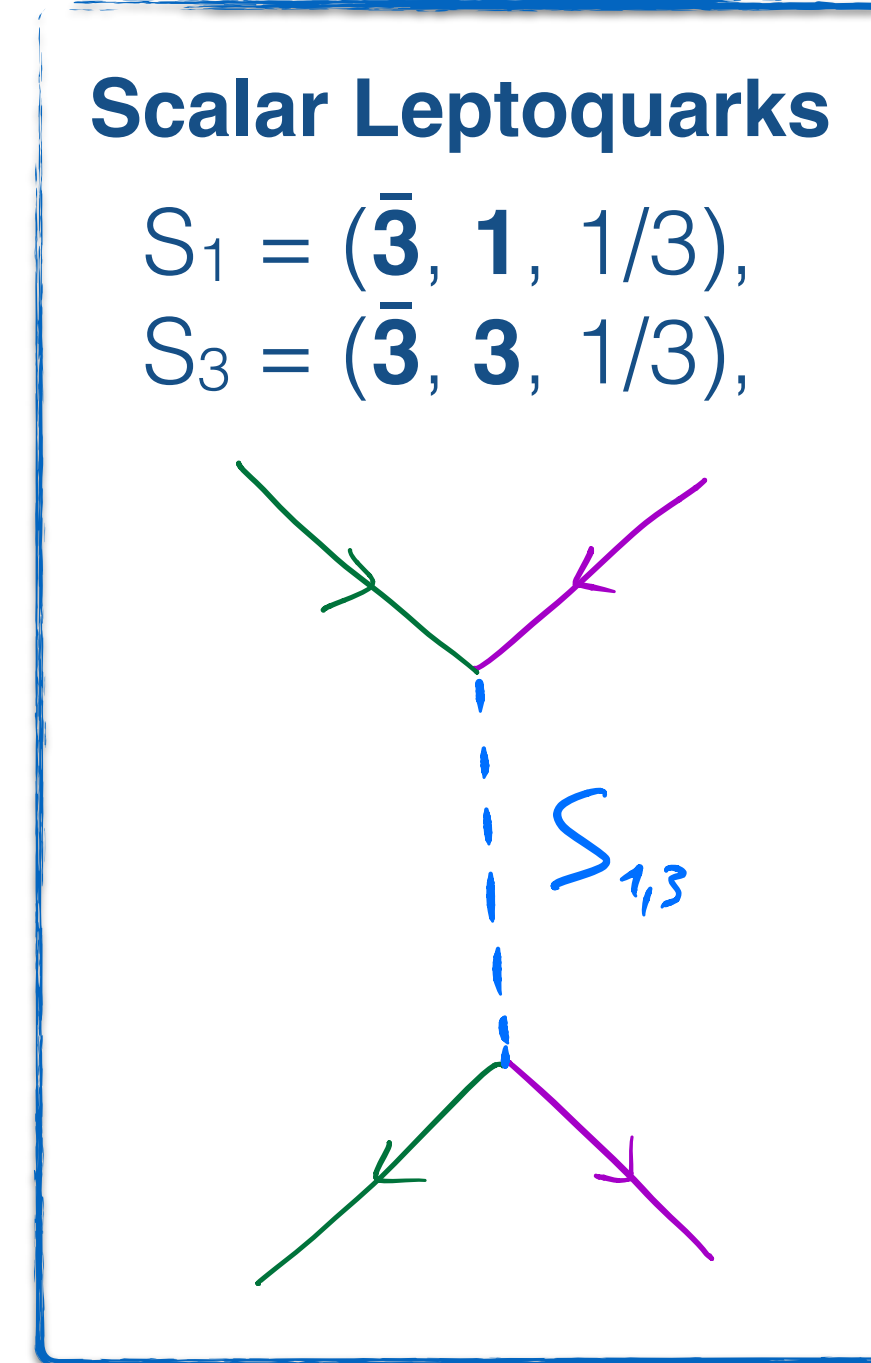
$$\mathcal{L}_{\text{eff}} \supset \frac{e^{i\alpha_{bs}}}{\Lambda_{bs}^2} (\bar{s}_L \gamma^\mu b_L) (\bar{\mu}_L \gamma_\mu \mu_L) + h.c.$$

Best-fit for  $\alpha_{bs}=0$ :  $\Lambda_{bs} \approx 37 \text{ TeV}$

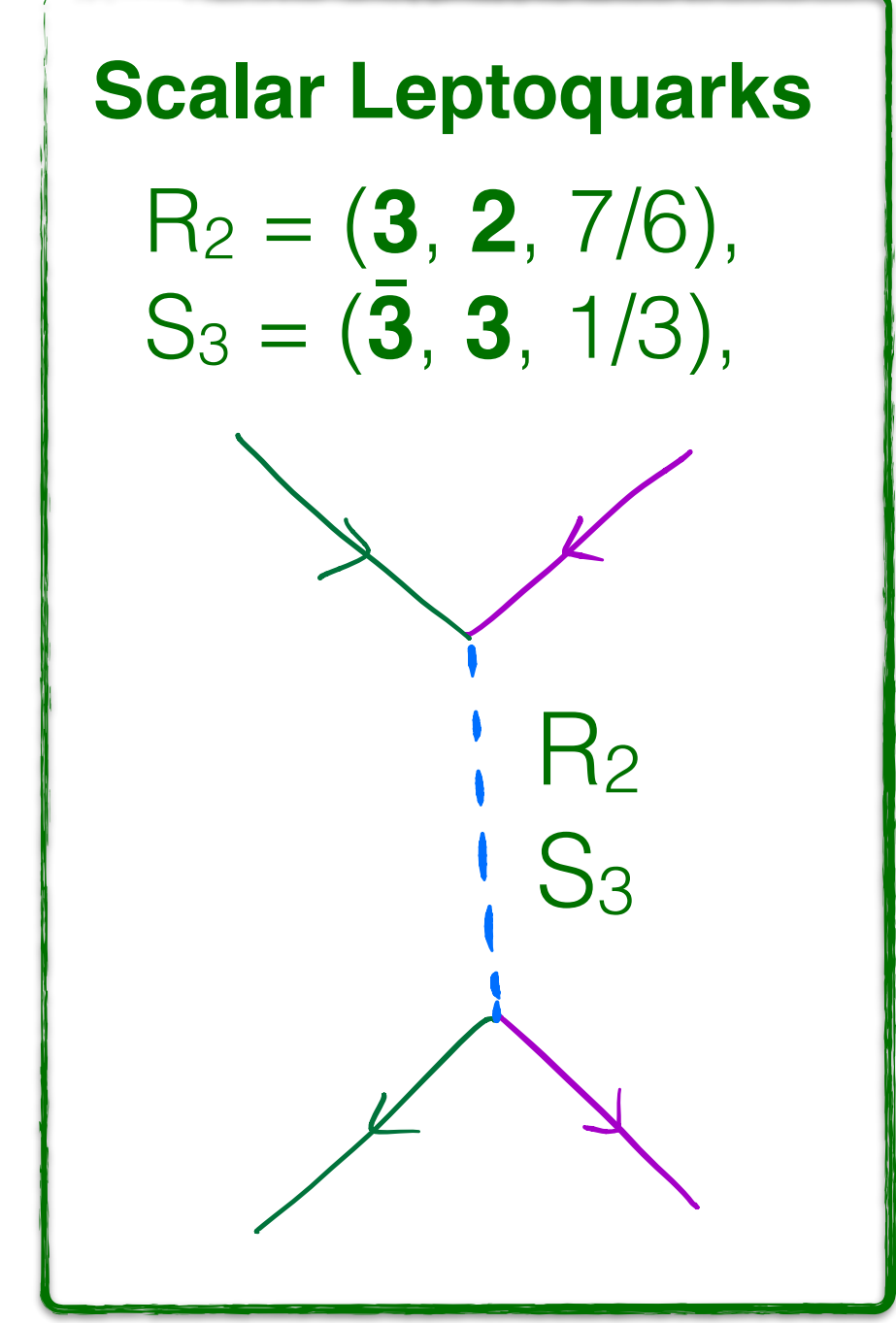
**U<sub>1</sub>** and **S<sub>3</sub>** can mediate  $b_L \rightarrow s_L \mu_L \mu_L$



Barbieri et al 1512.01560; Buttazzo, Greljo, Isidori, DM 1706.07808; Di Luzio et al 1708.08450; Bordone et al. 1712.01368; Calibbi et al. '17; Blanke, Crivellin '18; Cornella et al 2103.16558; Angelescu et al 1808.08179



Crivellin et al. 1703.09226; Buttazzo, Greljo, Isidori, DM 1706.07808; D.M. 1803.10972; Arnan et al 1901.06315; Bigaran et al. 1906.01870; Crivellin et al. 1912.04224; Saad 2005.04352; V. Gherardi, E. Venturini, D.M. 2003.12525, 2008.09548; Bordone, Catà, Feldmann, Mandal 2010.03297; Crivellin et al. 2010.06593, 2101.07811; ETC...



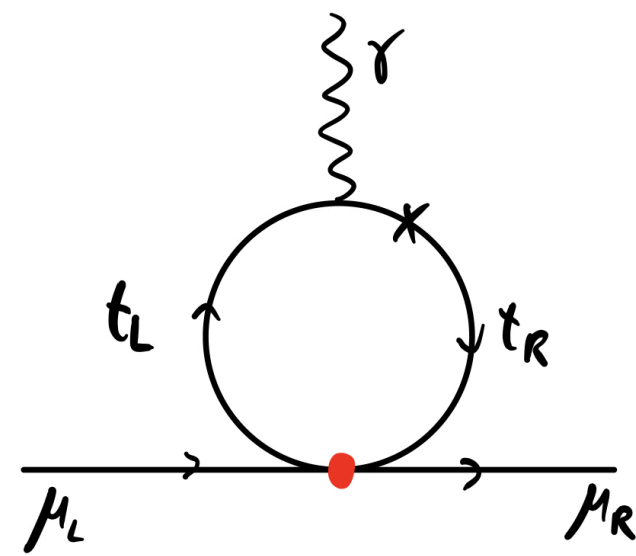
Becirevic et al. 1806.05689; Becirevic, Sumensari 1704.05835; Popov et al. 1905.06339; Angelescu et al. 2103.12504; ETC...

TeV-scale  $U_1$  or  $S_3$  LQs can fit the anomaly with small couplings.

What about **muon (g-2)**?

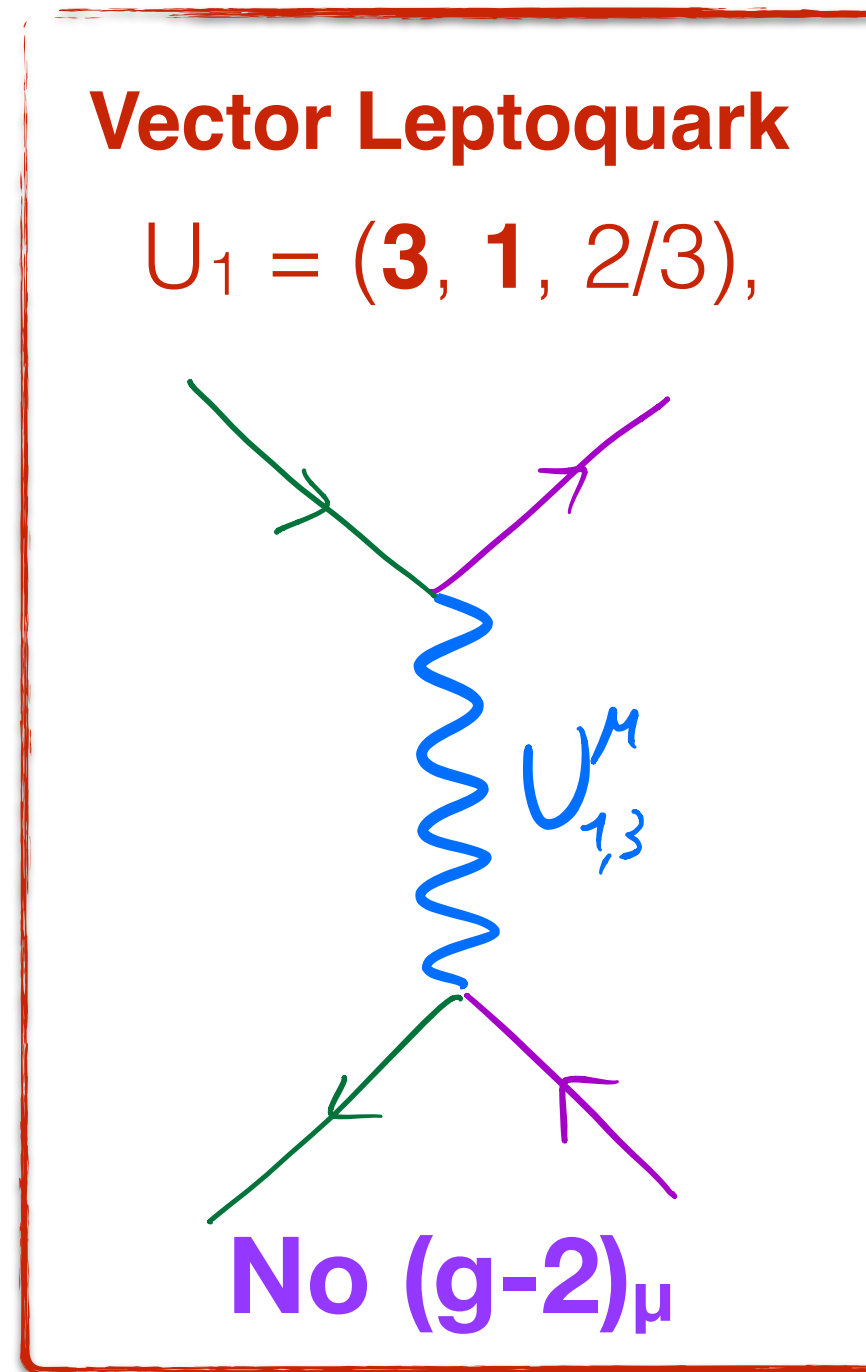
Leptoquarks with couplings to  $\mu_L \mu_R t_L t_R$  can generate  $a_\mu$  with  $TeV$  masses and small couplings:

$S_1$  or  $R_2$

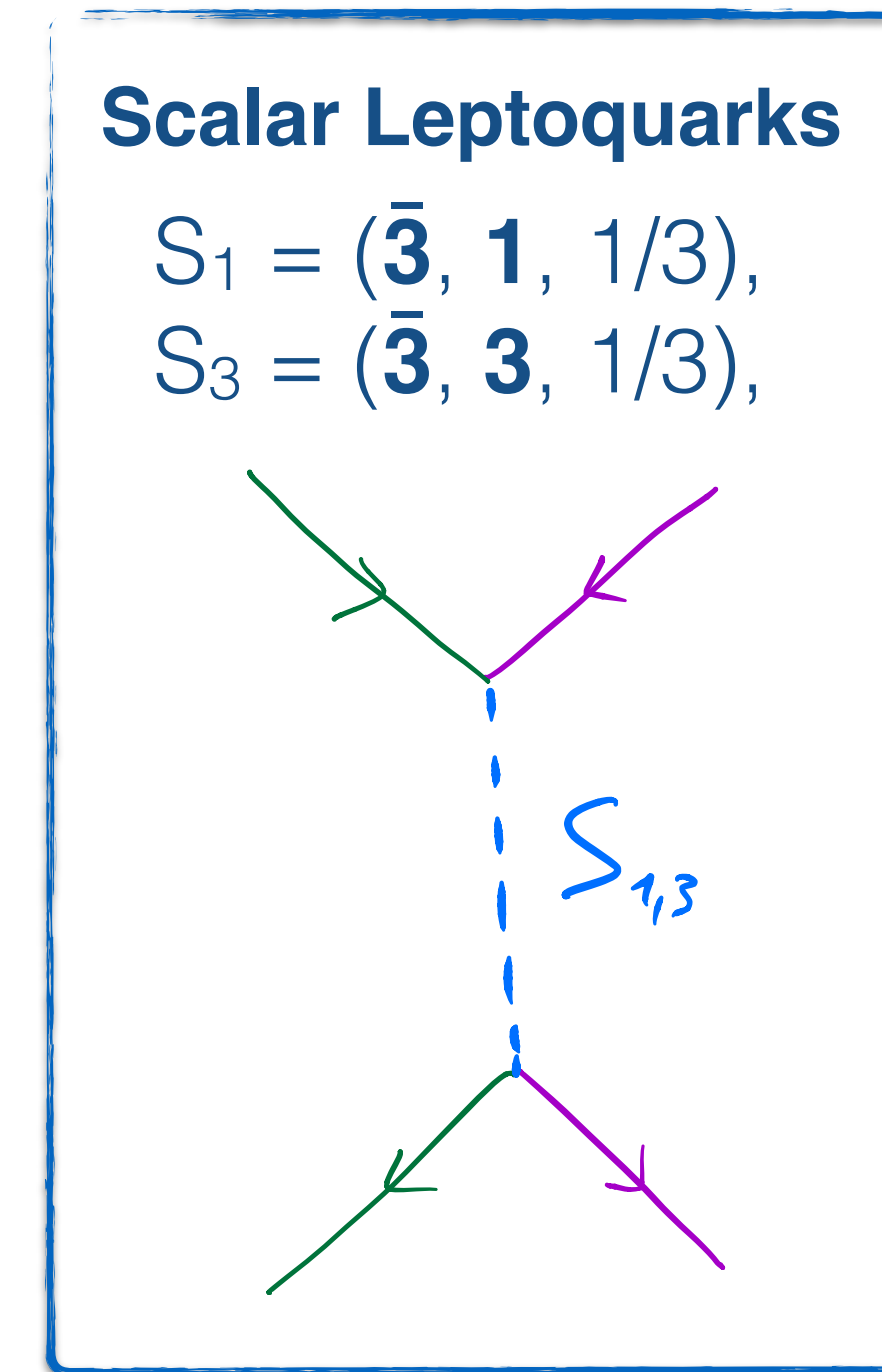


$$[L_{e\gamma}(\mu_{GW})]_{\mu\mu} = - \frac{e N_c m_t}{6\pi^2} [C_{lequ}^{(3)}(\Lambda)]_{\mu\mu tt} \log \frac{\Lambda^2}{m_t^2}$$

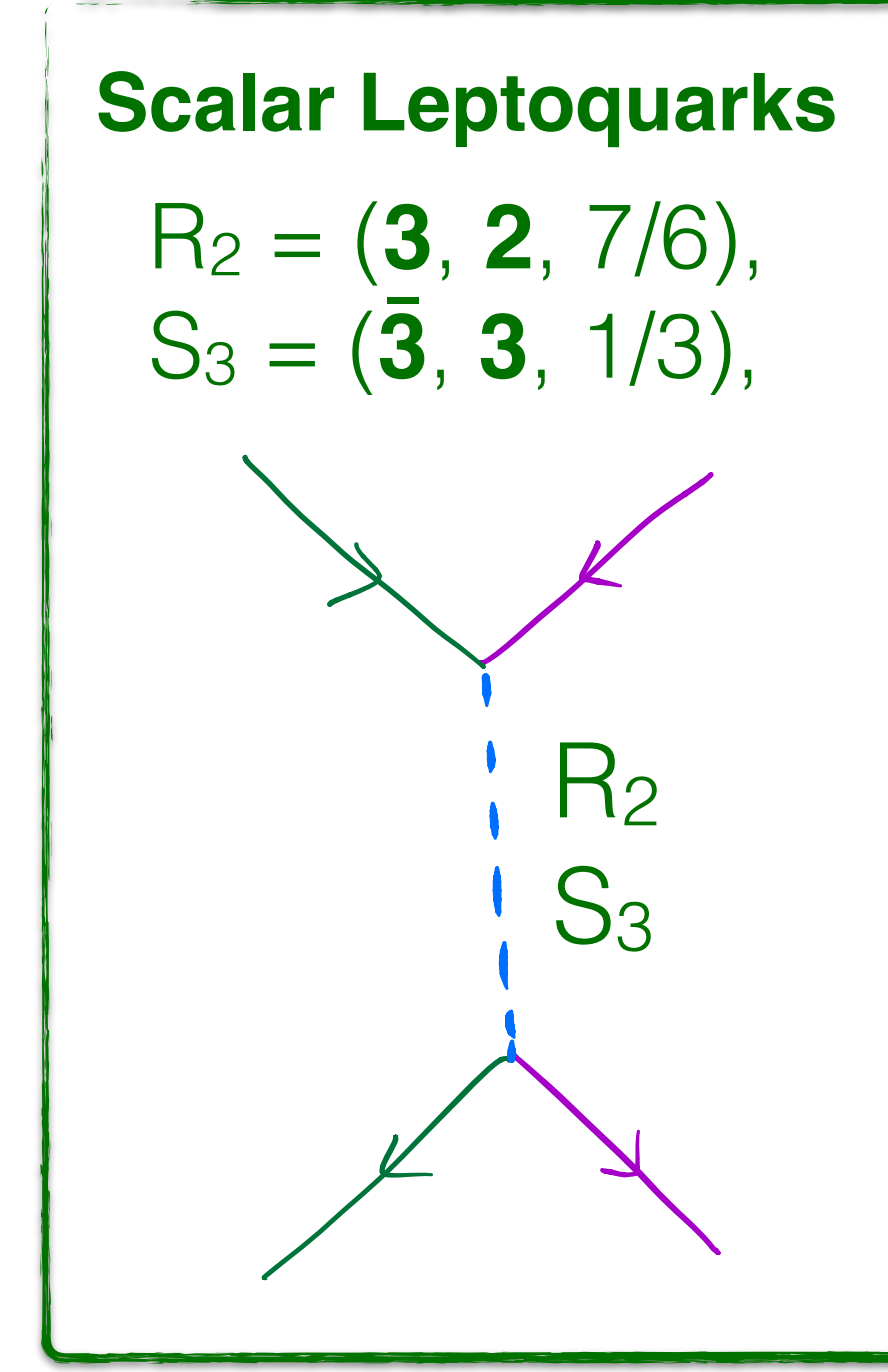
$$C_{lequ}^{(3)} = (\bar{l}_L \sigma_{\mu\nu} e_R) (\bar{q}_L \sigma^{\mu\nu} u_R)$$



Barbieri et al 1512.01560; Buttazzo, Greljo, Isidori, DM 1706.07808; Di Luzio et al 1708.08450; Bordone et al. 1712.01368; Calibbi et al. '17; Blanke, Crivellin '18; Cornella et al 2103.16558; Angelescu et al 1808.08179

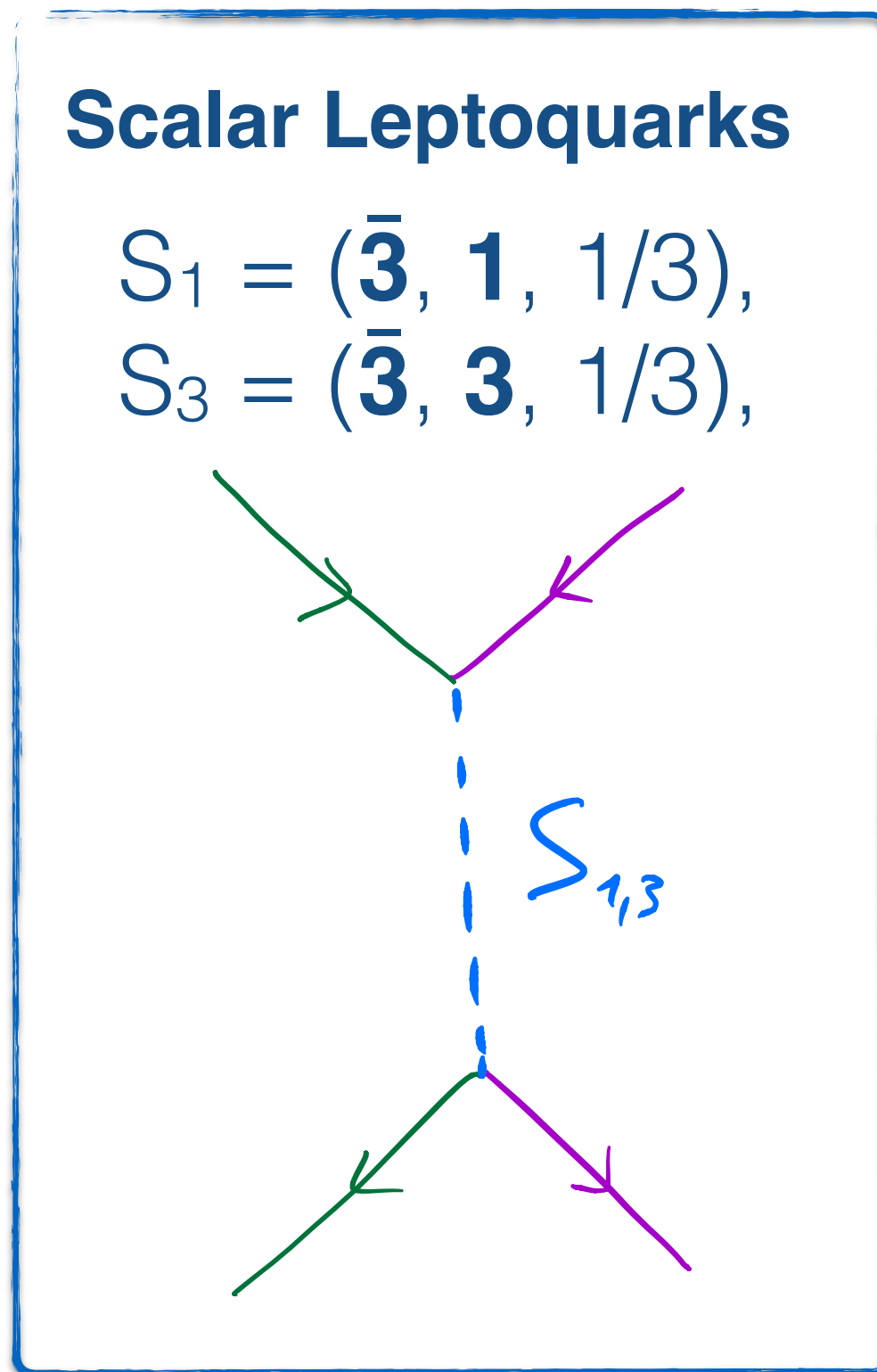


Crivellin et al. 1703.09226; Buttazzo, Greljo, Isidori, DM 1706.07808; D.M. 1803.10972; Arnan et al 1901.06315; Bigaran et al. 1906.01870; Crivellin et al. 1912.04224; Saad 2005.04352; V. Gherardi, E. Venturini, D.M. 2003.12525, 2008.09548; Bordone, Catà, Feldmann, Mandal 2010.03297; Crivellin et al. 2010.06593, 2101.07811; ETC...



Becirevic et al. 1806.05689; Becirevic, Sumensari 1704.05835; Popov et al. 1905.06339; Angelescu et al. 2103.12504; ETC...

# S<sub>1</sub> and S<sub>3</sub> scalar leptoquarks



$$\mathcal{L}_{\text{int}} \sim \left( \lambda_{ij}^{1L} q_L^i \varepsilon l_L^j + \lambda_{ij}^{1R} u_R^i e_R^j \right) S_1 + \lambda_{ij}^{3L} q_L^i \varepsilon c^A l_L^j S_3 + \text{h.c.}$$

**Why?**

- **Fully calculable** already at the simplified model level (unlike vector LQ)
- Can address the **muon (g-2)**.
- Potential **UV origin** from a **Composite Higgs Model** scenario, interesting for the potential connection to the **EW hierarchy problem**.

[D.M. 1803.10972]

Several important **observables** constraining this model are **induced at one-loop**.

We decided to approach this problem systematically in an **EFT approach**, performing a **complete one-loop SMEFT matching** and including an **exhaustive list of observables**.

Crivellin et al. 1703.09226; Buttazzo, Greljo, Isidori, DM 1706.07808; D.M. 1803.10972; Arnan et al 1901.06315; Bigaran et al. 1906.01870; Crivellin et al. 1912.04224; Saad 2005.04352; V. Gherardi, E. Venturini, D.M. 2003.12525, 2008.09548; Bordone, Catà, Feldmann, Mandal 2010.03297; Crivellin et al. 2010.06593, 2101.07811; S. Trifinopoulos, E. Venturini, D.M. [2106.15630]; ETC...

# $S_1$ and $S_3$ scalar leptoquarks

1) Match **SM** +  $S_1+S_3$  to **SMEFT** @ 1-loop

(SMEFT RGE, SMEFT-LEFT 1-loop matching, LEFT RGE already done in literature)

V. Gherardi, E. Venturini, D.M. [[2003.12525](#)]

[Alonso, Jenkins, Manohar, Trott '13]

[Dekens, Stoffer 1908.05295]

[Jenkins, Manohar, Stoffer 1711.05270]

2) Analysis of B-anomalies, including all observables sensitive to the relevant couplings

V. Gherardi, E. Venturini, D.M. [[2008.09548](#)]

3) Turn on **1st gen couplings** and study **Kaon** &  $\mu \rightarrow e$  observables.

Flavor symmetries correlate 1st gen to 2nd and 3rd gen couplings:

> case of  $U(2)^5$  flavor symmetry.

S. Trifinopoulos, E. Venturini, D.M. [[2106.15630](#)]

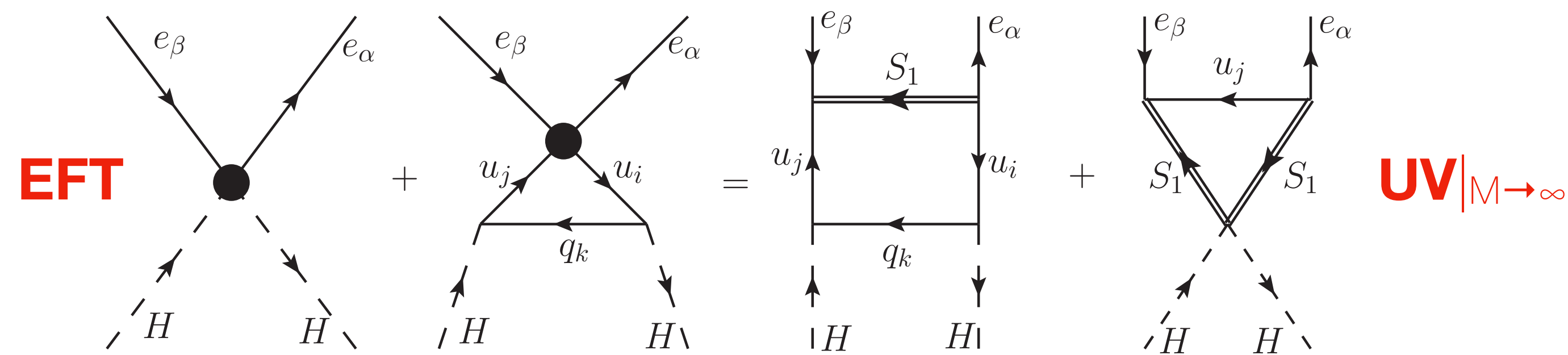


# Matching to SMEFT

V. Gherardi, E. Venturini, D.M. [2003.12525]

We match **off-shell Green's functions** for **One-Light-Particle-Irreducible (1LPI)** diagrams

Example:  $\mathcal{G} \equiv \langle e_\beta(p_1) \bar{e}_\alpha(p_2) H_b(q_1) H_a^\dagger(q_2) \rangle$



$$[\mathcal{O}_{He}]_{\alpha\beta} = (\bar{e}_\alpha \gamma^\mu e_\beta) (H^\dagger i \overleftrightarrow{D}_\mu H) ,$$

$$[\mathcal{O}'_{He}]_{\alpha\beta} = (\bar{e}_\alpha i \overleftrightarrow{D} e_\beta) (H^\dagger H) ,$$

$$[\mathcal{O}''_{He}]_{\alpha\beta} = (\bar{e}_\alpha \gamma^\mu e_\beta) \partial_\mu (H^\dagger H) .$$

Figure 1: Diagrams for the matching of the  $\langle \bar{e}eH^\dagger H \rangle$  Green function.

This procedure gives the matching for **operators** that are **independent under IBP and Fierz**, but are **redundant upon using field redefinitions: Green's basis**. Jiang et al. [1811.08878]

We obtained the *complete Green's basis at dim-6* and set of reduction equations to the Warsaw basis

Ours is the first such complete matching for a **very rich scenario**: most dim-6 operators are induced. **Useful as cross-check** for *functional* techniques and upcoming *computational* methods.

“Universal Scalar Leptoquark Action for Matching” Dedes, Mantzaropoulos [2108.10055]

CoDEx Bakshi, Chakraborty, Patra  
Matchete Fuentes-Martín, König, Pagès, Thomsen, Wilsch  
Matchmaker Anastasiou, Carmona, Lazopoulos, Santiago

# S<sub>1</sub> and S<sub>3</sub> - global analysis

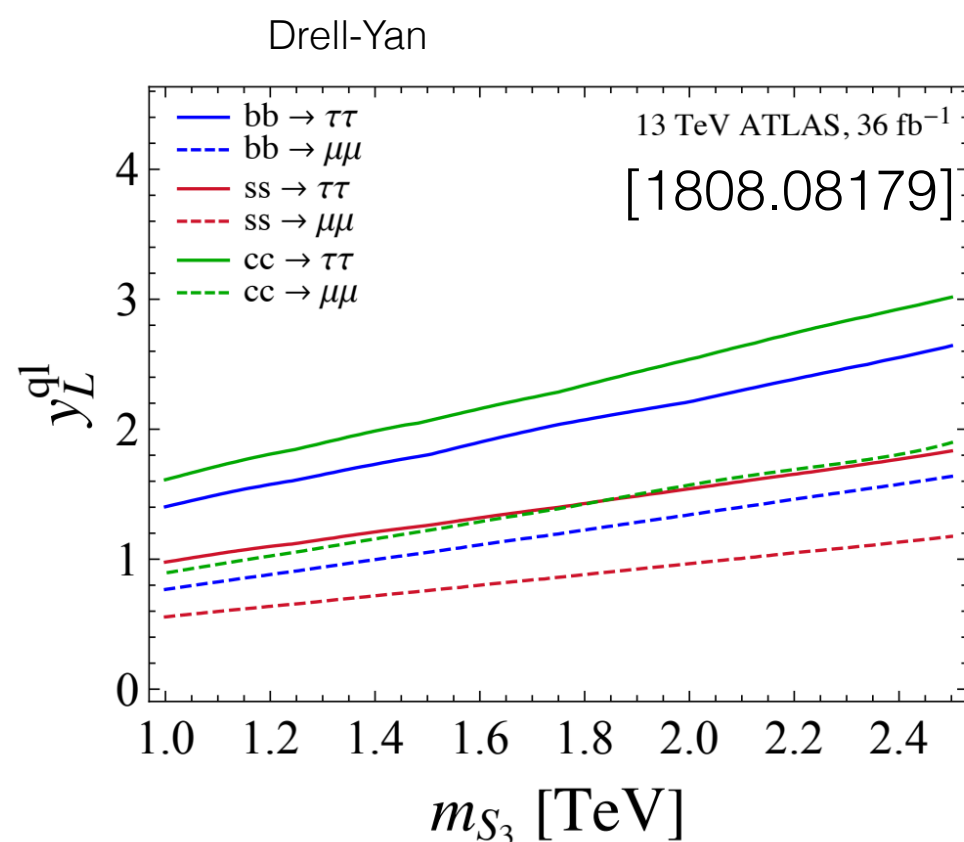
V. Gherardi, E. Venturini, D.M. [2008.09548]

Using the complete one-loop matching to SMEFT, we include in our analysis the following observables.

All these are used to build a **global likelihood**.

$$-2\log \mathcal{L} \equiv \chi^2(\lambda_x, M_x) = \sum_i \frac{(\mathcal{O}_i(\lambda_x, M_x) - \mu_i)^2}{\sigma_i^2}$$

Observable	Experimental bounds
Z boson couplings	App. A.12
$\delta g_{\mu L}^Z$	$(0.3 \pm 1.1)10^{-3}$ [99]
$\delta g_{\mu R}^Z$	$(0.2 \pm 1.3)10^{-3}$ [99]
$\delta g_{\tau L}^Z$	$(-0.11 \pm 0.61)10^{-3}$ [99]
$\delta g_{\tau R}^Z$	$(0.66 \pm 0.65)10^{-3}$ [99]
$\delta g_{bL}^Z$	$(2.9 \pm 1.6)10^{-3}$ [99]
$\delta g_{cR}^Z$	$(-3.3 \pm 5.1)10^{-3}$ [99]
$N_\nu$	$2.9963 \pm 0.0074$ [100]



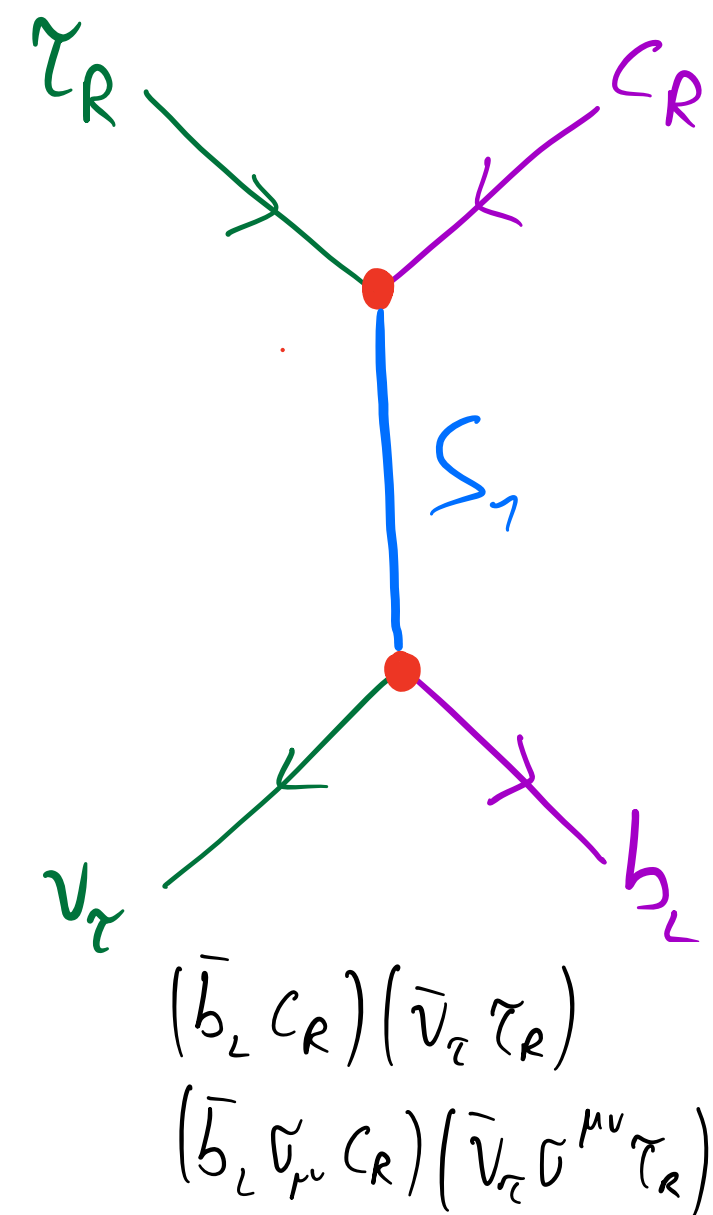
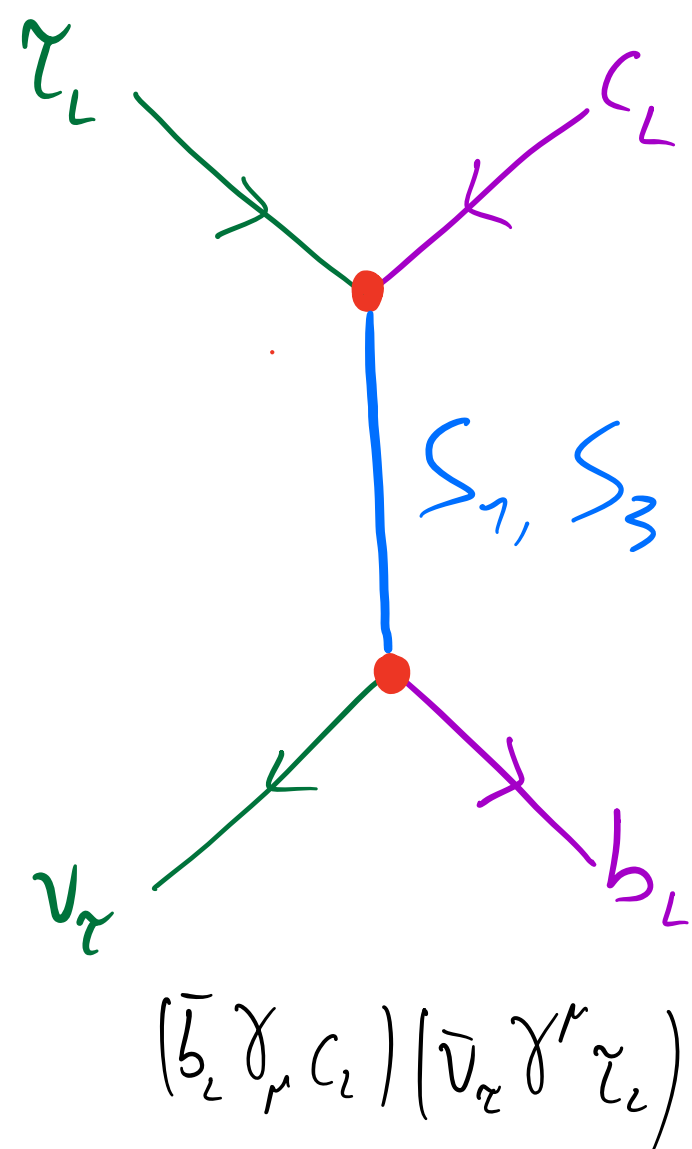
Observable	SM prediction	Experimental bounds
<i>b</i> → <i>s</i> ℓℓ observables		[37]
$\Delta C_9^{sb\mu\mu}$	0	$-0.43 \pm 0.09$ [79]
$C_9^{\text{univ}}$	0	$-0.48 \pm 0.24$ [79]
<i>b</i> → <i>c</i> τ(ℓ)ν observables		[37]
$R_D$	$0.299 \pm 0.003$ [12]	$0.34 \pm 0.027 \pm 0.013$ [12]
$R_D^*$	$0.258 \pm 0.005$ [12]	$0.295 \pm 0.011 \pm 0.008$ [12]
$P_\tau^{D^*}$	$-0.488 \pm 0.018$ [80]	$-0.38 \pm 0.51 \pm 0.2 \pm 0.018$ [7]
$F_L$	$0.470 \pm 0.012$ [80]	$0.60 \pm 0.08 \pm 0.038 \pm 0.012$ [81]
$\mathcal{B}(B_c^+ \rightarrow \tau^+\nu)$	2.3%	< 10% (95% CL) [82]
$R_D^{\mu/e}$	1	$0.978 \pm 0.035$ [83, 84]
<i>b</i> → <i>s</i> νν and <i>s</i> → <i>d</i> νν		[37]
$R_K^\nu$	1 [85]	< 4.7 [86]
$R_{K^*}^\nu$	1 [85]	< 3.2 [86]
<i>b</i> → <i>d</i> μμ and <i>b</i> → <i>d</i> ee		App. A.5
$\mathcal{B}(B^0 \rightarrow \mu\mu)$	$(1.06 \pm 0.09) \times 10^{-10}$ [87, 88]	$(1.1 \pm 1.4) \times 10^{-10}$ [89, 90]
$\mathcal{B}(B^+ \rightarrow \pi^+\mu\mu)$	$(2.04 \pm 0.21) \times 10^{-8}$ [87, 88]	$(1.83 \pm 0.24) \times 10^{-8}$ [89, 90]
$\mathcal{B}(B^0 \rightarrow ee)$	$(2.48 \pm 0.21) \times 10^{-15}$ [87, 88]	< $8.3 \times 10^{-8}$ [51]
$\mathcal{B}(B^+ \rightarrow \pi^+ee)$	$(2.04 \pm 0.24) \times 10^{-8}$ [87, 88]	< $8 \times 10^{-8}$ [51]
<i>B</i> LFV decays		[37]
$\mathcal{B}(B_d \rightarrow \tau^\pm\mu^\mp)$	0	< $1.4 \times 10^{-5}$ [91]
$\mathcal{B}(B_s \rightarrow \tau^\pm\mu^\mp)$	0	< $4.2 \times 10^{-5}$ [91]
$\mathcal{B}(B^+ \rightarrow K^+\tau^-\mu^+)$	0	< $5.4 \times 10^{-5}$ [92]
$\mathcal{B}(B^+ \rightarrow K^+\tau^+\mu^-)$	0	< $3.3 \times 10^{-5}$ [92] < $4.5 \times 10^{-5}$ [93]

Observable	SM prediction	Experimental bounds
<i>D</i> leptonic decay		[37] and App. A.4
$\mathcal{B}(D_s \rightarrow \tau\nu)$	$(5.169 \pm 0.004) \times 10^{-2}$ [94]	$(5.48 \pm 0.23) \times 10^{-2}$ [51]
$\mathcal{B}(D^0 \rightarrow \mu\mu)$	$\approx 10^{-11}$ [95]	< $7.6 \times 10^{-9}$ [96]
$\mathcal{B}(D^+ \rightarrow \pi^+\mu\mu)$	$\mathcal{O}(10^{-12})$ [97]	< $7.4 \times 10^{-8}$ [98]
Rare Kaon decays (νν)		App. A.1
$\mathcal{B}(K^+ \rightarrow \pi^+\nu\nu)$	$8.64 \times 10^{-11}$ [99]	$(11.0 \pm 4.0) \times 10^{-11}$ [100]
$\mathcal{B}(K_L \rightarrow \pi^0\nu\nu)$	$3.4 \times 10^{-11}$ [99]	< $3.6 \times 10^{-9}$ [101]
Rare Kaon decays (ℓℓ)		App. A.3 and A.2
$\mathcal{B}(K_L \rightarrow \mu\mu)_{SD}$	$8.4 \times 10^{-10}$ [102]	< $2.5 \times 10^{-9}$ [76]
$\mathcal{B}(K_S \rightarrow \mu\mu)$	$(5.18 \pm 1.5) \times 10^{-12}$ [76, 103, 104]	< $2.5 \times 10^{-10}$ [105]
$\mathcal{B}(K_L \rightarrow \pi^0\mu\mu)$	$(1.5 \pm 0.3) \times 10^{-11}$ [106]	< $4.5 \times 10^{-10}$ [107]
$\mathcal{B}(K_L \rightarrow \pi^0ee)$	$(3.2_{-0.8}^{+1.2}) \times 10^{-11}$ [108]	< $2.8 \times 10^{-10}$ [109]
LFV in Kaon decays		App. A.3 and A.2
$\mathcal{B}(K_L \rightarrow \mu e)$	0	< $4.7 \times 10^{-12}$ [110]
$\mathcal{B}(K^+ \rightarrow \pi^+\mu^-e^+)$	0	< $7.9 \times 10^{-11}$ [111]
$\mathcal{B}(K^+ \rightarrow \pi^+e^-\mu^+)$	0	< $1.5 \times 10^{-11}$ [112]
CP-violation		App. A.8
$\epsilon'_K/\epsilon_K$	$(15 \pm 7) \times 10^{-4}$ [113]	$(16.6 \pm 2.3) \times 10^{-4}$ [51]

Observable	SM prediction	Experimental bounds
$\Delta F = 2$ processes		[37]
$B^0 - \bar{B}^0:  C_{B_d}^1 $	0	< $9.1 \times 10^{-7}$ TeV <sup>-2</sup> [114, 115]
$B_s^0 - \bar{B}_s^0:  C_{B_s}^1 $	0	< $2.0 \times 10^{-5}$ TeV <sup>-2</sup> [114, 115]
$K^0 - \bar{K}^0: \text{Re}[C_K^1]$	0	< $8.0 \times 10^{-7}$ TeV <sup>-2</sup> [114, 115]
$K^0 - \bar{K}^0: \text{Im}[C_K^1]$	0	< $3.0 \times 10^{-9}$ TeV <sup>-2</sup> [114, 115]
$D^0 - \bar{D}^0: \text{Re}[C_D^1]$	0	< $3.6 \times 10^{-7}$ TeV <sup>-2</sup> [114, 115]
$D^0 - \bar{D}^0: \text{Im}[C_D^1]$	0	< $2.2 \times 10^{-8}$ TeV <sup>-2</sup> [114, 115]
$D^0 - \bar{D}^0: \text{Re}[C_D^4]$	0	< $3.2 \times 10^{-8}$ TeV <sup>-2</sup> [114, 115]
$D^0 - \bar{D}^0: \text{Im}[C_D^4]$	0	< $1.2 \times 10^{-9}$ TeV <sup>-2</sup> [114, 115]
$D^0 - \bar{D}^0: \text{Re}[C_D^5]$	0	< $2.7 \times 10^{-7}$ TeV <sup>-2</sup> [114, 115]
$D^0 - \bar{D}^0: \text{Im}[C_D^5]$	0	< $1.1 \times 10^{-8}$ TeV <sup>-2</sup> [114, 115]
LFU in τ decays		[37]
$ g_\mu/g_e ^2$	1	$1.0036 \pm 0.0028$ [116]
$ g_\tau/g_\mu ^2$	1	$1.0022 \pm 0.0030$ [116]
$ g_\tau/g_e ^2$	1	$1.0058 \pm 0.0030$ [116]
LFV observables		[37]
$\mathcal{B}(\tau \rightarrow \mu\phi)$	0	< $1.00 \times 10^{-7}$ [117]
$\mathcal{B}(\tau \rightarrow 3\mu)$	0	< $2.5 \times 10^{-8}$ [118]
$\mathcal{B}(\tau \rightarrow \mu\gamma)$	0	< $5.2 \times 10^{-8}$ [119]
$\mathcal{B}(\tau \rightarrow e\gamma)$	0	< $3.9 \times 10^{-8}$ [119]
$\mathcal{B}(\mu \rightarrow e\gamma)$	0	< $5.0 \times 10^{-13}$ [120]
$\mathcal{B}(\mu \rightarrow 3e)$	0	< $1.2 \times 10^{-12}$ [121]
$\mathcal{B}_{\mu e}^{(\text{Ti})}$	0	< $5.1 \times 10^{-12}$ [122]
$\mathcal{B}_{\mu e}^{(\text{Au})}$	0	< $8.3 \times 10^{-13}$ [123]
EDMs		[37]
$ d_e $	< $10^{-44}$ e · cm [124, 125]	< $1.3 \times 10^{-29}$ e · cm [126]
$ d_\mu $	< $10^{-42}$ e · cm [125]	< $1.9 \times 10^{-19}$ e · cm [127]
$d_\tau$	< $10^{-41}$ e · cm [125]	$(1.15 \pm 1.70) \times 10^{-17}$ e · cm [37]
$d_n$	< $10^{-33}$ e · cm [128]	< $2.1 \times 10^{-26}$ e · cm [129]
Anomalous Magnetic Moments		[37]
$a_e - a_e^{\text{SM}}$	$\pm 2.3 \times 10^{-13}$ [130, 131]	$(-8.9 \pm 3.6) \times 10^{-13}$ [132]
$a_\mu - a_\mu^{\text{SM}}$	$\pm 43 \times 10^{-11}$ [42]	$(279 \pm 76) \times 10^{-11}$ [40, 42]
$a_\tau - a_\tau^{\text{SM}}$	$\pm 3.9 \times 10^{-8}$ [130]	$(-2.1 \pm 1.7) \times 10^{-7}$ [133]

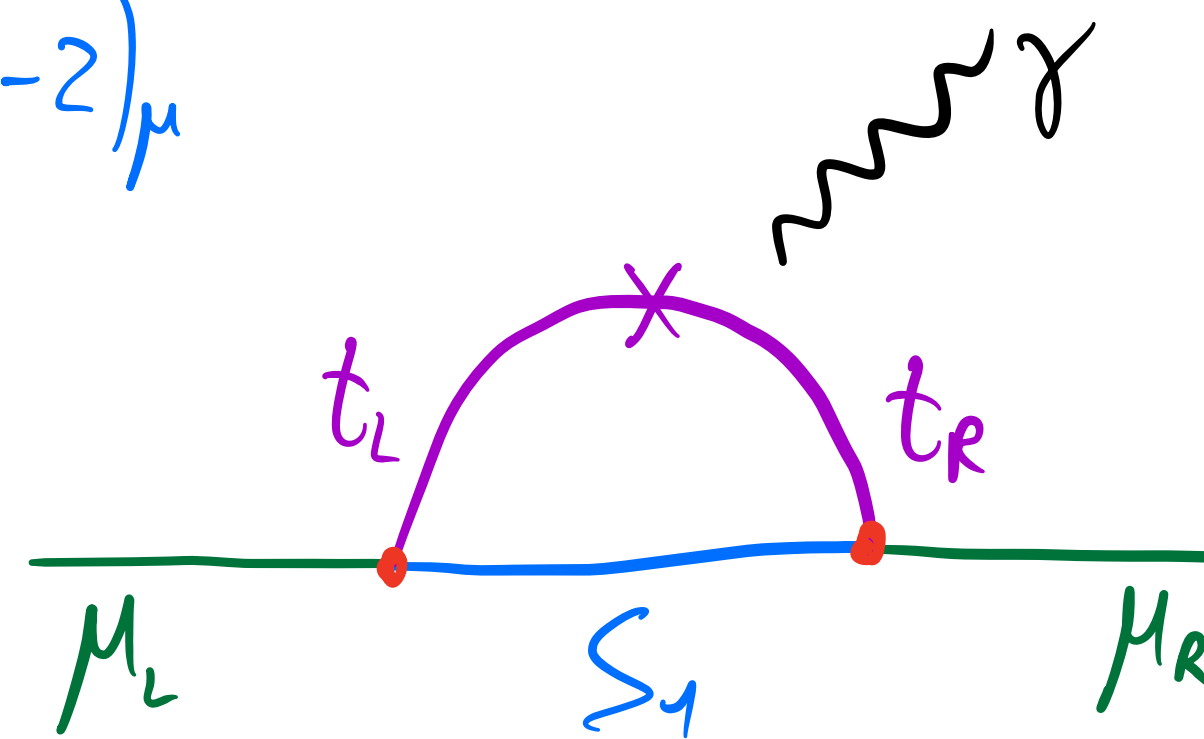
# S<sub>1</sub> and S<sub>3</sub> - contributions to anomalies

R(Δ<sup>(\*)</sup>)

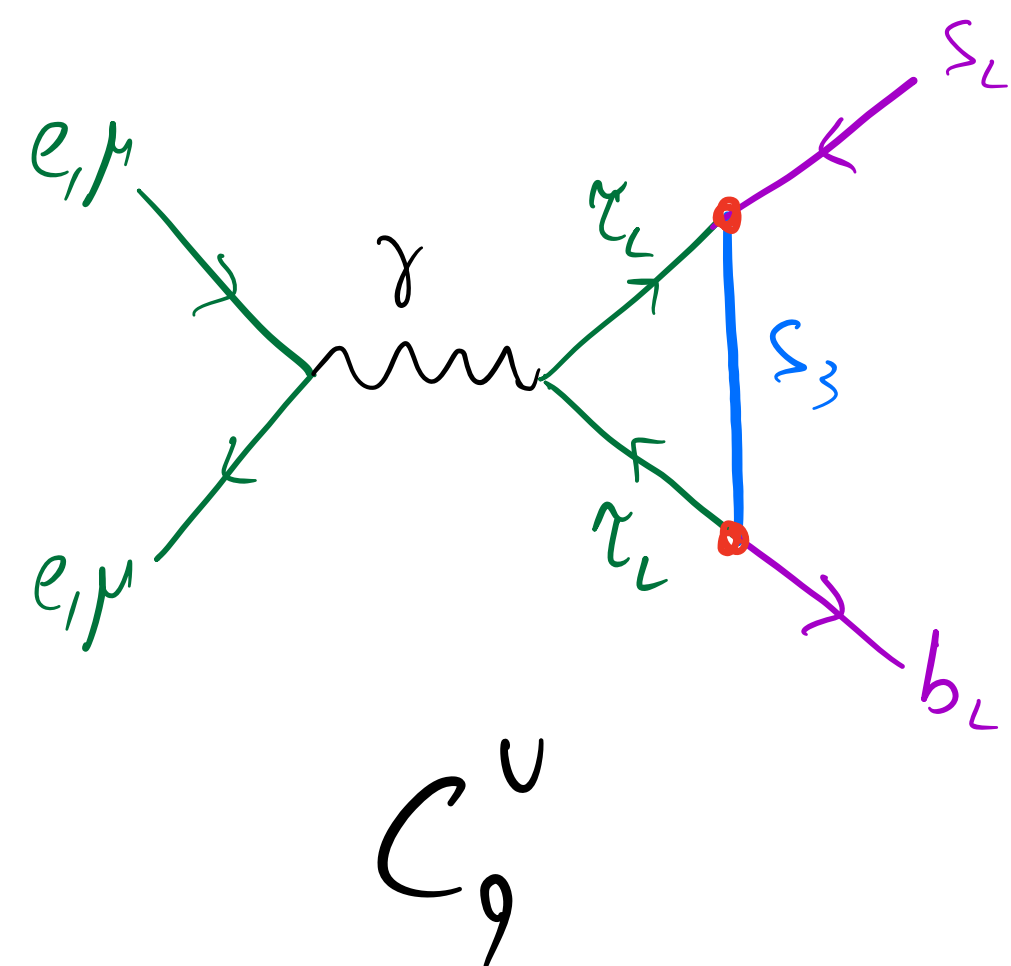
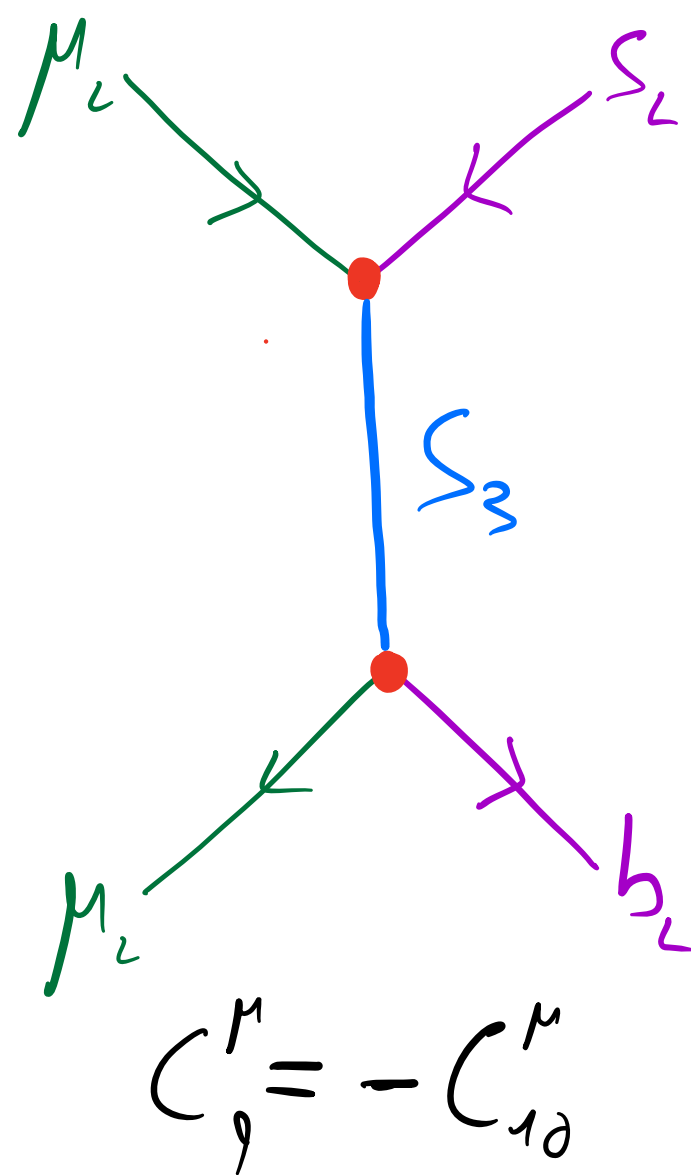


$$L_{int} \sim (\lambda_{ij}^{1L} q_L^i \varepsilon l_L^j + \lambda_{ij}^{1R} u_R^i e_R^j) S_1 + \lambda_{ij}^{3L} q_L^i \varepsilon_G^A l_L^j S_3 + h.c.$$

(g-2)<sub>μ</sub>



b → S μ μ



# S<sub>1</sub> and S<sub>3</sub> - benchmarks

Two **benchmark** scenarios:

$$\mathcal{L}_{\text{int}} \sim \left( \lambda_{ij}^{1L} q_L^i \varepsilon l_L^j + \lambda_{ij}^{1R} u_R^i e_R^j \right) \sum_1 + \lambda_{ij}^{3L} q_L^i \varepsilon \tilde{G}^A l_L^j \sum_3 + \text{h.c.}$$

## LH + RH

$$\lambda^{1L} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & s\tau \\ 0 & b\mu & b\tau \end{pmatrix}$$

$$\lambda^{3L} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & s\mu & s\tau \\ 0 & b\mu & b\tau \end{pmatrix}$$

$$\lambda^{1R} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & c\tau \\ 0 & t\mu & t\tau \end{pmatrix}$$

R( $\Delta^{(*)}$ )  
 $b \rightarrow s \mu \mu$   
 $(g-2)_\mu$

## Only LH

$$\lambda^{1L} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & s\tau \\ 0 & 0 & b\tau \end{pmatrix}$$

$$\lambda^{3L} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & s\mu & s\tau \\ 0 & b\mu & b\tau \end{pmatrix}$$

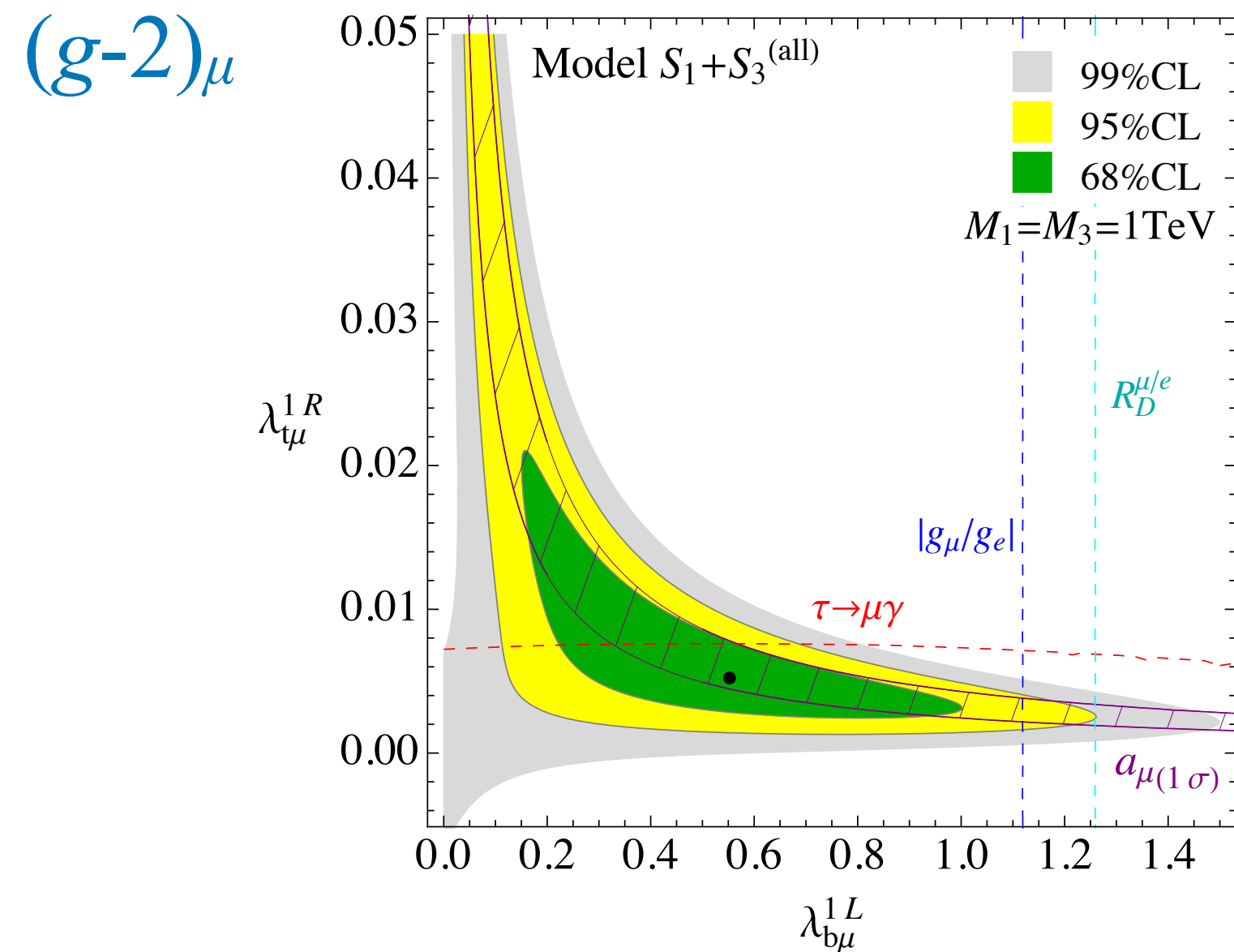
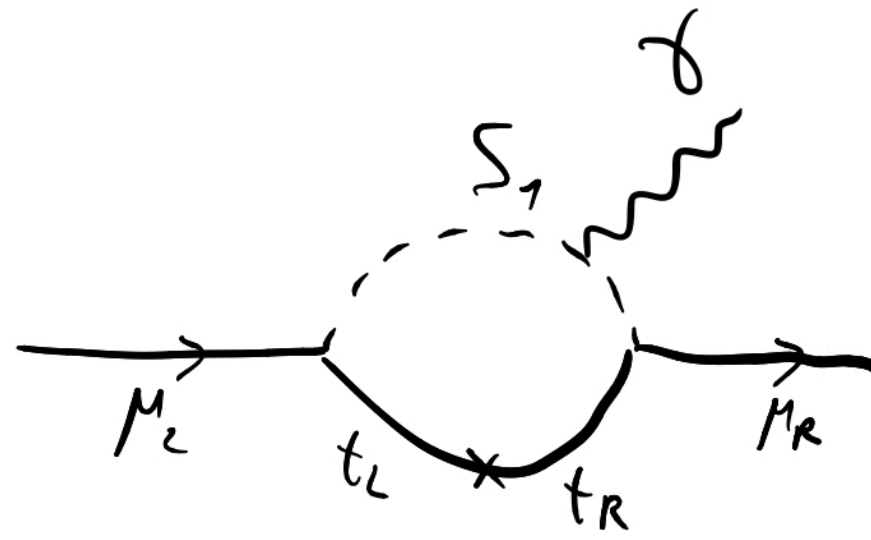
$$\lambda^{1R} = 0$$

$M_{S_{1,3}} \sim 1 \text{ TeV}$

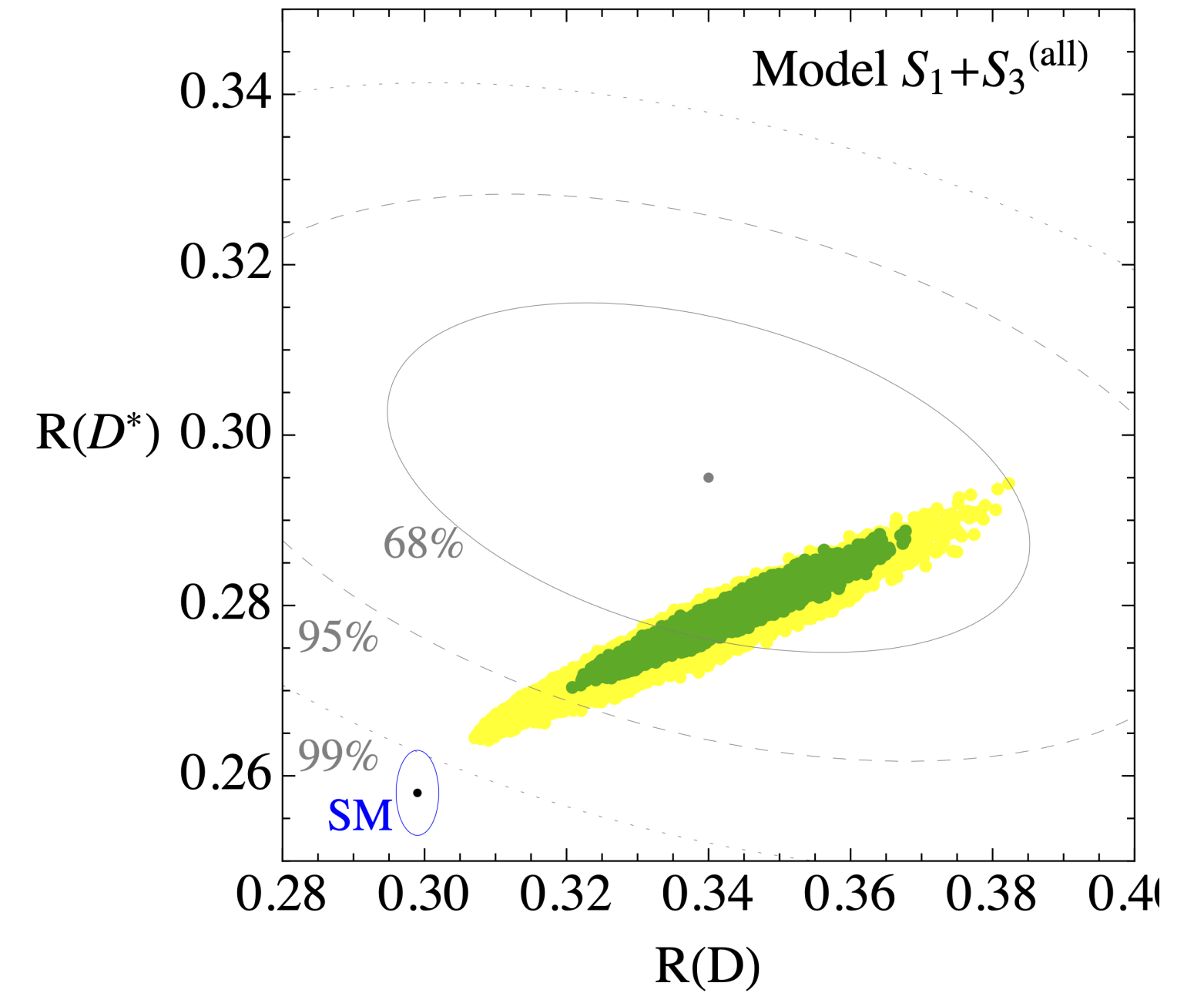
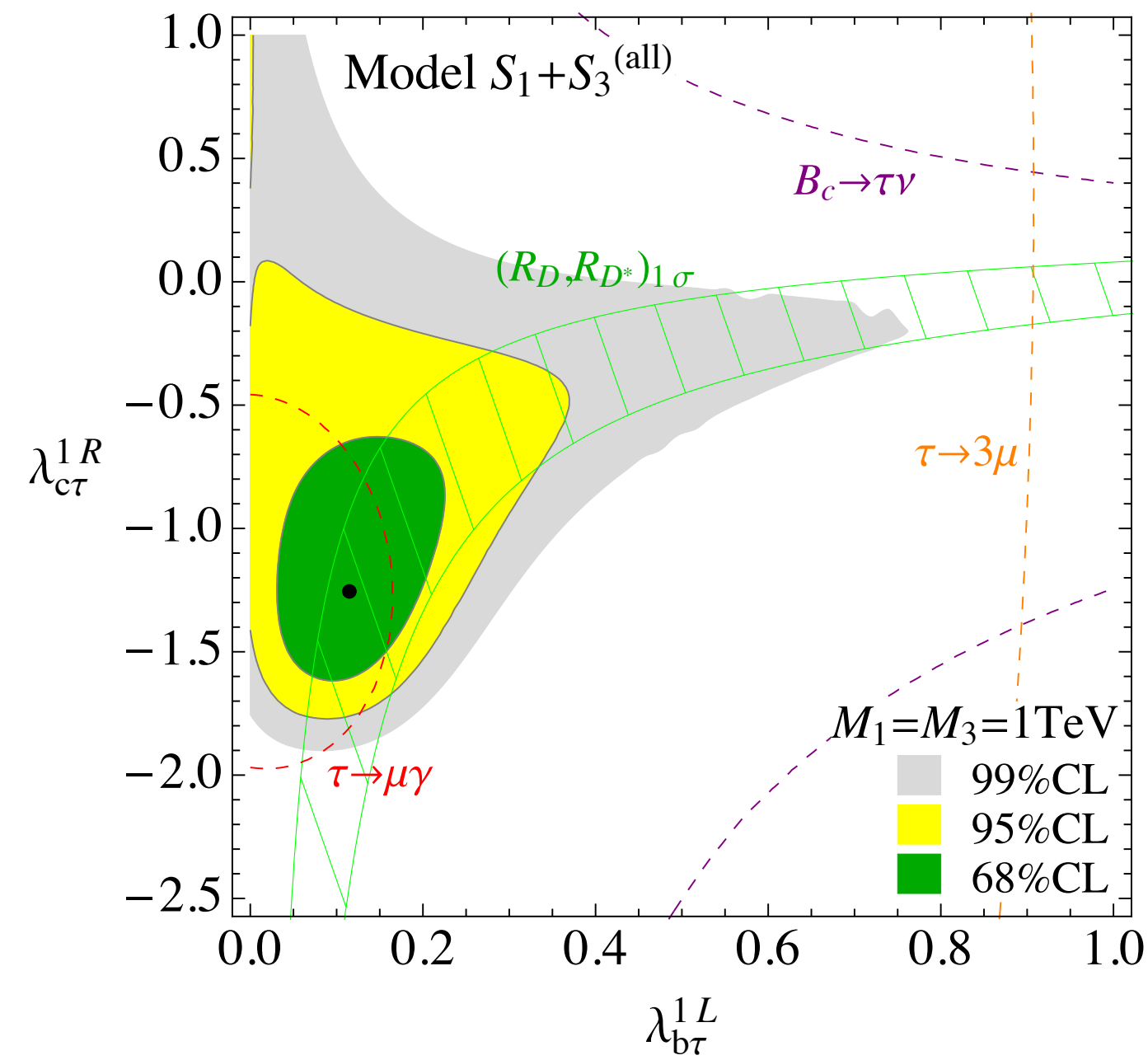
# $S_1$ and $S_3$ : $R(K^{(*)}) + R(D^{(*)}) + (g-2)_\mu$

$$\lambda^{1L} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & s\tau \\ 0 & b\mu & b\tau \end{pmatrix} \quad \lambda^{3L} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & s\mu & s\tau \\ 0 & b\mu & b\tau \end{pmatrix}$$

$$\lambda^{1R} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & c\tau \\ 0 & t\mu & t\tau \end{pmatrix}$$



## $R(D^{(*)})$



The fit to  $b \rightarrow s \mu \mu$  is very good (same as next slide)

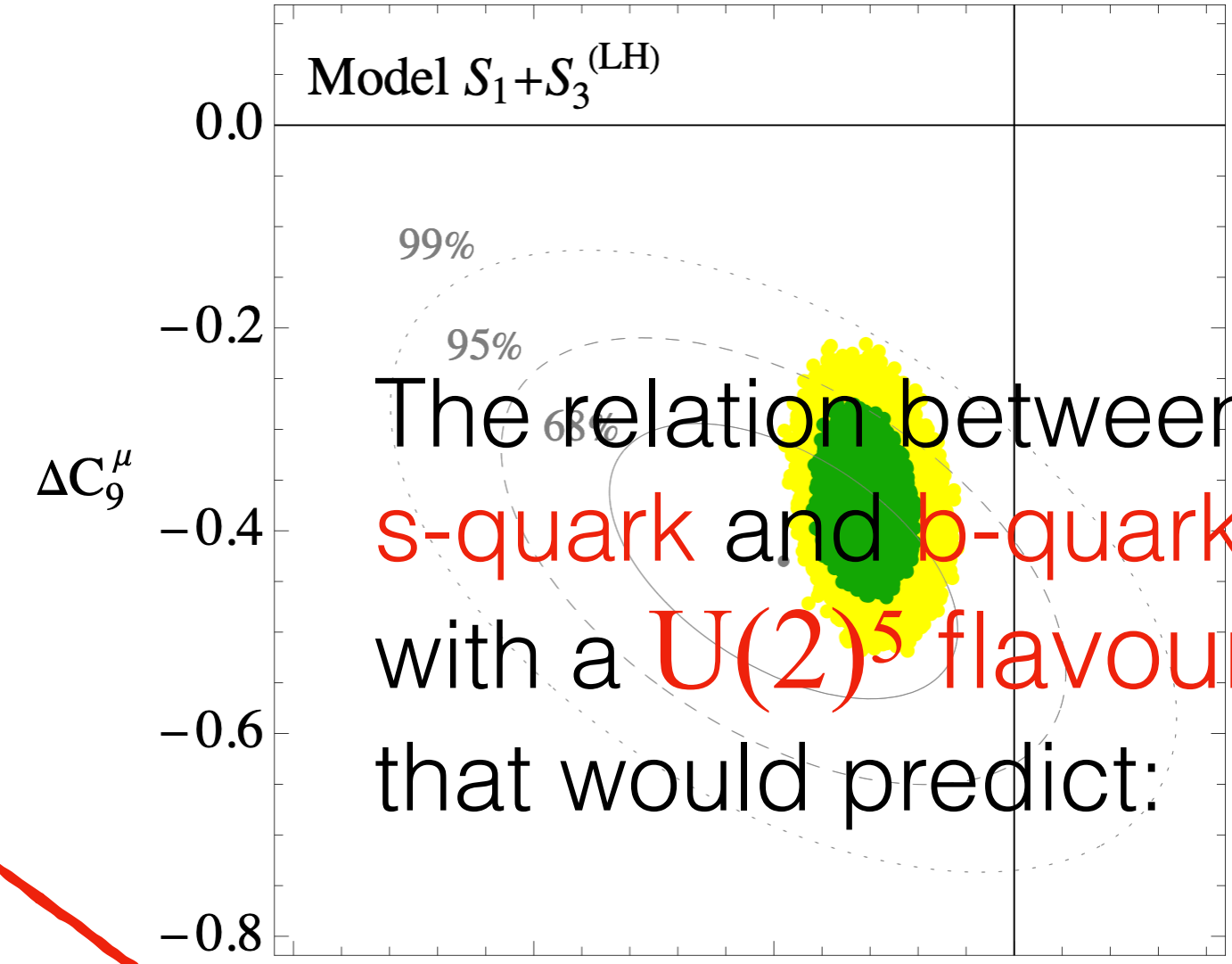
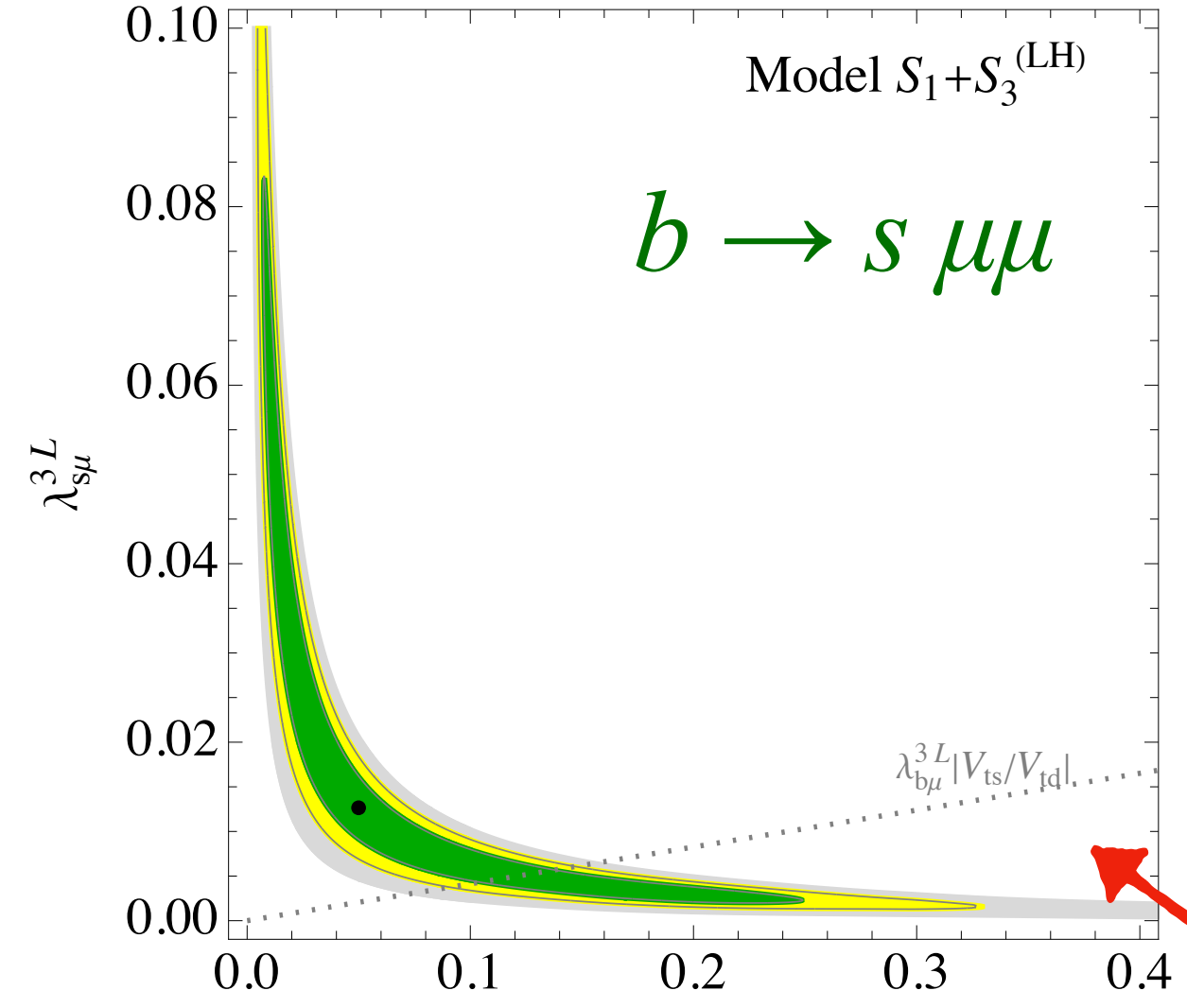
Contribution to  $R(D^{(*)})$  dominated by  $S_1$ : scalar+tensor op.  
Can also fit  $(g-2)_\mu$ .

**Very good fit of all anomalies!**

# S<sub>1</sub> and S<sub>3</sub> — only LH couplings: R(K<sup>\*</sup>) + R(D<sup>\*</sup>)

$$\lambda^{1L} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & s\tau \\ 0 & 0 & b\tau \end{pmatrix} \quad \lambda^{3L} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & s\mu & s\tau \\ 0 & b\mu & b\tau \end{pmatrix}$$

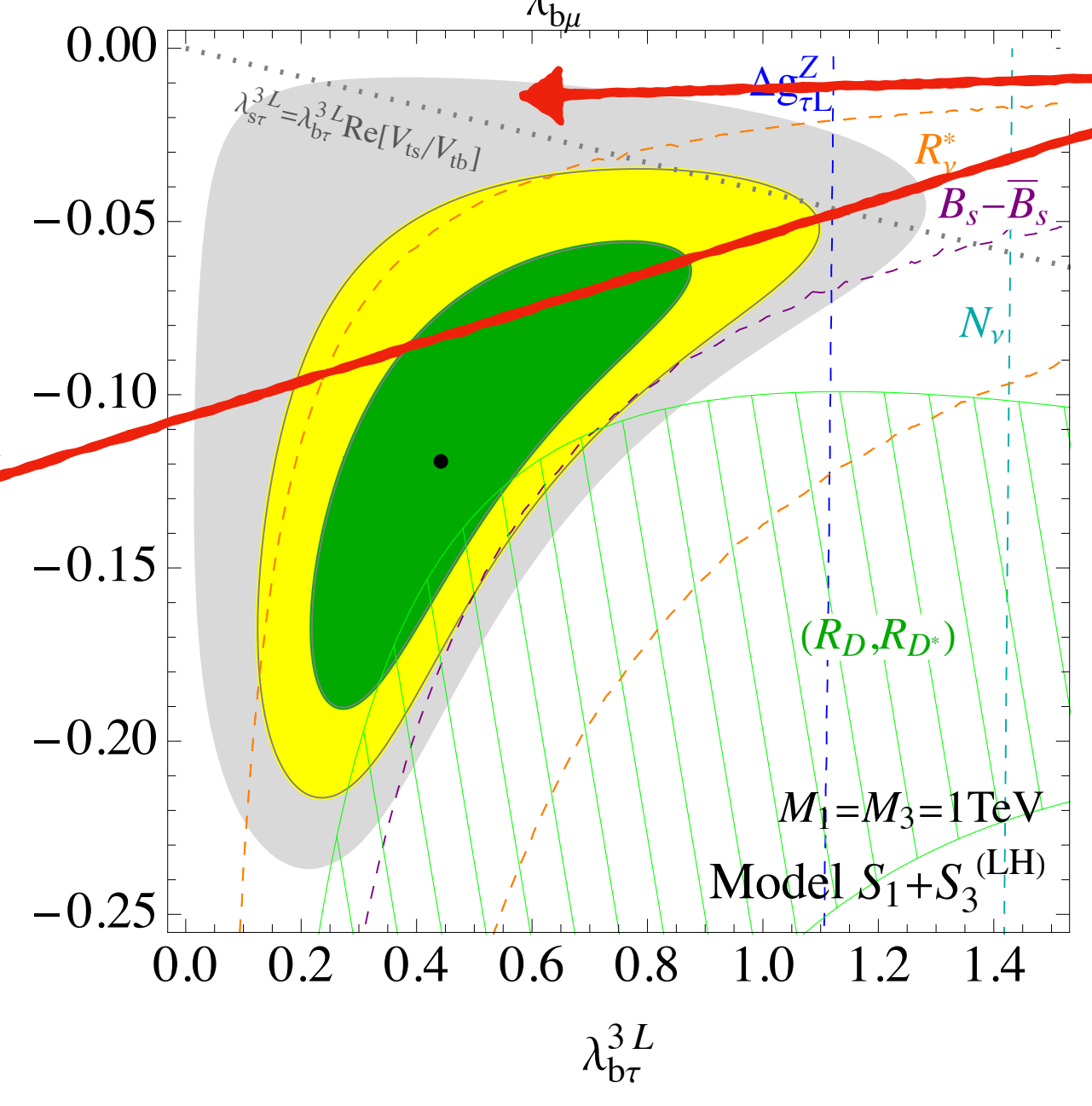
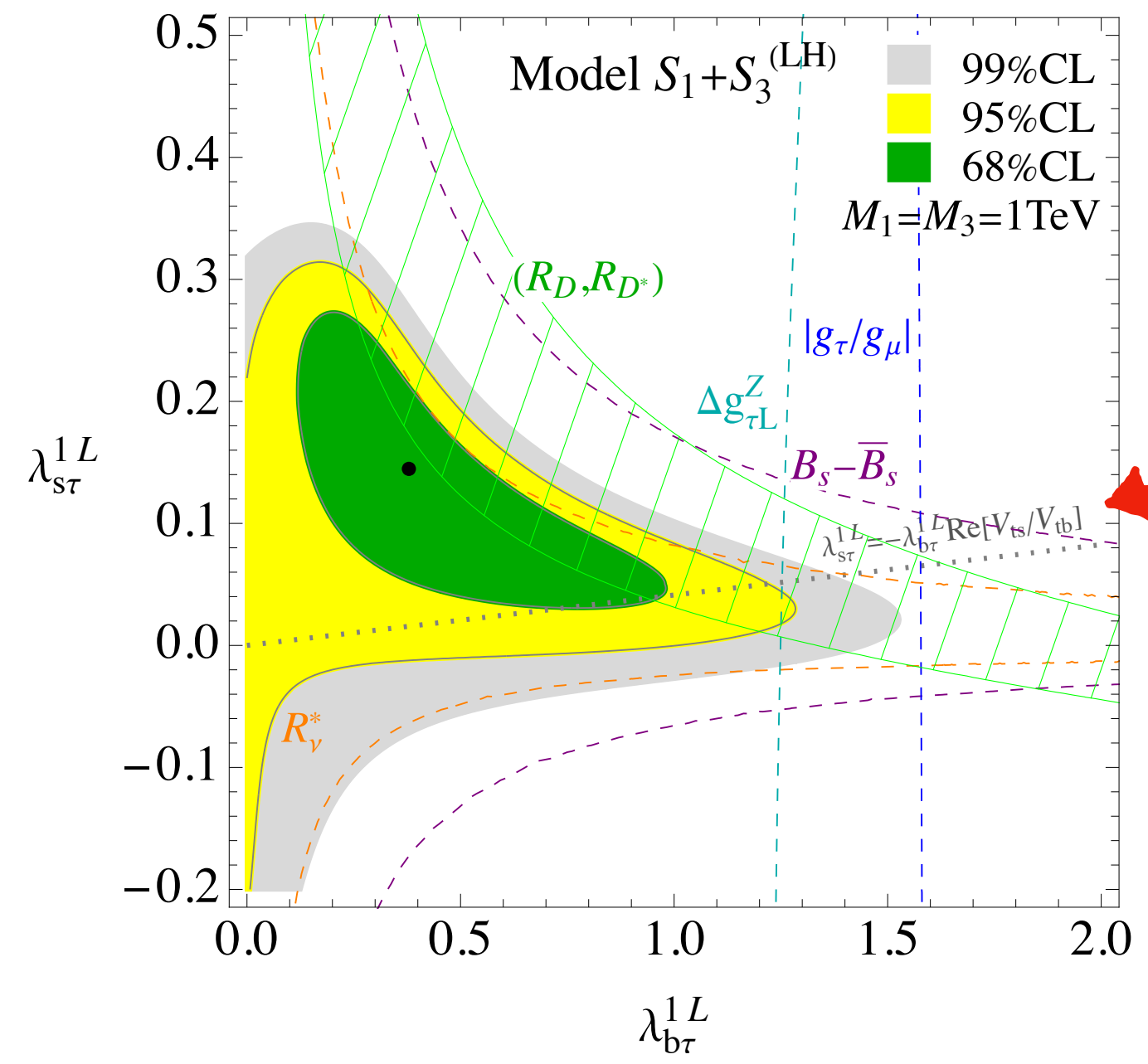
$\lambda 1R = 0 \rightarrow$  Cannot fit  $(g-2)_\mu$



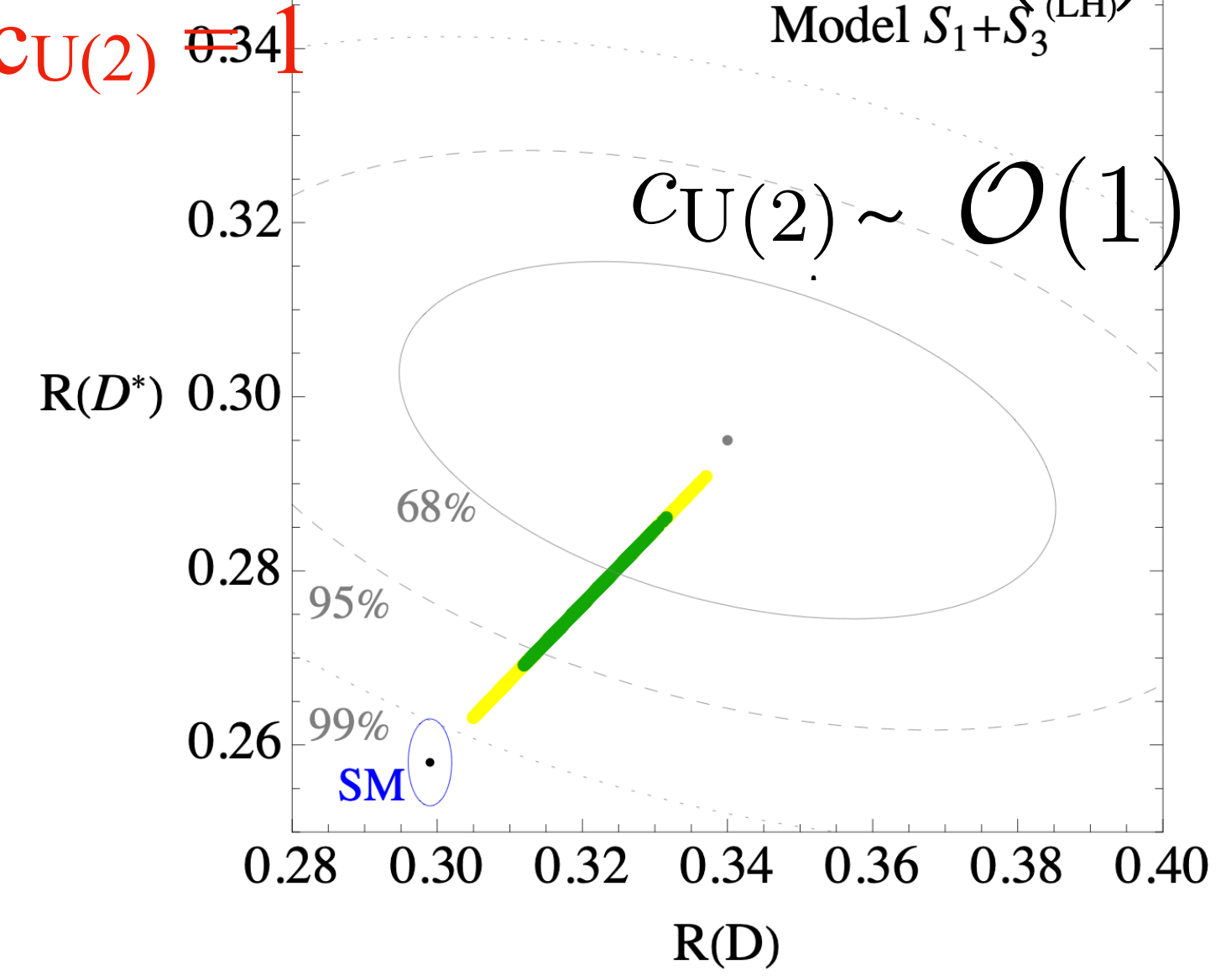
The relation between couplings to s-quark and b-quark is compatible with a  $U(2)^5$  flavour symmetry, that would predict:

**very good fit of B-anomalies**

R(D<sup>\*</sup>)

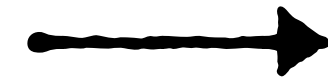


$$\lambda_{s\alpha} \stackrel{CU(2)}{=} C_{U(2)} V_{ts} \lambda_{b\alpha}$$



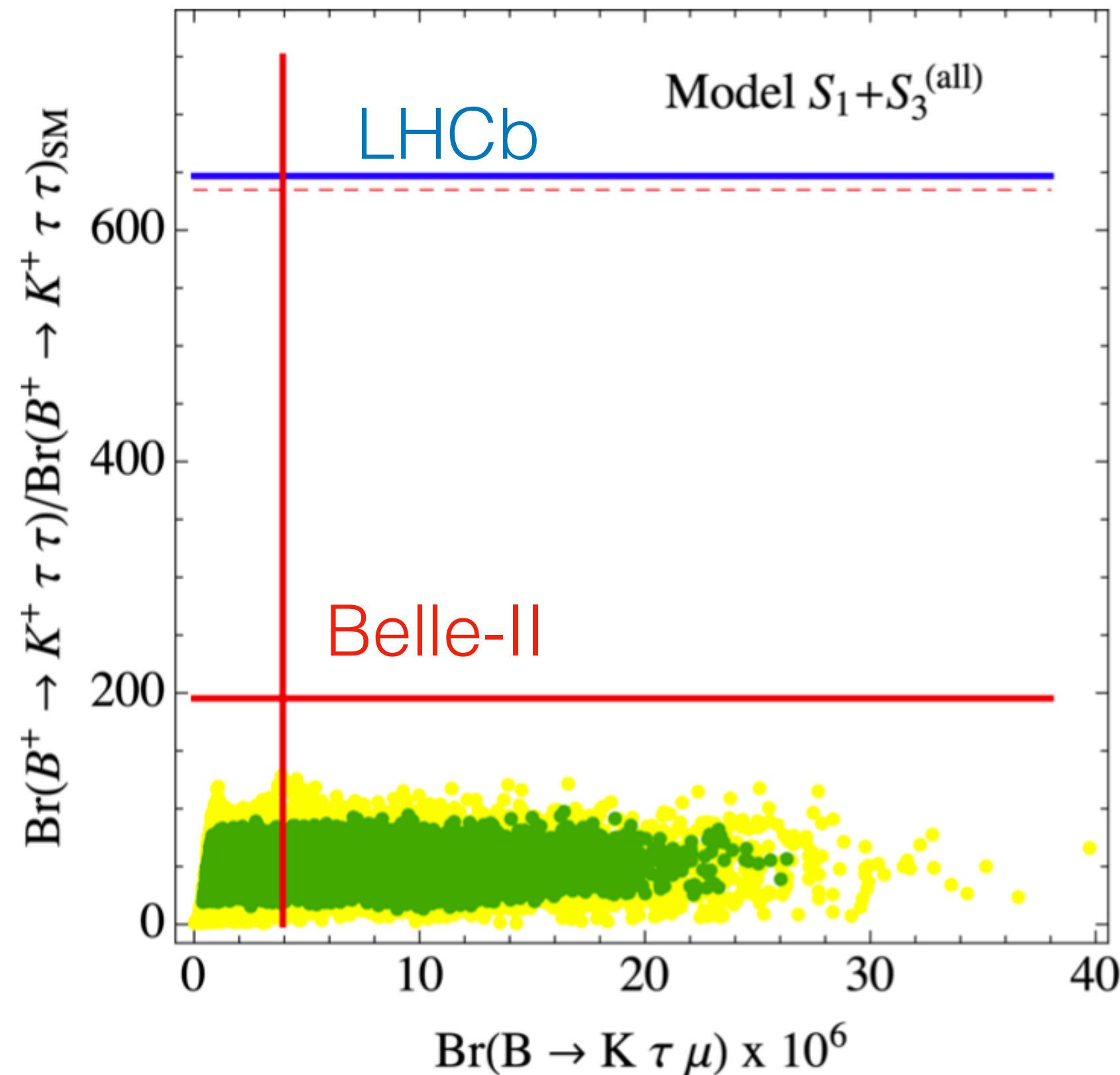
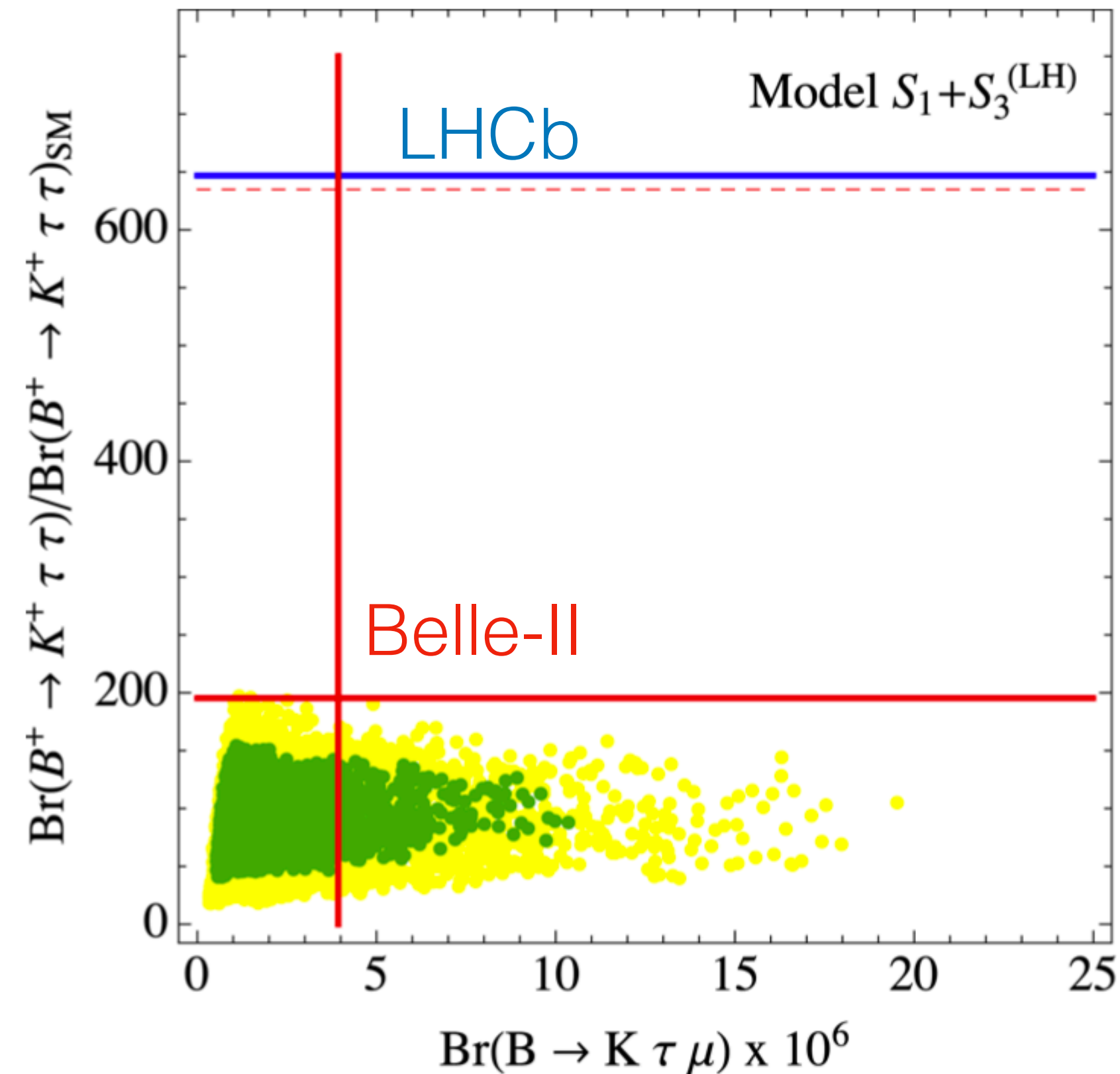
# Predictions

Typical for all models addressing B-anomalies



The large couplings to  $\tau$  imply signatures in DY tails of  $pp \rightarrow \tau\tau$ , deviations in  $\tau$  LFU tests and  $\tau \rightarrow \mu$  LFV tests (Belle-II). Also  $B_s$ -mixing is typically close to present bounds.

Large effects are also expected in  $b \rightarrow s \tau \tau$  and  $b \rightarrow s \tau \mu$  transitions:



# **From B to Kaon physics with scalar leptoquarks and $U(2)^5$ flavor symmetry**

D.M., S. Trifinopoulos, E. Venturini, in preparation [2106.yyyy]



# The motivation

$$b \rightarrow c \tau \nu \quad + \quad b \rightarrow s \mu \mu$$

↓

**TeV-scale leptoquark** coupled to **2nd** and **3rd** generation

In “realistic” flavor models LQ must also couple to **1st** generation fermions.

**What are the implications of this for:**

$s \rightarrow d$  i.e. Kaon physics

$\mu \rightarrow e$  LFV processes

?

# A hint towards $U(2)^5$

CC & NC B-anomalies fit with **only LH couplings**  
seems to be consistent with a  $U(2)^5$  flavor symmetry relation

$$\lambda^{1L} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & s\tau \\ 0 & 0 & b\tau \end{pmatrix} \quad \lambda^{3L} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & s\mu & s\tau \\ 0 & b\mu & b\tau \end{pmatrix} \quad \lambda^{1R} = \mathbf{0} \quad \lambda_{s\alpha} = c_{U(2)} V_{ts} \lambda_{b\alpha}$$

$c_{U(2)} \sim \mathcal{O}(1)$

A flavor model typically also predicts **couplings to 1st generation**

**Does the picture remain the same?**

**What is the impact of Kaon or  $\mu \rightarrow e$  observables?**

Similar question addressed in EFT context or in relation to  $b \rightarrow s\mu\mu$  only in:

Bordone, Buttazzo, Isidori, Monnard [1705.10729];

Borsato, Gligorov, Guadagnoli, Martinez Santos, Sumensari [1808.02006]

Fajfer, Kosnik, Vale-Silva [1802.00786]

# $U(2)^5$ flavour symmetry

Barbieri et al. [1105.2296, 1203.4218, 1211.5085]

In the limit where only 3rd gen fermions are massive, SM enjoys a **global symmetry**

$$G_F = U(2)_q \times U(2)_\ell \times U(2)_u \times U(2)_d \times U(2)_e$$

The **minimal breaking** of this symmetry due to Yukawas can be described in terms of some **spurions**, transforming under  $G_F$ :

$$\begin{aligned} \mathbf{V}_q &\sim (\mathbf{2}, \mathbf{1}, \mathbf{1}, \mathbf{1}, \mathbf{1}), & \mathbf{V}_\ell &\sim (\mathbf{1}, \mathbf{2}, \mathbf{1}, \mathbf{1}, \mathbf{1}), \\ \Delta_u &\sim (\mathbf{2}, \mathbf{1}, \bar{\mathbf{2}}, \mathbf{1}, \mathbf{1}), & \Delta_d &\sim (\mathbf{2}, \mathbf{1}, \mathbf{1}, \bar{\mathbf{2}}, \mathbf{1}), & \Delta_e &\sim (\mathbf{1}, \mathbf{2}, \mathbf{1}, \mathbf{1}, \bar{\mathbf{2}}). \end{aligned}$$

$$Y_{u(d)} = y_{t(b)} \begin{pmatrix} \Delta_{u(d)} & x_{t(b)} \mathbf{V}_q \\ 0 & 1 \end{pmatrix}, \quad Y_e = y_\tau \begin{pmatrix} \Delta_e & x_\tau \mathbf{V}_\ell \\ 0 & 1 \end{pmatrix} \quad x_{t,b,\tau} \text{ are } \mathcal{O}(1)$$

This is a **very good approximate symmetry**: the largest breaking has size  $\epsilon \approx y_t |V_{ts}| \approx 0.04$

Diagonalizing quark masses, the  **$V_q$  doublet spurion is fixed** to be  $\mathbf{V}_q = \kappa_q (V_{td}^*, V_{ts}^*)^T$   $\kappa_q \sim \mathcal{O}(1)$

See also Fuentes-Martin, Isidori, Pagès, Yamamoto [1909.02519]

# U(2)<sup>5</sup> flavour symmetry and leptoquarks

Applying the same symmetry assumptions to the leptoquark couplings to SM fermions we get a structure:

$$\lambda^{1(3)L} = \lambda^{1(3)} \begin{pmatrix} \begin{matrix} \mathbf{e}_L & & \\ X_{9l}^{1(3)} \mathbf{s}_e V_\ell V_{td} & X_{9l}^{1(3)} V_\ell V_{td} & X_9^{1(3)} V_{td} \\ X_{9l}^{1(3)} \mathbf{s}_e V_\ell V_{ts} & X_{9l}^{1(3)} V_\ell V_{ts} & X_9^{1(3)} V_{ts} \\ X_l^{1(3)} \mathbf{s}_e V_\ell & X_l^{1(3)} V_\ell & 1 \end{matrix} & \begin{matrix} \mathbf{d}_L \\ \mathbf{s}_L \\ \mathbf{b}_L \end{matrix} \end{pmatrix} \quad \lambda^{1R} \approx \lambda_R^1 \begin{pmatrix} 0 & 0 \\ 0 & \tilde{x}_{t\tau}^{1R} \end{pmatrix}$$

→ only RH coupling allowed is to  $t_R \tau_R$ .

$\mathbf{s}_e = \sin \vartheta_e$  : rotation diagonalizing electrons and muon masses

$V_\ell$  : leptonic doublet spurion

$\mathbf{x}^{1(3)}$ : **O(1)** arbitrary complex parameters.

} *Arbitrary parameters*

Generic features of U(2)<sup>5</sup> symmetry:

- Largest couplings to  $\mathbf{b}_L$ ,  $\mathbf{t}_L$ ,  $\mathbf{\tau}_L$  and  $\mathbf{v}_\tau$ ,
- Coupl. to  $\mathbf{s}_L$  suppressed by  $\sim V_{ts}$ ,
- Coupl. to  $\mathbf{d}_L$  suppressed by  $\sim V_{td}$ ,
- Coupl. to  $\mathbf{\mu}_L$  suppressed by  $V_\ell$ ,
- Coupl. to  $\mathbf{e}_L$  suppressed by  $\mathbf{s}_e V_\ell$ .

# U(2)<sup>5</sup> flavour symmetry and leptoquarks

Applying the same symmetry assumptions to the leptoquark couplings to SM fermions we get a structure:

$$\lambda^{1(3)L} = \lambda^{1(3)} \begin{pmatrix} X_{9l}^{1(3)} S_e V_l V_{td} & X_{9l}^{1(3)} V_l V_{td} & X_9^{1(3)} V_{td} \\ X_{9l}^{1(3)} S_e V_l V_{ts} & X_{9l}^{1(3)} V_l V_{ts} & X_9^{1(3)} V_{ts} \\ X_l^{1(3)} S_e V_l & X_l^{1(3)} V_l & 1 \end{pmatrix} \begin{matrix} \mathbf{d}_L \\ \mathbf{s}_L \\ \mathbf{b}_L \end{matrix}$$

$$\lambda^{1R} \approx \lambda_R^1 \begin{pmatrix} 0 & 0 \\ 0 & \tilde{x}_{t\tau}^{1R} \end{pmatrix}$$

→ only RH coupling allowed is to  $t_R \tau_R$ .

$S_e = \sin \vartheta_e$  : rotation diagonalizing electrons and muon masses

$V_l$  : leptonic doublet spurion

$x^{1(3)}$ : **O(1)** arbitrary complex parameters.

} *Arbitrary parameters*

The leptoquark **couplings to first generations** are now **fixed** in terms of couplings to the second generation:

$$\lambda_{d\alpha}^{1(3)L} = \lambda_{s\alpha}^{1(3)L} \frac{V_{td}}{V_{ts}}$$

$$\lambda_{ie}^{1(3)L} = \lambda_{i\mu}^{1(3)L} \sin \vartheta_e$$

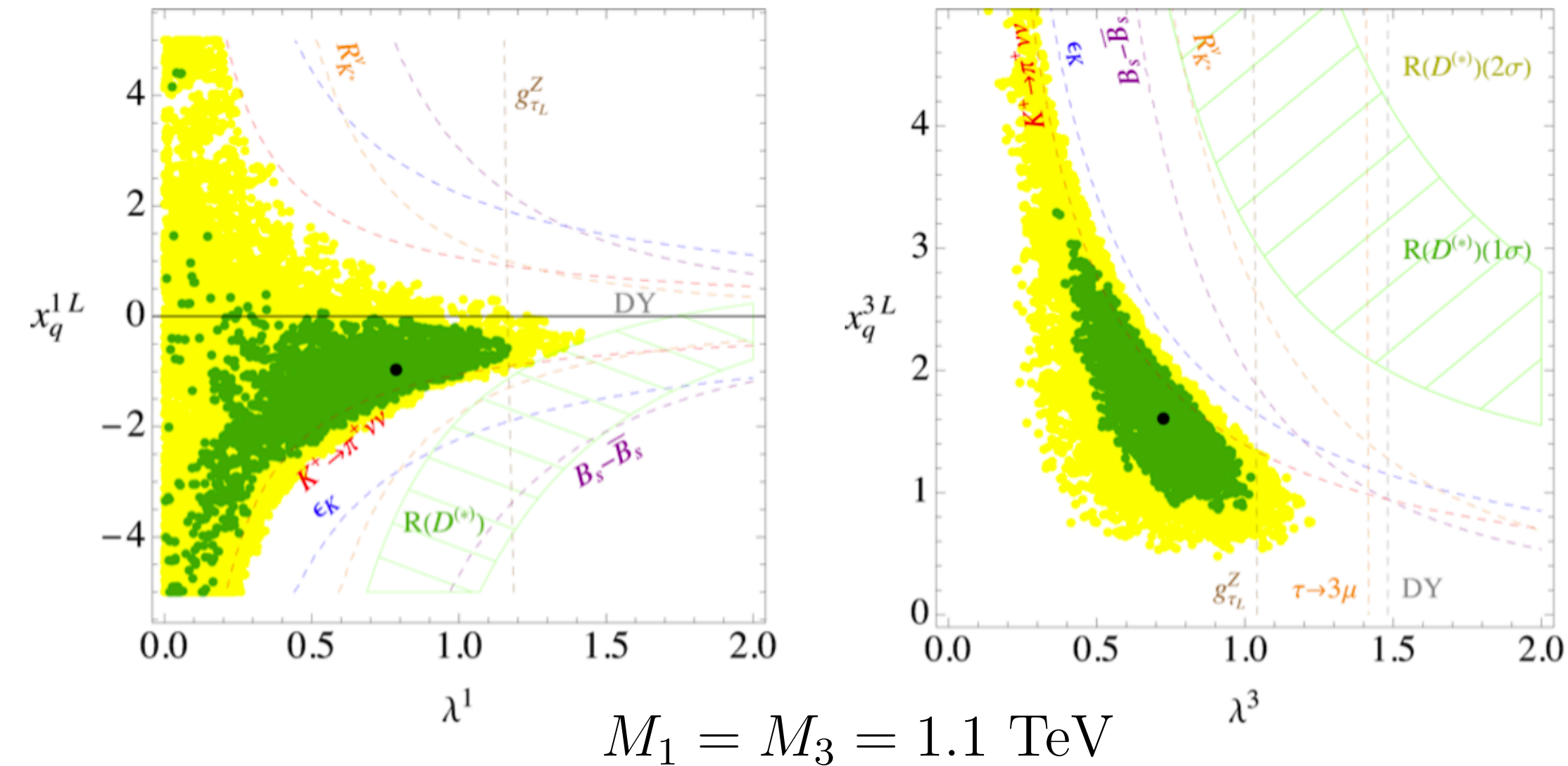
**Exact relations  
(selection rules)**

We can now **correlate Kaon physics** observables **to B-anomalies!**

# From B to K with LQ and $U(2)^5$

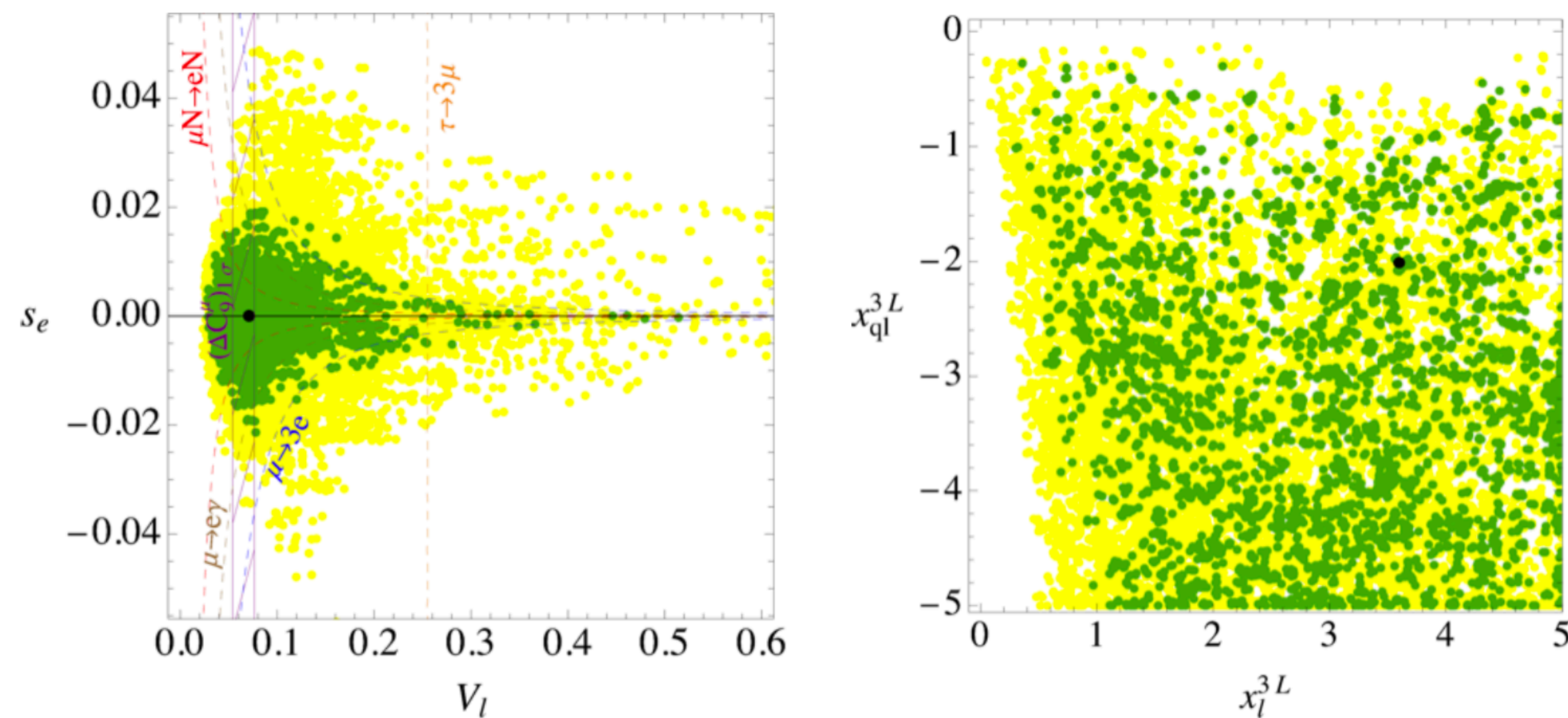
S. Trifinopoulos, E. Venturini, D.M. [2106.15630]

We perform a global fit in the  $U(2)^5$  flavour structure.



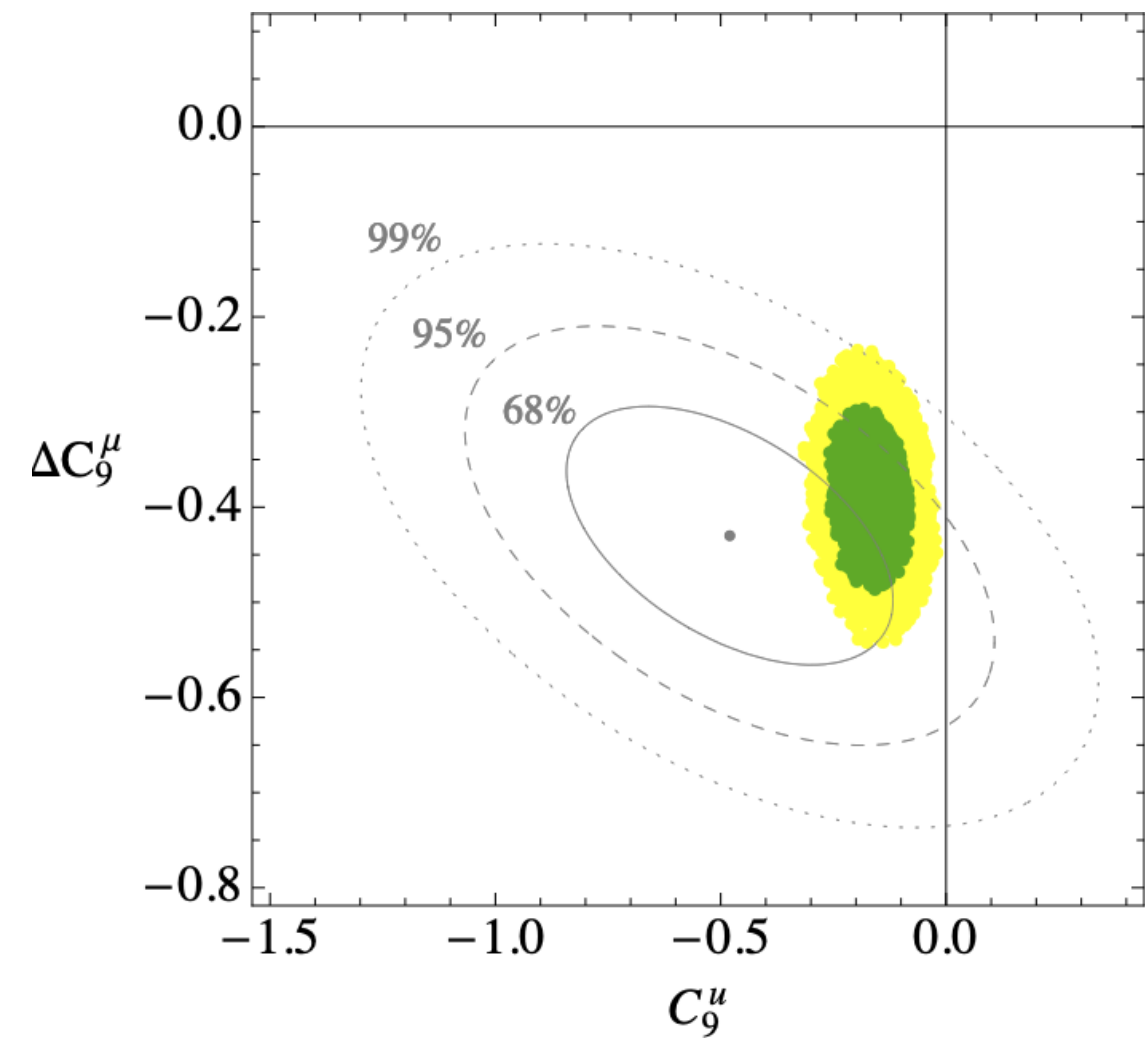
- The parameters are indeed consistent with a  $U(2)^5$  structure: **all  $x$ 's are  $O(1)$ .**

-  $V_\ell \sim 0.1$ ,  $|s_e| \simeq 0.02$

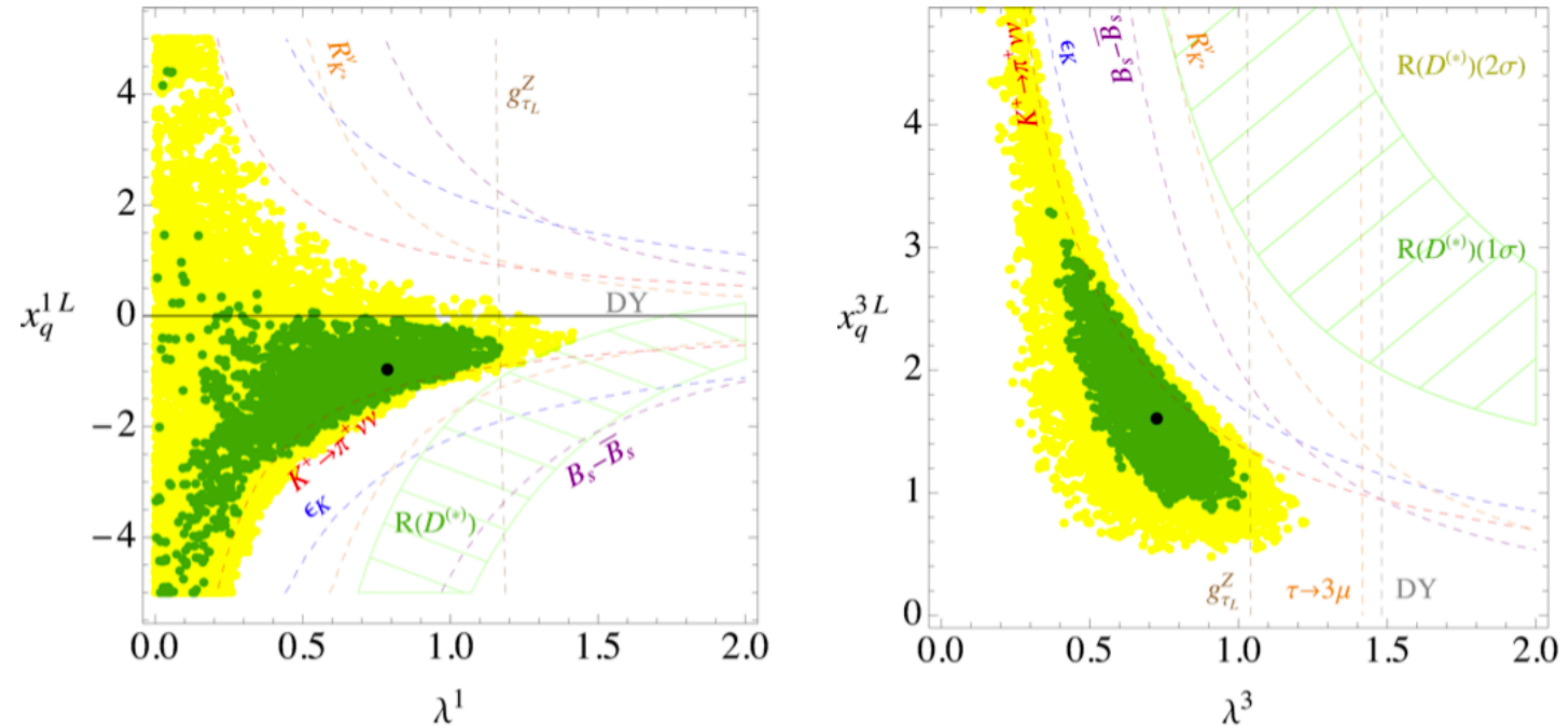


# From B to K with LQ and U(2)<sup>5</sup>

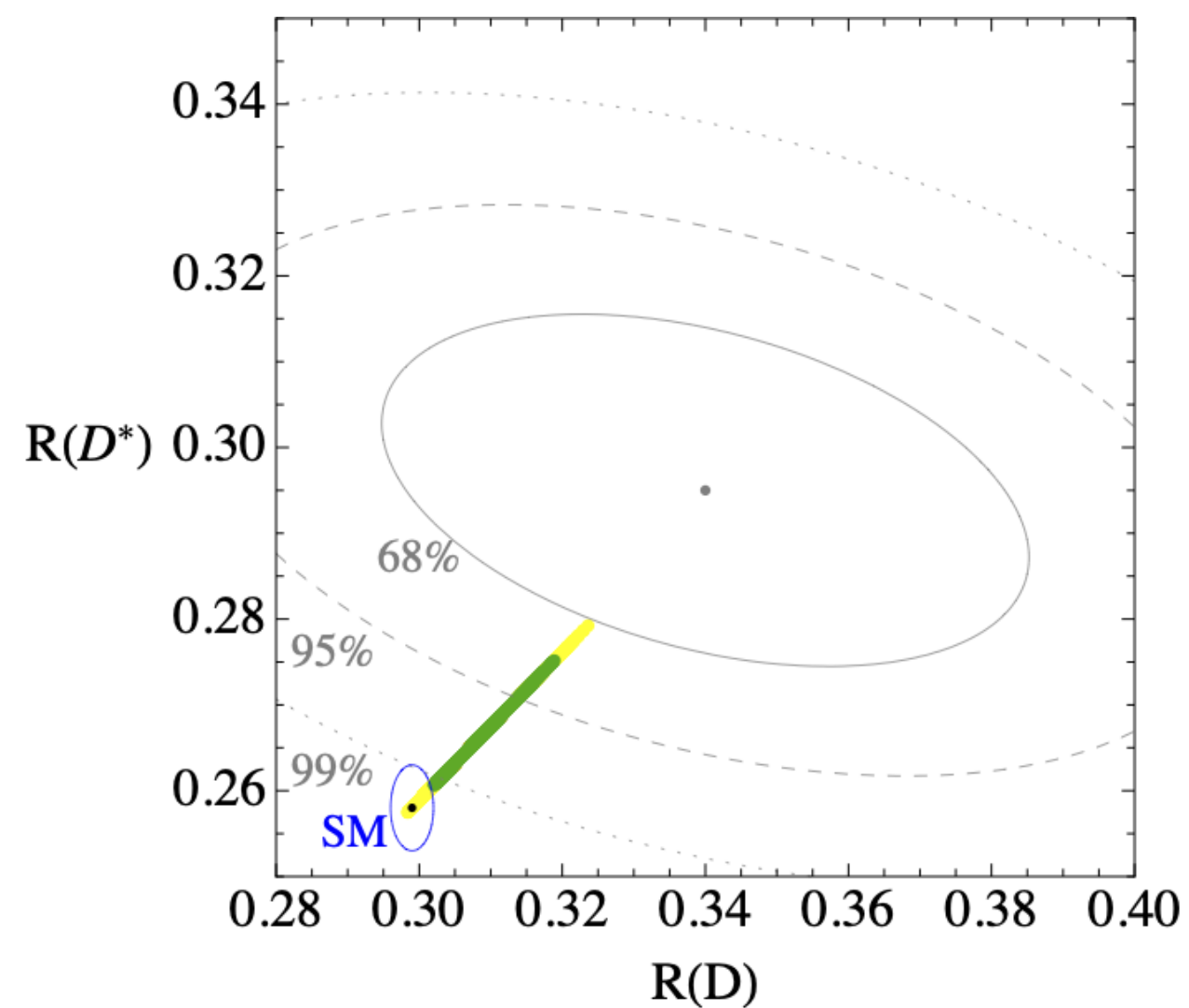
$b \rightarrow s \mu \mu$  can be addressed:



This is due to the combination of the **constraints from  $Z \rightarrow \tau\tau$  and  $K^+ \rightarrow \pi^+ \nu\nu$**



$R(D^{(*)})$  instead can only be addressed at  $2\sigma$ :



$R(D^{(*)})$

$$\frac{\Delta R(D^{(*)})}{R(D^{(*)})_{\text{SM}}} \approx v^2 \left( 1.09 \frac{|\lambda^1|^2 (1 - x_q^{1*} V_{tb}^*)}{2M_1^2} - 1.02 \frac{|\lambda^3|^2 (1 - x_q^{3*} V_{tb}^*)}{2M_3^2} \right)$$

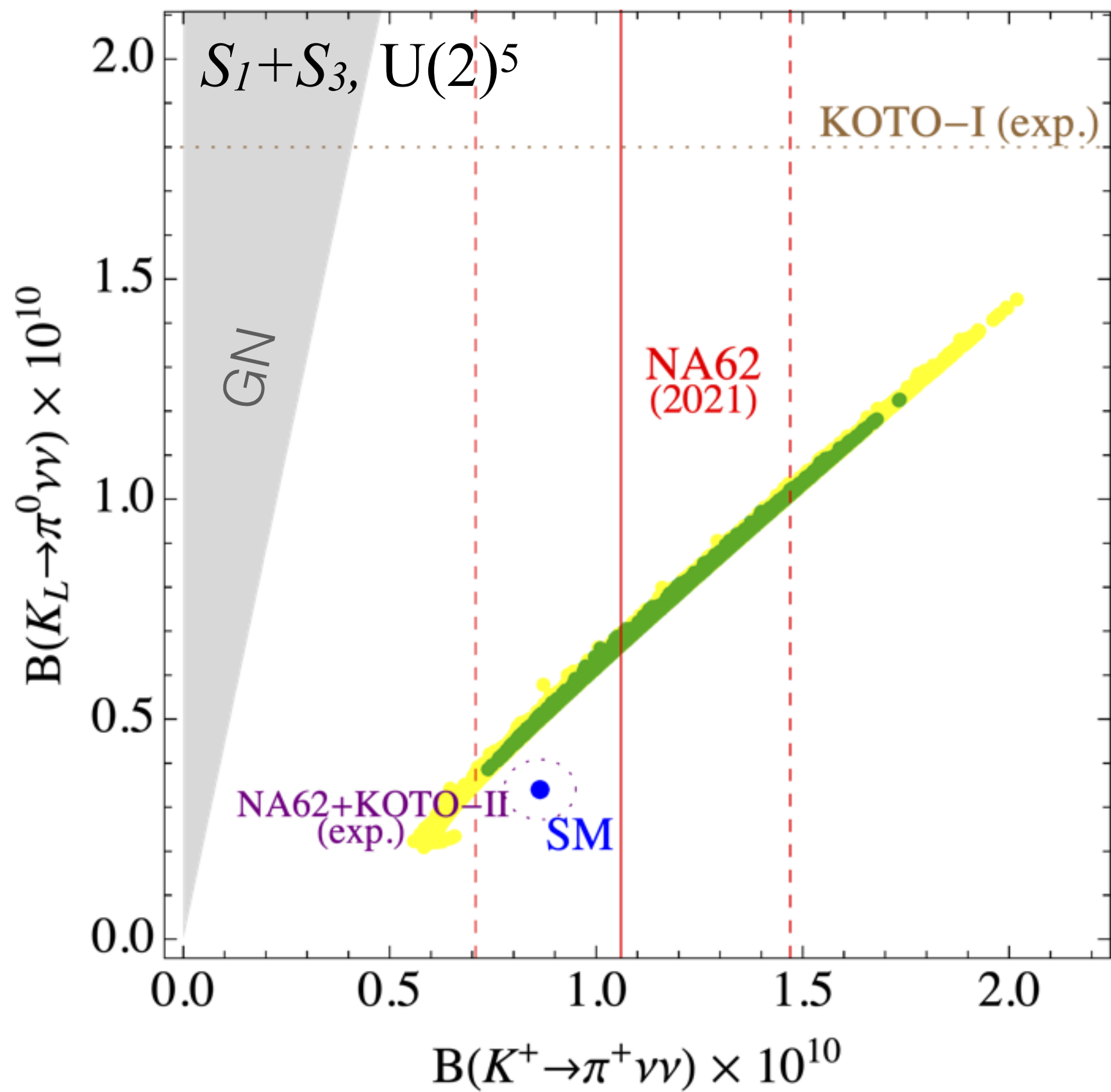
$K^+ \rightarrow \pi^+ \nu\nu$

$$[L_{\nu d}^{VLL}]_{\nu\tau\nu\tau ds} \approx V_{td}^* V_{ts} \left( \frac{|\lambda^1|^2 |x_q^1|^2}{2M_1^2} + \frac{|\lambda^3|^2 |x_q^3|^2}{2M_3^2} \right)$$

$Z \rightarrow \tau\tau$

$$10^3 \delta g_{\tau L}^Z \approx 0.59 \frac{|\lambda^1|^2}{M_1^2 / \text{TeV}^2} + 0.80 \frac{|\lambda^1|^2}{M_1^2 / \text{TeV}^2}$$

# Leading effects in Kaon physics



Dominated by **tau neutrinos**, due to largest couplings.

The **NA62 bound is already very constraining** for this setup, future updated will put even more tension with  $R(D^{(*)})$ , or eventually a signal could be observed.

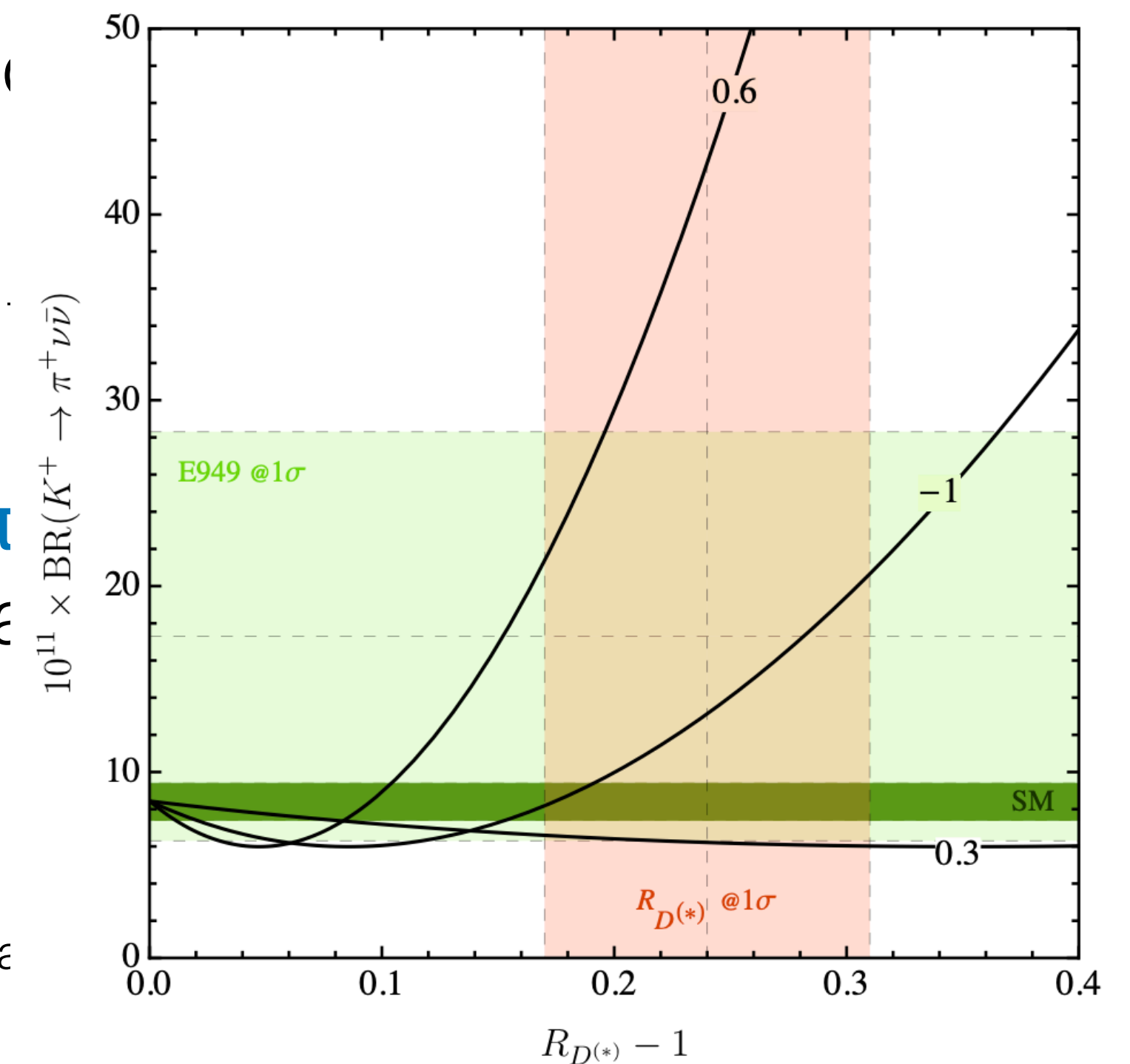
The correlation in the full model is stronger than just in EFT.

[see: Bordone, Buttazzo, Isidori, Monnard 1705.10729]

The **phase of NP** contribution

$$[L_{\nu d}^{VLL}]_{\nu_\tau \nu_\tau ds} \approx V_{td}^* V_{ts} \left( \dots \right)$$

As consequence, the  $K_L \rightarrow \pi$  below the KOTO stage-I final

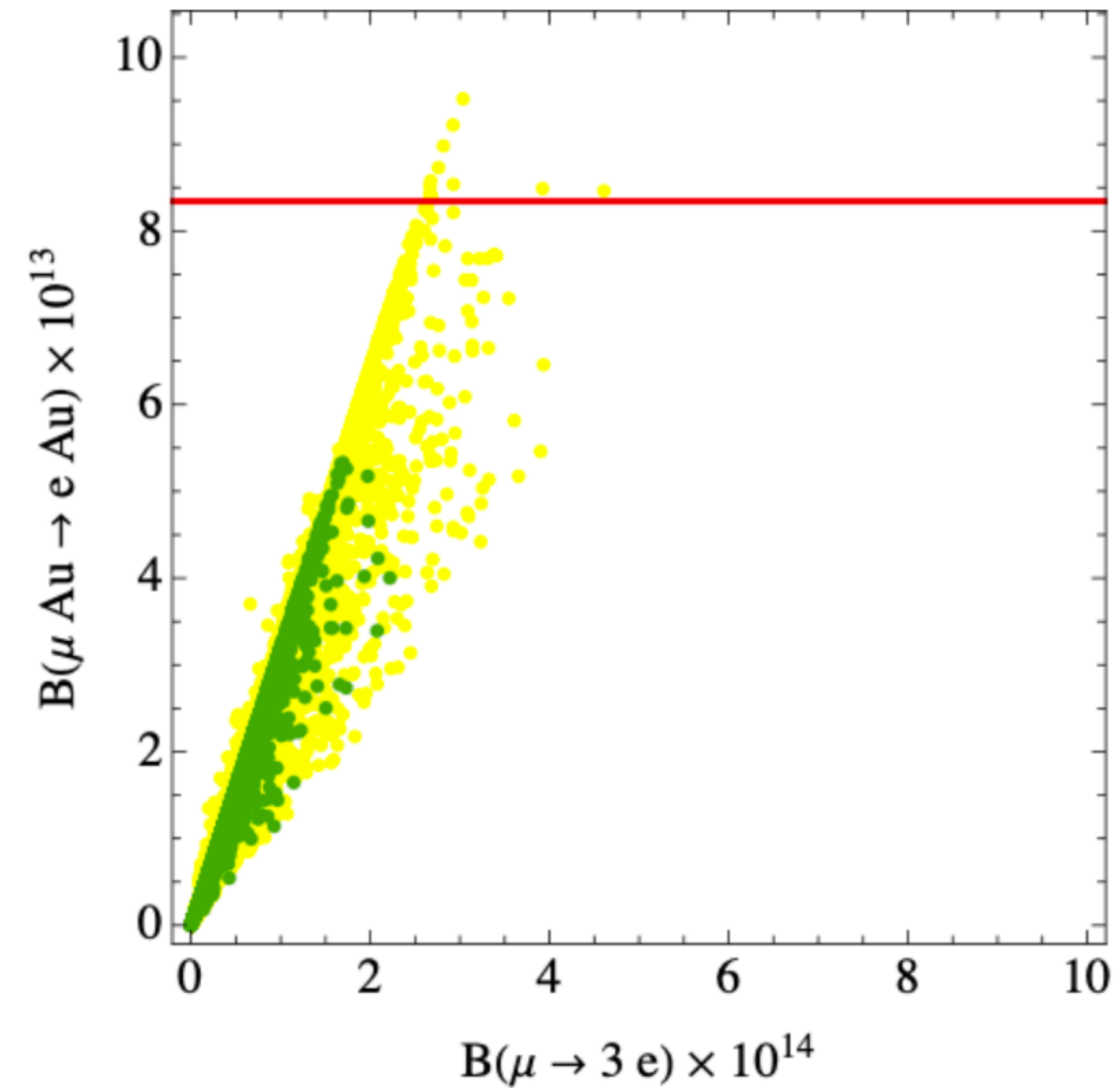


About other Kaon decays:

The effect in  $K_L \rightarrow \mu\mu$  saturates the bound, while the SD contribution to  $K_S \rightarrow \mu\mu$  is  $\sim 10^{-13}$  (b.e). We also obtain  $\text{Br}(K_L \rightarrow \mu e) \sim 10^{-15}$  and  $\text{Br}(K^+ \rightarrow \pi^+ \mu e) \sim 10^{-18}$ .



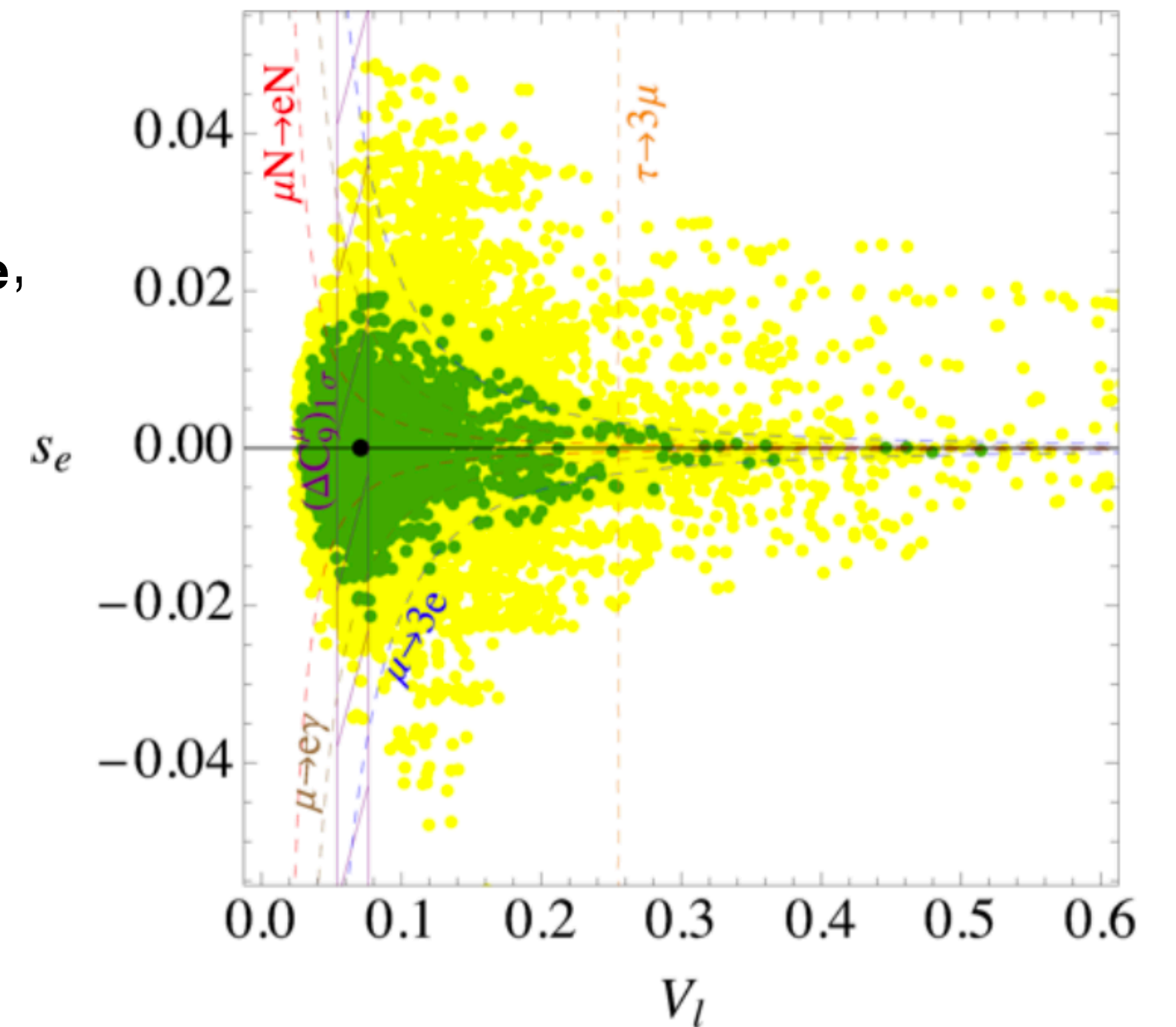
# $\mu \rightarrow e$ conversion



$\mu \rightarrow e$  conversion in gold nuclei sets the **strongest constraint on  $s_e$** .

*COMET* and *Mu2e* will push this bound to  $\sim 10^{-16}$ , while *Mu3e* at PSI will push the limit on  **$\text{Br}(\mu \rightarrow 3e)$**  to  $\sim 10^{-16}$ .

These will set much stronger **bounds on  $s_e$** , or could see a New Physics effect.



# Combined interpretation of $R_K$ , $R(D^{(*)})$ , $(g-2)_\mu$ , and CAA

DM, Sokratis Trifinopoulos  
PRL **127**, 061803 (2021) [2104.05730]

$$S_1 \sim (\bar{\mathbf{3}}, \mathbf{1})_{1/3} , \quad \phi^+ \sim (\mathbf{1}, \mathbf{1})_1$$

# A do-it-all model?

Let us consider a simplified model with only these two new weak-singlets states:

$$S_1 \sim (\bar{\mathbf{3}}, \mathbf{1})_{1/3}, \quad \phi^+ \sim (\mathbf{1}, \mathbf{1})_1$$

**Note:** same gauge quantum numbers as **sbottom** and **stau**, but different **L** and **B** assignments.

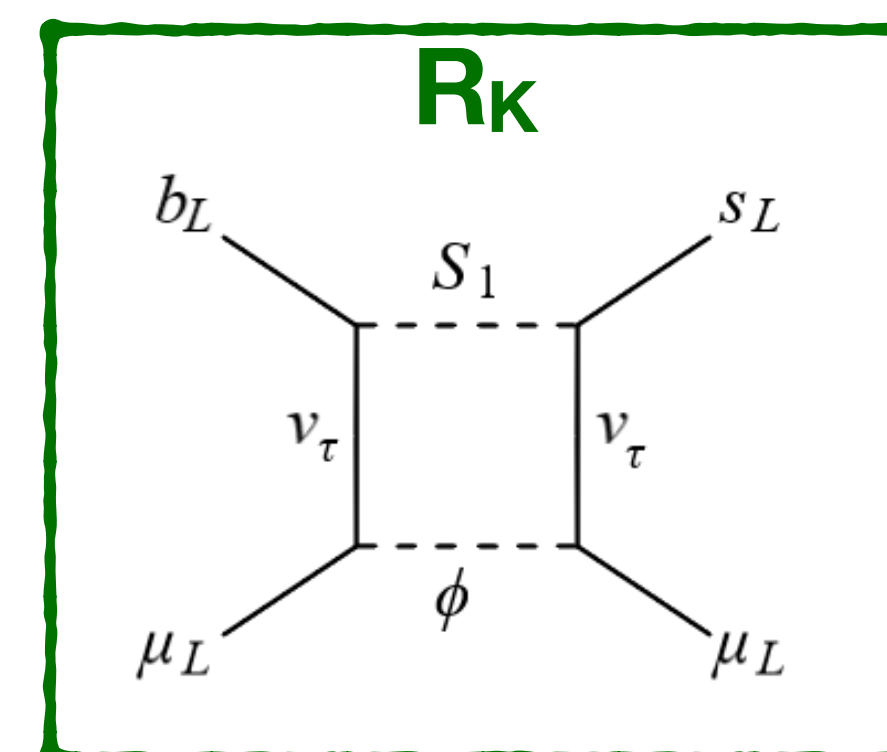
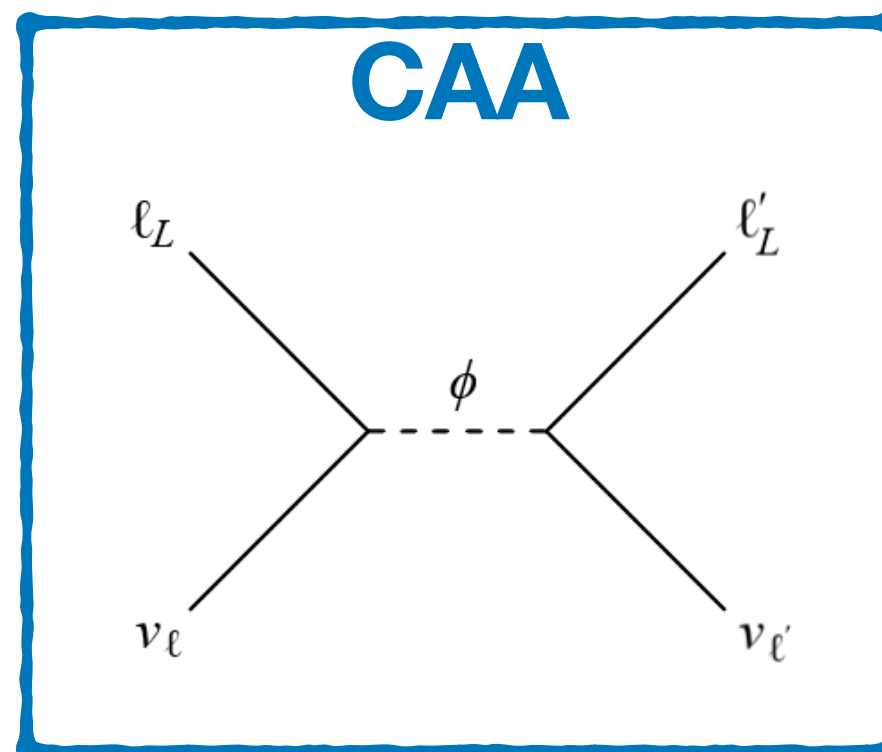
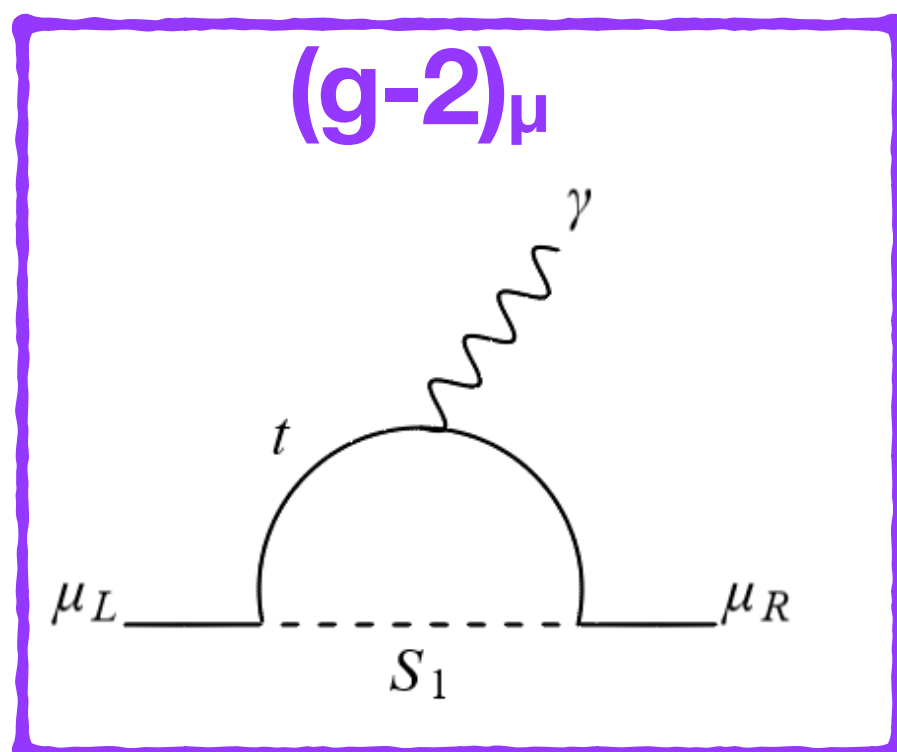
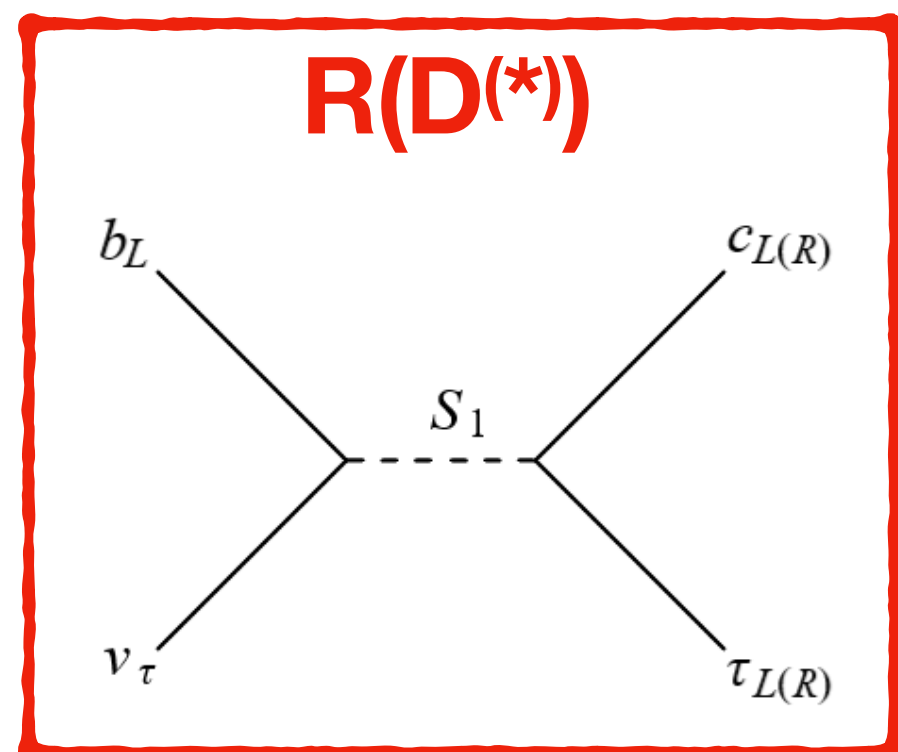
$\phi^+$  couples to di-leptons:

$$\mathcal{L}_{S_1+\phi} = \frac{1}{2} \lambda_{\alpha\beta} \bar{\ell}_\alpha^c \ell_\beta \phi^+ + \lambda_{i\alpha}^{1L} \bar{q}_i^c \ell_\alpha S_1 + \lambda_{i\alpha}^{1R} \bar{u}_i^c e_\alpha S_1 + \text{h.c.}$$

**S<sub>1</sub>**

**ϕ<sup>+</sup>**

**S<sub>1</sub> + ϕ<sup>+</sup>**



Crivellin, Kirk, Manzari, Panizzi 2012.09845;  
Felkl, Herrero-Garcia, Schmidt 2102.09898

$$R_D \approx 0.299 - 0.235 \frac{\lambda_{b\tau}^{1L} \lambda_{c\tau}^{1R}}{m_1^2} (1 + 0.05 \log m_1^2)$$

$$R_{D^*} \approx 0.258 - 0.088 \frac{\lambda_{b\tau}^{1L} \lambda_{c\tau}^{1R}}{m_1^2} (1 + 0.02 \log m_1^2)$$

$$\Delta a_\mu \approx \frac{m_\mu m_t \lambda_{b\mu}^{1L} \lambda_{t\mu}^{1R}}{4\pi^2 M_1^2} \left( \log M_1^2 / m_t^2 - \frac{7}{4} \right)$$

$$\delta(\mu \rightarrow e\nu\nu) \approx \frac{v^2 |\lambda_{12}|^2}{4M_\phi^2} + \frac{3m_t^2 |\lambda_{b\mu}^{1L}|^2}{32\pi^2 M_1^2} \left( \frac{1}{2} - \log \frac{M_1^2}{m_t^2} \right)$$

$$\mathcal{O}_{LL(LR)}^{bs\mu\mu} = (\bar{s}\gamma^\alpha P_L b)(\bar{\mu}\gamma_\alpha P_{L(R)}\mu)$$

$$C_{LL} \approx -\lambda_{b\tau}^{1L} \lambda_{s\tau}^{1L*} \left( \frac{|\lambda_{b\mu}^{1L}|^2}{64\pi^2 M_1^2} + \frac{|\lambda_{\mu\tau}|^2 \log M_1^2 / M_\phi^2}{64\pi^2 (M_\phi^2 - M_1^2)} \right)$$

$$C_{LR} \approx -\frac{|\lambda_{c\mu}^{1R}|^2 \lambda_{b\tau}^{1L} \lambda_{s\tau}^{1L*}}{64\pi^2 M_1^2}$$

$$C_{B_s}^1 = \frac{(\lambda_{b\tau}^{1L*} \lambda_{s\tau}^{1L})^2}{128\pi^2 M_1^2}, \quad C_D^1 = \frac{(V_{ci} \lambda_{i\alpha}^{1L*} \lambda_{j\alpha}^{1L} V_{uj}^*)^2}{128\pi^2 M_1^2}$$

**Large masses** are preferred to avoid meson mixing.

We fix:  $M_1 = M_\phi = 5.5\text{TeV}$

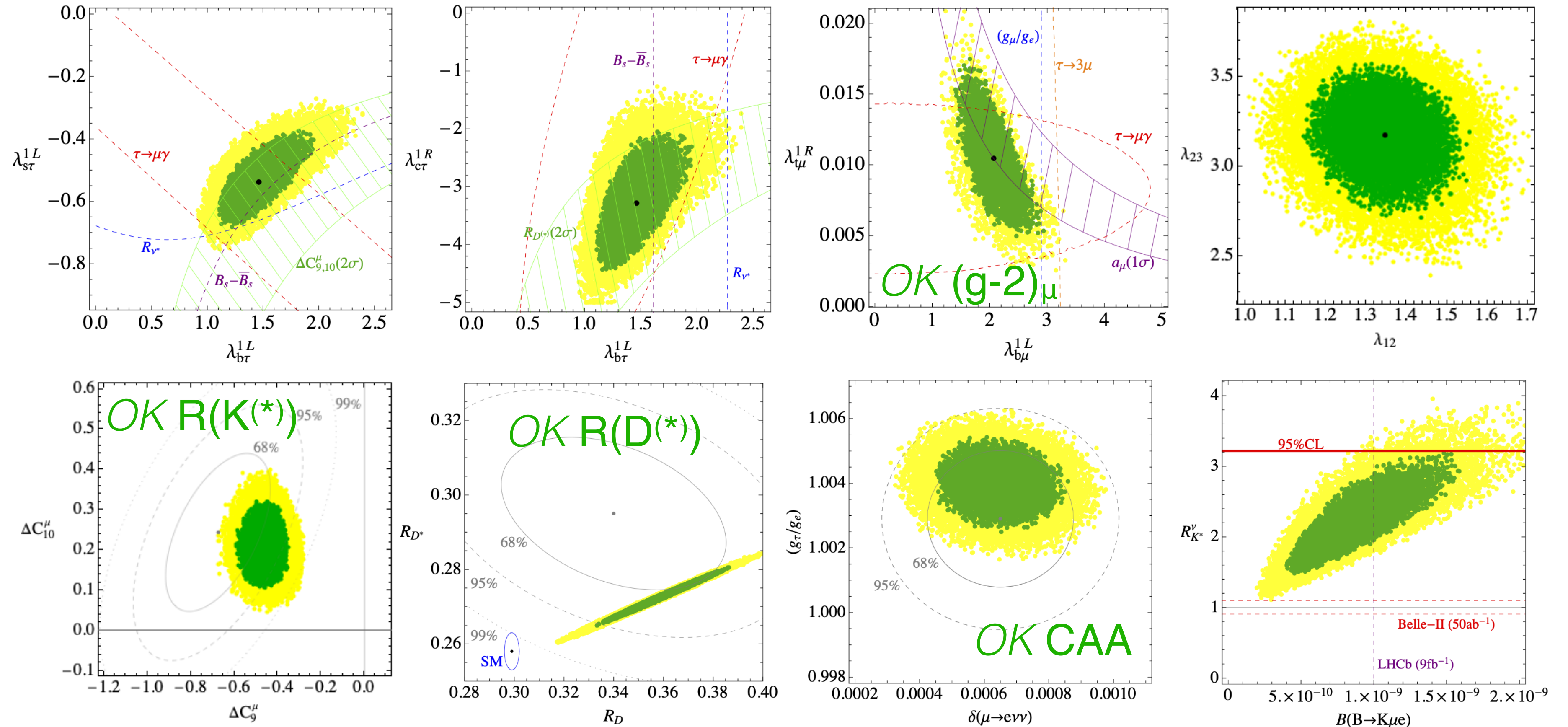
# A do-it-all model?

DM, Sokratis Trifinopoulos 2104.05730

We do a global analysis including all the observables

$$M_1 = M_\phi = 5.5\text{TeV}$$

Observable	Experimental value
$R_D$	$0.34 \pm 0.029$ [56]
$R_{D^*}$	$0.295 \pm 0.013$ [56]
$\Delta C_9^\mu$	$-0.675 \pm 0.16$ [20]
$\Delta C_{10}^\mu$	$0.244 \pm 0.13$ [20]
$\Delta a_\mu$	$(2.51 \pm 0.59) \times 10^{-9}$ [27, 28]
$\delta(\mu \rightarrow e\nu\nu)$	$(6.5 \pm 1.5) \times 10^{-4}$ [41]
$R_D^{\mu/e}$	$0.978 \pm 0.035$ [57, 58]
$\mathcal{B}(B_c \rightarrow \tau\nu)$	$< 0.1$ [59]
$R_{K^{(*)}}^\nu$	$< 2.7$ [60]
$C_{B_s}^1$	$< 2.01 \times 10^{-5} \text{ TeV}^{-2}$ [61]
$ \text{Re}(C_D^1) $	$< 3.57 \times 10^{-7} \text{ TeV}^{-2}$ [61]
$ \text{Im}(C_D^1) $	$< 2.23 \times 10^{-8} \text{ TeV}^{-2}$ [61]
$\frac{g_\tau}{g_e}$	$1.0058 \pm 0.0030$ [56]
$\frac{g_\tau}{g_\mu}$	$1.0022 \pm 0.0030$ [56]
$\frac{g_\mu}{g_e}$	$1.0036 \pm 0.0028$ [56]
$\delta g_{\tau L}^Z$	$(-0.11 \pm 0.61) \times 10^{-3}$ [62]
$\delta g_{\tau R}^Z$	$(0.66 \pm 0.65) \times 10^{-3}$ [62]
$\delta g_{\mu L}^Z$	$(0.3 \pm 1.1) \times 10^{-3}$ [62]
$\delta g_{\mu R}^Z$	$(0.2 \pm 1.3) \times 10^{-3}$ [62]
$\mathcal{B}(\tau \rightarrow \mu\gamma)$	$< 4.4 \times 10^{-8}$ [63]
$\mathcal{B}(\tau \rightarrow 3\mu)$	$< 2.1 \times 10^{-8}$ [63]



- **Good fit** of all anomalies
- **Cancellation** of approx. **1 part in 3** required to avoid  $\tau \rightarrow \mu\gamma$ : via  $\lambda_{c\mu}^{1R}$
- **Large couplings** required, due to the large masses needed to avoid meson mixing.

# Conclusions

- **Flavor anomalies** still require data (and theory) to give us a definitive picture, some could stay, some could go.
- If any will remain, it will be a revolutionary **stepping stone to an unexpected New Physics sector!**

We must **keep an open mind** and **explore all possibilities**.

- Exploring combined explanations is a useful exploratory exercise, it allows us to **connect B-anomalies with other observables**, both at high and low energy.
- Observations or limits from correlated effects in completely different processes will be crucial to understand the underlying UV physics and its flavor structure.

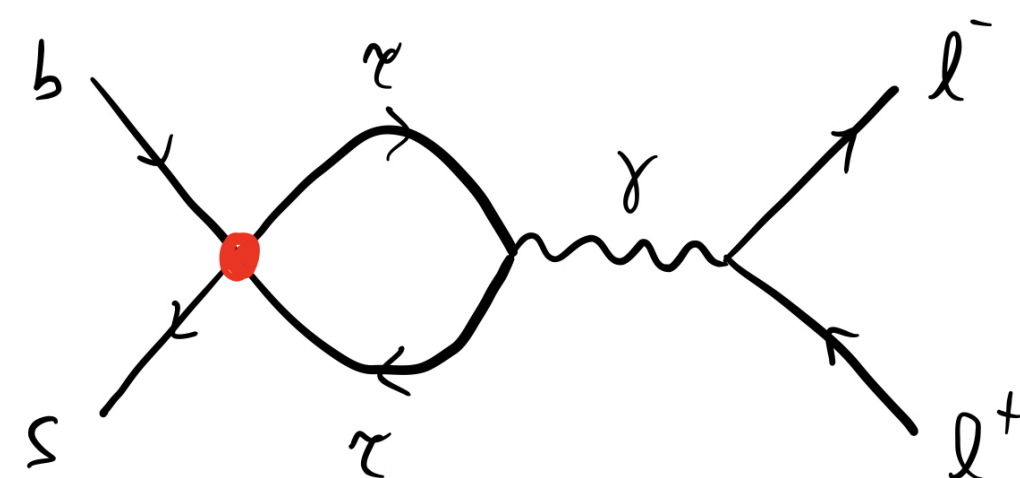
***Thank you!***

# Backup

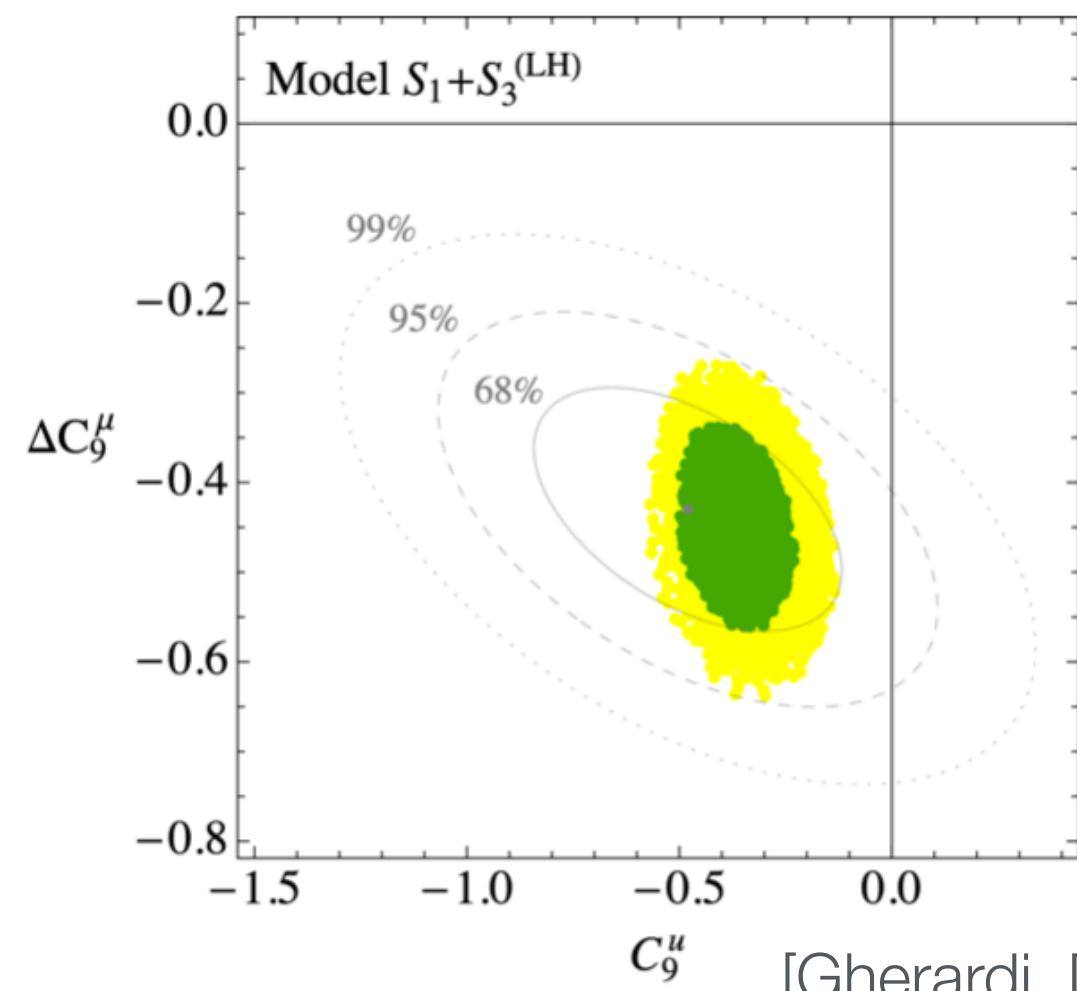
# From $R_K$ to $R(D^{(*)})$ anomalies

A large coupling to the  $\tau$  induces an RG-enhanced **lepton-flavor universal** contribution proportional to  $C_9^U$

Capdevila et al. 1712.01919, Crivellin et al. 1807.02068



$$C_9^U \approx 7.5 \left( 1 - \sqrt{\frac{R_{D^{(*)}}}{R_{D^{(*)}SM}}} \right) \left( 1 + \frac{\log(\Lambda^2/(1\text{TeV}^2))}{10.5} \right)$$



$$R_K \longrightarrow \sim \frac{g_\mu V_{ts}}{\Lambda^2} (\bar{b}_L \gamma_\alpha s_L) (\bar{\mu}_L \gamma^\alpha \mu_L)$$

$$\Lambda/\sqrt{g_\mu} \sim 7 \text{ TeV}$$

CKM-like flavor structure

SM gauge invariance  $SU(2)_L$

$$C_T (\bar{Q}_L^i \gamma_\mu \sigma^a Q_L^j) (\bar{L}_L^\alpha \gamma^\mu \sigma^a L_L^\beta) + C_S (\bar{Q}_L^i \gamma_\mu Q_L^j) (\bar{L}_L^\alpha \gamma^\mu L_L^\beta)$$

Usually UV physics generates both. The exception are  $Z'$  models, which generate only the singlet

$$\sim \frac{g_\mu V_{cb}}{\Lambda^2} (\bar{b}_L \gamma_\alpha c_L) (\bar{\nu}_L^\mu \gamma^\alpha \mu_L)$$

Charged-current in muons

Generalising lepton flavour

$$\sim \frac{g_\tau V_{cb}}{\Lambda^2} (\bar{b}_L \gamma_\alpha c_L) (\bar{\nu}_L^\tau \gamma^\alpha \tau_L)$$

$R(D^{(*)})$

$$\Lambda/\sqrt{g_\tau} \sim 1 \text{ TeV}$$

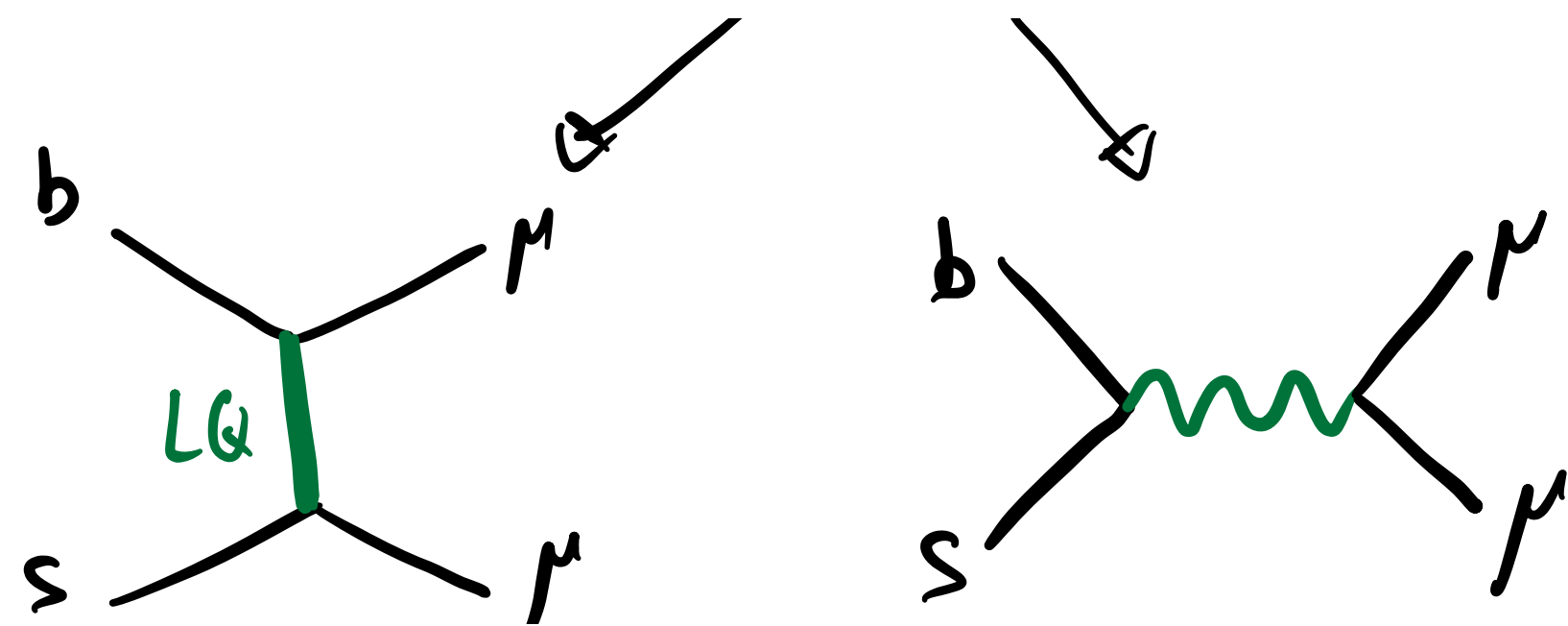
If  $g_e \ll g_\mu \ll g_\tau$  same hierarchy as

$$m_e \ll m_\mu \ll m_\tau$$

Required for  $R_K$

# UV completions for $b \rightarrow s \mu^+ \mu^-$ anomalies

## TREE LEVEL



Leptoquark

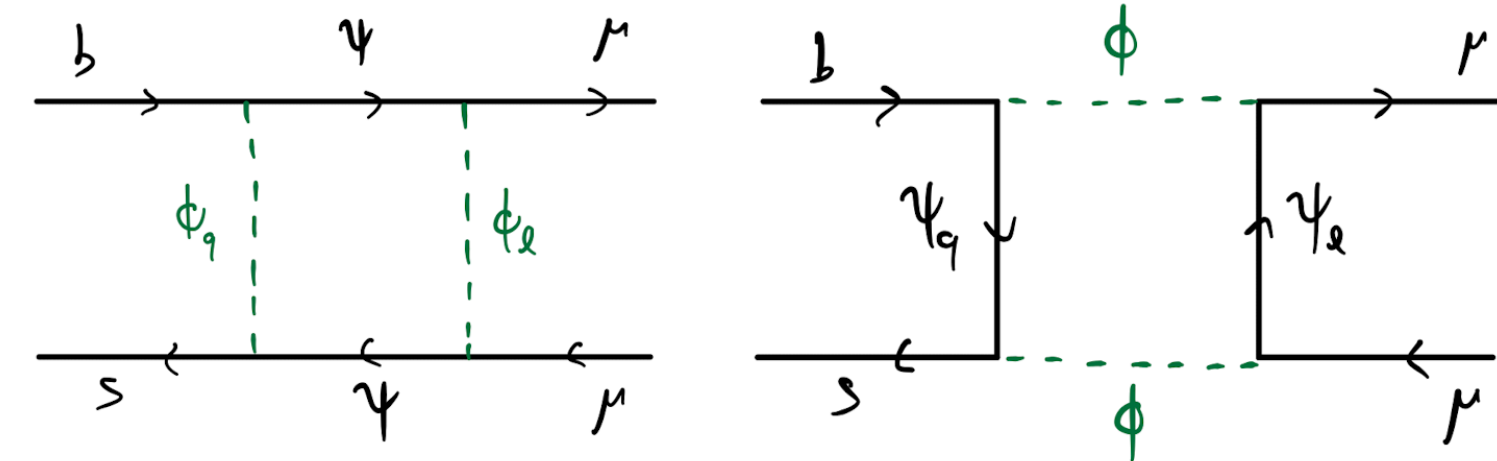
vector  $U_1$  or scalar  $S_3$

$Z'$

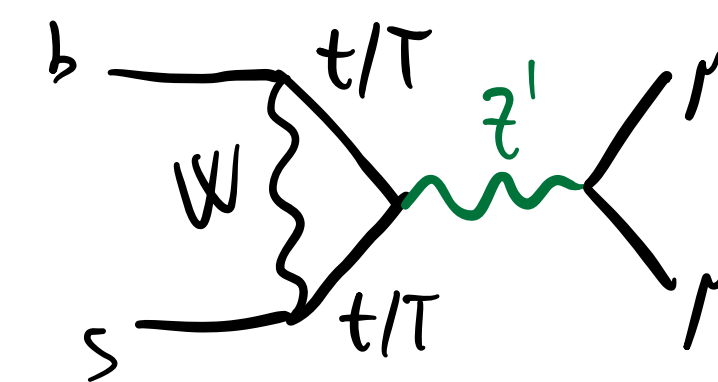
## LOOP LEVEL

### LFU anomalies from boxes

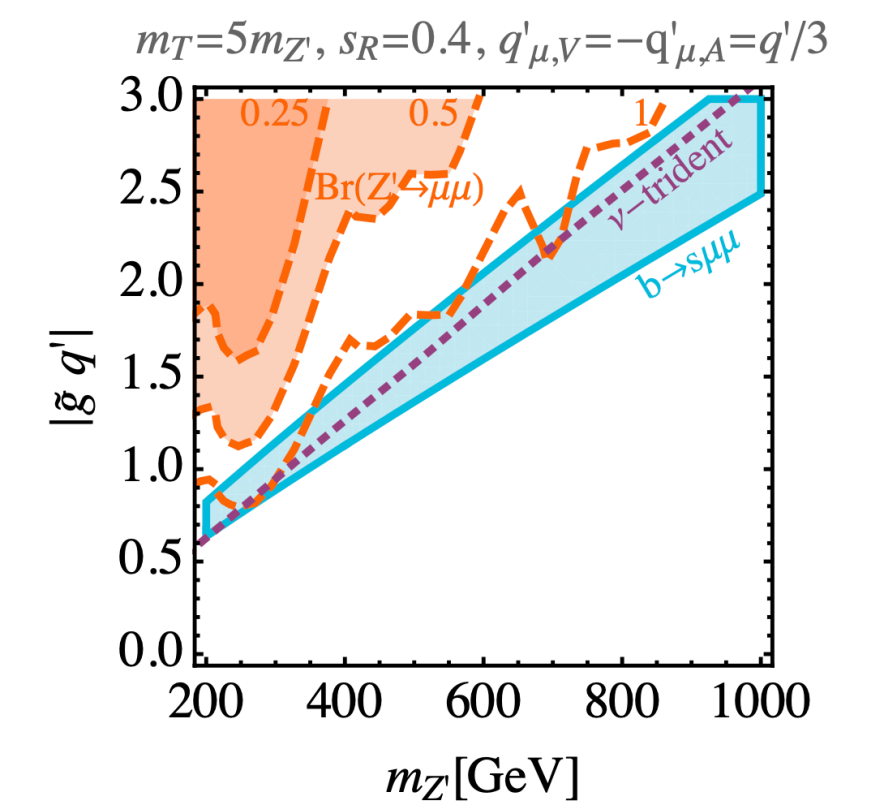
e.g. Arcadi, Calibbi, Fedele, Mescia [2104.03228](#)



Top-philic  $Z'$



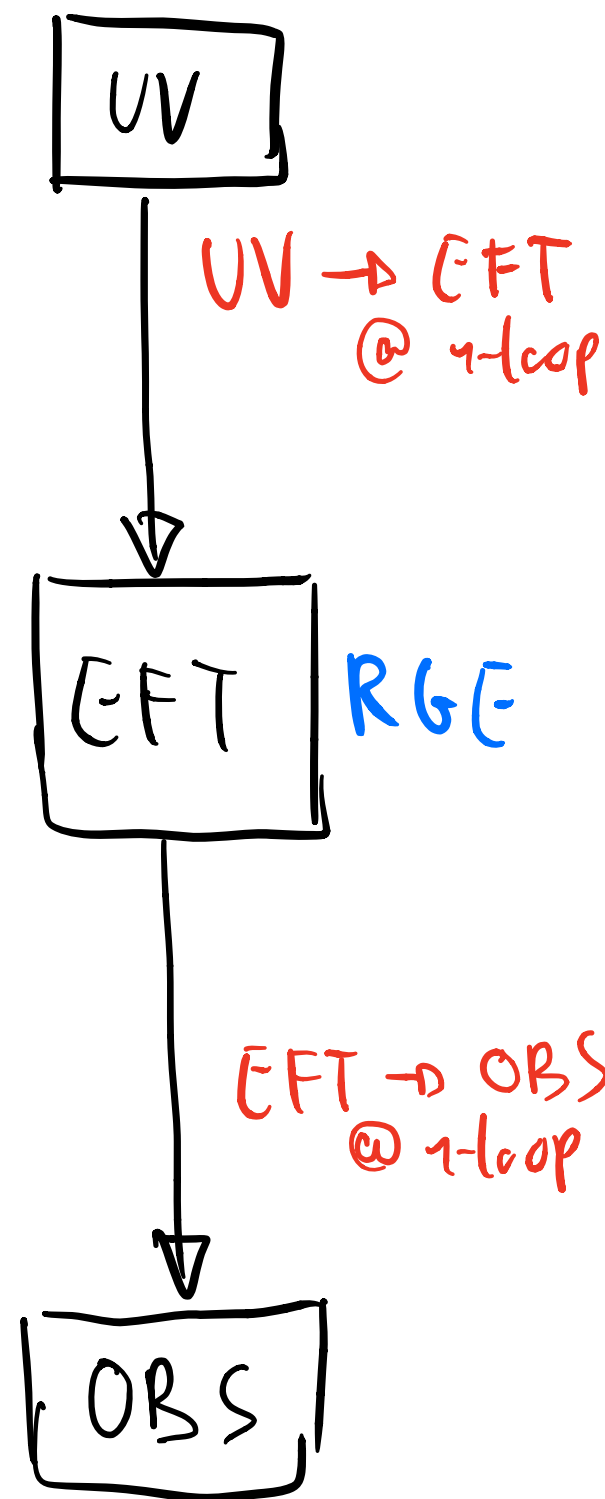
Kamenik, Soreq, Zupan [[1704.06005](#)]





# Complete one-loop matching to SMEFT

V. Gherardi, E. Venturini, D.M. [2003.12525]



## Motivations:

1. **finite terms** (non logs) of loop contributions **are important for several observables:**  
Meson mixing, magnetic dipole moments, Z couplings, LFV leptonic decays, etc..
2. Once the matching is performed, a **large number of observables** can be readily evaluated.
3. It is the first such complete matching for a very rich scenario, many operators are induced.

**Useful as cross-check** for other techniques that aim to do this more automatically.

*MatchMaker* (diagrammatic approach) [Anastasiou, Carmona, Lazopoulos, Santiago, in progress],  
methods based on *Covariant Derivative Expansion* (CDE)  
[Henning, Lu, Murayama '14, Drozd, Ellis, Quevillion, You, Zhang '15, '16, '17, Fuentes-Martin, Portoles, Ruiz-Femenia]

Other necessary contributions:

SMEFT 1-loop RGE

[Alonso, Jenkins, Manohar, Trott '13]

SMEFT > LEFT matching @1-loop

[Dekens, Stoffer 1908.05295]

LEFT 1-loop RGE

[Jenkins, Manohar, Stoffer 1711.05270]

The alternative is to compute on-shell loops for each observable, as in:

Crivellin et al. 1912.04224; Saad 2005.04352;

# “Green’s Basis” of the SMEFT

V. Gherardi, E. Venturini, D.M. [2003.12525]

When off-shell one-loop diagrams are evaluated, also operators outside of the chosen basis (e.g. Warsaw) are generated, which must be reduced to the basis via E.O.M.

The complete **set of independent operators independent upon integration by parts** (but possibly redundant under EOM), is called “**Green's basis**”

$$\mathcal{G} \equiv \langle e_\beta(p_1) \bar{e}_\alpha(p_2) H_b(q_1) H_a^\dagger(q_2) \rangle$$

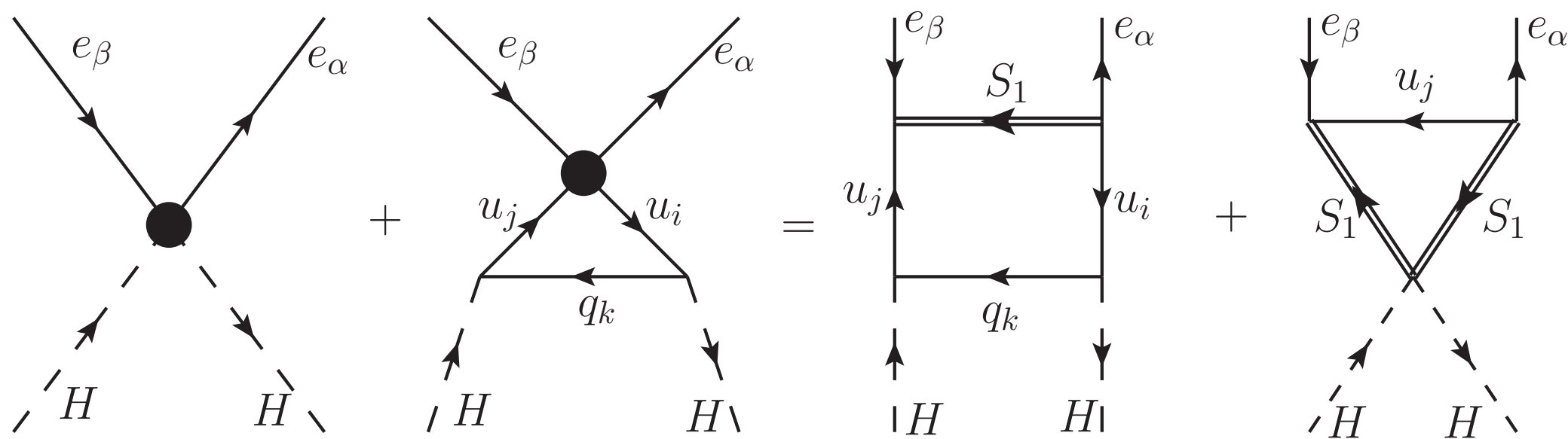


Figure 1: Diagrams for the matching of the  $\langle \bar{e}eH^\dagger H \rangle$  Green function.

Relevant Green’s basis operators:

$$[\mathcal{O}_{He}]_{\alpha\beta} = (\bar{e}_\alpha \gamma^\mu e_\beta) (H^\dagger i \overleftrightarrow{D}_\mu H),$$

$$[\mathcal{O}'_{He}]_{\alpha\beta} = (\bar{e}_\alpha i \overleftrightarrow{D} e_\beta) (H^\dagger H),$$

$$[\mathcal{O}''_{He}]_{\alpha\beta} = (\bar{e}_\alpha \gamma^\mu e_\beta) \partial_\mu (H^\dagger H).$$

Matching conditions in the Green’s basis:

$$[G_{He}(\mu_M)]_{\alpha\beta} = -\frac{N_c (\lambda^{1R\dagger} y_U^T y_U^* \lambda^{1R})_{\alpha\beta}}{32\pi^2 M_1^2} \left( 1 + \log \frac{\mu_M^2}{M_1^2} \right),$$

$$[G'_{He}(\mu_M)]_{\alpha\beta} = -\frac{N_c (\lambda^{1R\dagger} y_U^T y_U^* \lambda^{1R})_{\alpha\beta}}{64\pi^2 M_1^2} + \frac{N_c \lambda_{H1} (\lambda^{1R\dagger} \lambda^{1R})_{\alpha\beta}}{64\pi^2 M_1^2},$$

$$[G''_{He}(\mu_M)]_{\alpha\beta} = 0.$$

The last two must be rotated to the Warsaw basis:

$$(\mathcal{O}'_{He})_{\alpha\beta} \rightarrow (y_E^*)_{\gamma\beta} (\mathcal{O}_{eH})_{\gamma\alpha}^\dagger + (y_E)_{\gamma\alpha} (\mathcal{O}_{eH})_{\gamma\beta}$$

$$[\mathcal{O}''_{He}]_{\alpha\beta} \rightarrow i(y_E^*)_{\gamma\beta} [\mathcal{O}_{eH}]_{\gamma\alpha}^\dagger - i(y_E)_{\gamma\alpha} (\mathcal{O}_{eH})_{\gamma\beta}$$

While the first operators receives contributions also from other ones:

$$[C_{He}]_{\alpha\beta}^{(1)} = -\frac{N_c}{30} g'^4 Y_H Y_e \delta_{\alpha\beta} \left( \frac{3Y_{S_3}^2}{M_3^2} + \frac{Y_{S_1}^2}{M_1^2} \right) + \frac{N_c}{12} \left( 3 \frac{(y_E^\dagger \Lambda_\ell^{(3)} y_E)_{\alpha\beta}}{M_3^2} + \frac{(y_E^\dagger \Lambda_\ell^{(1)} y_E)_{\alpha\beta}}{M_1^2} \right) + \frac{N_c}{3} g'^2 Y_H \left( \frac{8Y_u - Y_{S_1}}{6} + Y_u L_1 \right) \frac{(\Lambda_e)_{\alpha\beta}}{M_1^2} - \frac{N_c}{2} (1 + L_1) \frac{(X_{2U}^{1R})_{\alpha\beta}}{M_1^2}.$$

# “Green’s Basis” of the SMEFT

V. Gherardi, E. Venturini, D.M. [2003.12525]

The **grey ones** are those already present in the **Warsaw basis**

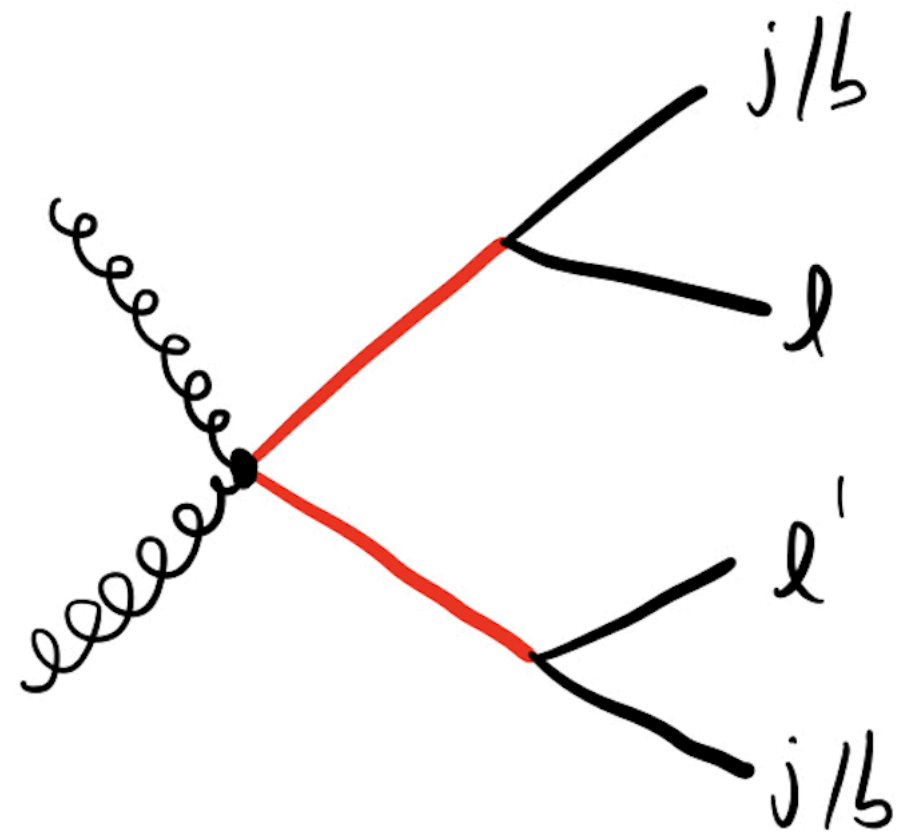
$X^3$		$X^2 H^2$		$H^2 D^4$	
$\mathcal{O}_{3G}$	$f^{ABC} G_{\mu}^{Av} G_{\nu}^{B\rho} G_{\rho}^{C\mu}$	$\mathcal{O}_{HG}$	$G_{\mu\nu}^A G^{A\mu\nu} (H^\dagger H)$	$\mathcal{O}_{DH}$	$(D_\mu D^\mu H)^\dagger (D_\nu D^\nu H)$
$\mathcal{O}_{\widetilde{3G}}$	$f^{ABC} \widetilde{G}_{\mu}^{Av} \widetilde{G}_{\nu}^{B\rho} \widetilde{G}_{\rho}^{C\mu}$	$\mathcal{O}_{H\widetilde{G}}$	$\widetilde{G}_{\mu\nu}^A G^{A\mu\nu} (H^\dagger H)$	$H^4 D^2$	
$\mathcal{O}_{3W}$	$\epsilon^{IJK} W_{\mu}^{I\nu} W_{\nu}^{J\rho} W_{\rho}^{K\mu}$	$\mathcal{O}_{HW}$	$W_{\mu\nu}^I W^{I\mu\nu} (H^\dagger H)$		
$\mathcal{O}_{\widetilde{3W}}$	$\epsilon^{IJK} \widetilde{W}_{\mu}^{I\nu} \widetilde{W}_{\nu}^{J\rho} \widetilde{W}_{\rho}^{K\mu}$	$\mathcal{O}_{H\widetilde{W}}$	$\widetilde{W}_{\mu\nu}^I W^{I\mu\nu} (H^\dagger H)$	$\mathcal{O}_{H\Box}$	$(H^\dagger H)\Box(H^\dagger H)$
$X^2 D^2$		$\mathcal{O}_{HB}$	$B_{\mu\nu} B^{\mu\nu} (H^\dagger H)$	$\mathcal{O}_{HD}$	$(H^\dagger D^\mu H)^\dagger (H^\dagger D_\mu H)$
		$\mathcal{O}_{H\widetilde{B}}$	$\widetilde{B}_{\mu\nu} B^{\mu\nu} (H^\dagger H)$	$\mathcal{O}'_{HD}$	$(H^\dagger H)(D_\mu H)^\dagger (D^\mu H)$
$\mathcal{O}_{2G}$	$-\frac{1}{2}(D_\mu G^{A\mu\nu})(D^\rho G_{\rho\nu}^A)$	$\mathcal{O}_{H\widetilde{B}}$	$\widetilde{B}_{\mu\nu} B^{\mu\nu} (H^\dagger H)$	$\mathcal{O}''_{HD}$	$(H^\dagger H)D_\mu (H^\dagger i \overleftrightarrow{D}^\mu H)$
$\mathcal{O}_{2W}$	$-\frac{1}{2}(D_\mu W^{I\mu\nu})(D^\rho W_{\rho\nu}^I)$	$\mathcal{O}_{HWB}$	$W_{\mu\nu}^I B^{\mu\nu} (H^\dagger \sigma^I H)$	$H^6$	
$\mathcal{O}_{2B}$	$-\frac{1}{2}(\partial_\mu B^{\mu\nu})(\partial^\rho B_{\rho\nu})$	$\mathcal{O}_{H\widetilde{W}B}$	$\widetilde{W}_{\mu\nu}^I B^{\mu\nu} (H^\dagger \sigma^I H)$		
$H^2 X D^2$		$\mathcal{O}_{WDH}$	$D_\nu W^{I\mu\nu} (H^\dagger i \overleftrightarrow{D}^\mu H)$	$\mathcal{O}_H$	$(H^\dagger H)^3$
		$\mathcal{O}_{BDH}$	$\partial_\nu B^{\mu\nu} (H^\dagger i \overleftrightarrow{D}^\mu H)$		

Four-quark		Four-lepton		Semileptonic	
$\mathcal{O}_{qq}^{(1)}$	$(\bar{q}\gamma^\mu q)(\bar{q}\gamma_\mu q)$	$\mathcal{O}_{\ell\ell}$	$(\bar{\ell}\gamma^\mu \ell)(\bar{\ell}\gamma_\mu \ell)$	$\mathcal{O}_{lq}^{(1)}$	$(\bar{\ell}\gamma^\mu \ell)(\bar{q}\gamma_\mu q)$
$\mathcal{O}_{qq}^{(3)}$	$(\bar{q}\gamma^\mu \sigma^I q)(\bar{q}\gamma_\mu \sigma^I q)$	$\mathcal{O}_{ee}$	$(\bar{e}\gamma^\mu e)(\bar{e}\gamma_\mu e)$	$\mathcal{O}_{lq}^{(3)}$	$(\bar{\ell}\gamma^\mu \sigma^I \ell)(\bar{q}\gamma_\mu \sigma^I q)$
$\mathcal{O}_{uu}$	$(\bar{u}\gamma^\mu u)(\bar{u}\gamma_\mu u)$	$\mathcal{O}_{le}$	$(\bar{\ell}\gamma^\mu \ell)(\bar{e}\gamma_\mu e)$	$\mathcal{O}_{eu}$	$(\bar{e}\gamma^\mu e)(\bar{u}\gamma_\mu u)$
$\mathcal{O}_{dd}$	$(\bar{d}\gamma^\mu d)(\bar{d}\gamma_\mu d)$			$\mathcal{O}_{ed}$	$(\bar{e}\gamma^\mu e)(\bar{d}\gamma_\mu d)$
$\mathcal{O}_{ud}^{(1)}$	$(\bar{u}\gamma^\mu u)(\bar{d}\gamma_\mu d)$			$\mathcal{O}_{qe}$	$(\bar{q}\gamma^\mu q)(\bar{e}\gamma_\mu e)$
$\mathcal{O}_{ud}^{(8)}$	$(\bar{u}\gamma^\mu T^A u)(\bar{d}\gamma_\mu T^A d)$			$\mathcal{O}_{lu}$	$(\bar{\ell}\gamma^\mu \ell)(\bar{u}\gamma_\mu u)$
$\mathcal{O}_{qu}^{(1)}$	$(\bar{q}\gamma^\mu q)(\bar{u}\gamma_\mu u)$			$\mathcal{O}_{ld}$	$(\bar{\ell}\gamma^\mu \ell)(\bar{d}\gamma_\mu d)$
$\mathcal{O}_{qu}^{(8)}$	$(\bar{q}\gamma^\mu T^A q)(\bar{u}\gamma_\mu T^A u)$			$\mathcal{O}_{ledq}$	$(\bar{\ell}e)(\bar{d}q)$
$\mathcal{O}_{qd}^{(1)}$	$(\bar{q}\gamma^\mu q)(\bar{d}\gamma_\mu d)$			$\mathcal{O}_{lequ}^{(1)}$	$(\bar{\ell}^r e)\epsilon_{rs}(\bar{q}^s u)$
$\mathcal{O}_{qd}^{(8)}$	$(\bar{q}\gamma^\mu T^A q)(\bar{d}\gamma_\mu T^A d)$			$\mathcal{O}_{lequ}^{(3)}$	$(\bar{\ell}^r \sigma^{\mu\nu} e)\epsilon_{rs}(\bar{q}^s \sigma_{\mu\nu} u)$
$\mathcal{O}_{quqd}^{(1)}$	$(\bar{q}^r u)\epsilon_{rs}(\bar{q}^s d)$				
$\mathcal{O}_{quqd}^{(8)}$	$(\bar{q}^r T^A u)\epsilon_{rs}(\bar{q}^s T^A d)$				

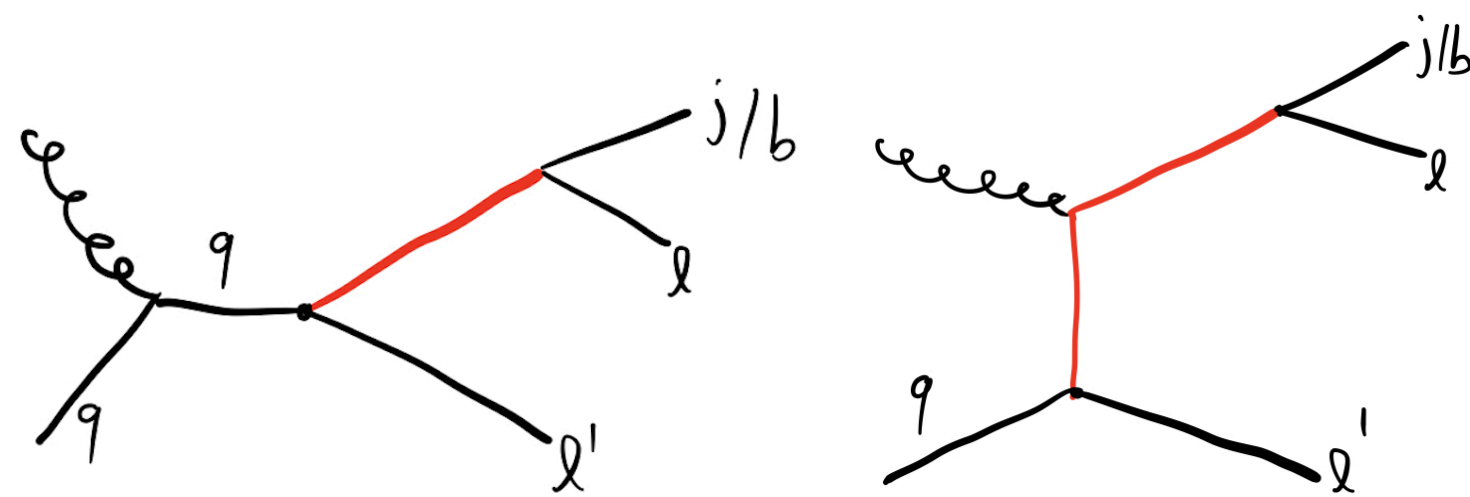
$\psi^2 D^3$		$\psi^2 X D$		$\psi^2 D H^2$	
$\mathcal{O}_{qD}$	$\frac{i}{2}\bar{q}\{D_\mu D^\mu, \not{D}\}q$	$\mathcal{O}_{Gq}$	$(\bar{q}T^A \gamma^\mu q)D^\nu G_{\mu\nu}^A$	$\mathcal{O}_{Hq}^{(1)}$	$(\bar{q}\gamma^\mu q)(H^\dagger i \overleftrightarrow{D}^\mu H)$
$\mathcal{O}_{uD}$	$\frac{i}{2}\bar{u}\{D_\mu D^\mu, \not{D}\}u$	$\mathcal{O}'_{Gq}$	$\frac{1}{2}(\bar{q}T^A \gamma^\mu i \overleftrightarrow{D}^\nu q)G_{\mu\nu}^A$	$\mathcal{O}'_{Hq}^{(1)}$	$(\bar{q}i \overleftrightarrow{D}^\mu q)(H^\dagger H)$
$\mathcal{O}_{dD}$	$\frac{i}{2}\bar{d}\{D_\mu D^\mu, \not{D}\}d$	$\mathcal{O}'_{\widetilde{G}q}$	$\frac{1}{2}(\bar{q}T^A \gamma^\mu i \overleftrightarrow{D}^\nu q)\widetilde{G}_{\mu\nu}^A$	$\mathcal{O}''_{Hq}^{(1)}$	$(\bar{q}\gamma^\mu q)\partial_\mu (H^\dagger H)$
$\mathcal{O}_{\ell D}$	$\frac{i}{2}\bar{\ell}\{D_\mu D^\mu, \not{D}\}\ell$	$\mathcal{O}_{Wq}$	$(\bar{q}\sigma^I \gamma^\mu q)D^\nu W_{\mu\nu}^I$	$\mathcal{O}_{Hq}^{(3)}$	$(\bar{q}\sigma^I \gamma^\mu q)(H^\dagger i \overleftrightarrow{D}^\mu H)$
$\mathcal{O}_{eD}$	$\frac{i}{2}\bar{e}\{D_\mu D^\mu, \not{D}\}e$	$\mathcal{O}'_{Wq}$	$\frac{1}{2}(\bar{q}\sigma^I \gamma^\mu i \overleftrightarrow{D}^\nu q)W_{\mu\nu}^I$	$\mathcal{O}'_{Hq}^{(3)}$	$(\bar{q}i \overleftrightarrow{D}^\mu q)(H^\dagger \sigma^I H)$
$\psi^2 H D^2 + \text{h.c.}$		$\mathcal{O}'_{\widetilde{W}q}$	$\frac{1}{2}(\bar{q}\sigma^I \gamma^\mu i \overleftrightarrow{D}^\nu q)\widetilde{W}_{\mu\nu}^I$	$\mathcal{O}''_{Hq}^{(3)}$	$(\bar{q}\sigma^I \gamma^\mu q)D_\mu (H^\dagger \sigma^I H)$
		$\mathcal{O}_{uHD1}$	$(\bar{q}u)D_\mu D^\mu \widetilde{H}$	$\mathcal{O}_{Bq}$	$(\bar{q}\gamma^\mu q)\partial^\nu B_{\mu\nu}$
$\mathcal{O}_{uHD2}$	$(\bar{q}i\sigma_{\mu\nu} D^\mu u)D^\nu \widetilde{H}$	$\mathcal{O}'_{Bq}$	$\frac{1}{2}(\bar{q}\gamma^\mu i \overleftrightarrow{D}^\nu q)B_{\mu\nu}$	$\mathcal{O}'_{Hu}$	$(\bar{u}i \overleftrightarrow{D}^\mu u)(H^\dagger H)$
$\mathcal{O}_{uHD3}$	$(\bar{q}D_\mu D^\mu u)\widetilde{H}$	$\mathcal{O}'_{\widetilde{B}q}$	$\frac{1}{2}(\bar{q}\gamma^\mu i \overleftrightarrow{D}^\nu q)\widetilde{B}_{\mu\nu}$	$\mathcal{O}''_{Hu}$	$(\bar{u}\gamma^\mu u)\partial_\mu (H^\dagger H)$
$\mathcal{O}_{uHD4}$	$(\bar{q}D_\mu u)D^\mu \widetilde{H}$	$\mathcal{O}_{Gu}$	$(\bar{u}T^A \gamma^\mu u)D^\nu G_{\mu\nu}^A$	$\mathcal{O}_{Hd}$	$(\bar{d}\gamma^\mu d)(H^\dagger i \overleftrightarrow{D}^\mu H)$
$\mathcal{O}_{dHD1}$	$(\bar{q}d)D_\mu D^\mu H$	$\mathcal{O}'_{Gu}$	$\frac{1}{2}(\bar{u}T^A \gamma^\mu i \overleftrightarrow{D}^\nu u)G_{\mu\nu}^A$	$\mathcal{O}'_{Hd}$	$(\bar{d}i \overleftrightarrow{D}^\mu d)(H^\dagger H)$
$\mathcal{O}_{dHD2}$	$(\bar{q}i\sigma_{\mu\nu} D^\mu d)D^\nu H$	$\mathcal{O}'_{\widetilde{G}u}$	$\frac{1}{2}(\bar{u}T^A \gamma^\mu i \overleftrightarrow{D}^\nu u)\widetilde{G}_{\mu\nu}^A$	$\mathcal{O}''_{Hd}$	$(\bar{d}\gamma^\mu d)\partial_\mu (H^\dagger H)$
$\mathcal{O}_{dHD3}$	$(\bar{q}D_\mu D^\mu d)H$	$\mathcal{O}_{Bu}$	$(\bar{u}\gamma^\mu u)\partial^\nu B_{\mu\nu}$	$\mathcal{O}_{Hud}$	$(\bar{u}\gamma^\mu d)(\widetilde{H}^\dagger i \overleftrightarrow{D}^\mu H)$
$\mathcal{O}_{dHD4}$	$(\bar{q}D_\mu d)D^\mu H$	$\mathcal{O}'_{Bu}$	$\frac{1}{2}(\bar{u}\gamma^\mu i \overleftrightarrow{D}^\nu u)B_{\mu\nu}$	$\mathcal{O}_{H\ell}^{(1)}$	$(\bar{\ell}\gamma^\mu \ell)(H^\dagger i \overleftrightarrow{D}^\mu H)$
$\mathcal{O}_{eHD1}$	$(\bar{\ell}e)D_\mu D^\mu H$	$\mathcal{O}'_{\widetilde{B}u}$	$\frac{1}{2}(\bar{u}\gamma^\mu i \overleftrightarrow{D}^\nu u)\widetilde{B}_{\mu\nu}$	$\mathcal{O}'_{H\ell}^{(1)}$	$(\bar{\ell}i \overleftrightarrow{D}^\mu \ell)(H^\dagger H)$
$\mathcal{O}_{eHD2}$	$(\bar{\ell}i\sigma_{\mu\nu} D^\mu e)D^\nu H$	$\mathcal{O}_{Gd}$	$(\bar{d}T^A \gamma^\mu d)D^\nu G_{\mu\nu}^A$	$\mathcal{O}''_{H\ell}^{(1)}$	$(\bar{\ell}\gamma^\mu \ell)\partial_\mu (H^\dagger H)$
$\mathcal{O}_{eHD3}$	$(\bar{\ell}D_\mu D^\mu e)H$	$\mathcal{O}'_{Gd}$	$\frac{1}{2}(\bar{d}T^A \gamma^\mu i \overleftrightarrow{D}^\nu d)G_{\mu\nu}^A$	$\mathcal{O}_{H\ell}^{(3)}$	$(\bar{\ell}\sigma^I \gamma^\mu \ell)(H^\dagger i \overleftrightarrow{D}^\mu H)$
$\mathcal{O}_{eHD4}$	$(\bar{\ell}D_\mu e)D^\mu H$	$\mathcal{O}'_{\widetilde{G}d}$	$\frac{1}{2}(\bar{d}T^A \gamma^\mu i \overleftrightarrow{D}^\nu d)\widetilde{G}_{\mu\nu}^A$	$\mathcal{O}'_{H\ell}^{(3)}$	$(\bar{\ell}i \overleftrightarrow{D}^\mu \ell)(H^\dagger \sigma^I H)$
$\psi^2 X H + \text{h.c.}$		$\mathcal{O}_{Bd}$	$(\bar{d}\gamma^\mu d)\partial^\nu B_{\mu\nu}$	$\mathcal{O}''_{H\ell}^{(3)}$	$(\bar{\ell}\sigma^I \gamma^\mu \ell)D_\mu (H^\dagger \sigma^I H)$
		$\mathcal{O}_{uG}$	$(\bar{q}T^A \sigma^{\mu\nu} u)\widetilde{H}G_{\mu\nu}^A$	$\mathcal{O}_{He}$	$(\bar{e}\gamma^\mu e)(H^\dagger i \overleftrightarrow{D}^\mu H)$
$\mathcal{O}_{uW}$	$(\bar{q}\sigma^{\mu\nu} u)\sigma^I \widetilde{H}W_{\mu\nu}^I$	$\mathcal{O}'_{Bd}$	$\frac{1}{2}(\bar{d}\gamma^\mu i \overleftrightarrow{D}^\nu d)B_{\mu\nu}$	$\mathcal{O}'_{He}$	$(\bar{e}i \overleftrightarrow{D}^\mu e)(H^\dagger H)$
$\mathcal{O}_{uB}$	$(\bar{q}\sigma^{\mu\nu} u)\widetilde{H}B_{\mu\nu}$	$\mathcal{O}'_{\widetilde{B}d}$	$\frac{1}{2}(\bar{d}\gamma^\mu i \overleftrightarrow{D}^\nu d)\widetilde{B}_{\mu\nu}$	$\mathcal{O}''_{He}$	$(\bar{e}\gamma^\mu e)\partial_\mu (H^\dagger H)$
$\mathcal{O}_{dG}$	$(\bar{q}T^A \sigma^{\mu\nu} d)HG_{\mu\nu}^A$	$\mathcal{O}_{W\ell}$	$(\bar{\ell}\sigma^I \gamma^\mu \ell)D^\nu W_{\mu\nu}^I$	$\psi^2 H^3 + \text{h.c.}$	
$\mathcal{O}_{dW}$	$(\bar{q}\sigma^{\mu\nu} d)\sigma^I HW_{\mu\nu}^I$	$\mathcal{O}'_{W\ell}$	$\frac{1}{2}(\bar{\ell}\sigma^I \gamma^\mu i \overleftrightarrow{D}^\nu \ell)W_{\mu\nu}^I$		
$\mathcal{O}_{dB}$	$(\bar{q}\sigma^{\mu\nu} d)HB_{\mu\nu}$	$\mathcal{O}'_{\widetilde{W}\ell}$	$\frac{1}{2}(\bar{\ell}\sigma^I \gamma^\mu i \overleftrightarrow{D}^\nu \ell)\widetilde{W}_{\mu\nu}^I$	$\mathcal{O}_{uH}$	$(H^\dagger H)\bar{q}\widetilde{H}u$
$\mathcal{O}_{eW}$	$(\bar{\ell}\sigma^{\mu\nu} e)\sigma^I HW_{\mu\nu}^I$	$\mathcal{O}_{Bl}$	$(\bar{\ell}\gamma^\mu \ell)\partial^\nu B_{\mu\nu}$	$\mathcal{O}_{dH}$	$(H^\dagger H)\bar{q}Hd$
$\mathcal{O}_{eB}$	$(\bar{\ell}\sigma^{\mu\nu} e)HB_{\mu\nu}$	$\mathcal{O}'_{Bl}$	$\frac{1}{2}(\bar{\ell}\gamma^\mu i \overleftrightarrow{D}^\nu \ell)B_{\mu\nu}$	$\mathcal{O}_{eH}$	$(H^\dagger H)\bar{\ell}He$
		$\mathcal{O}'_{\widetilde{B}\ell}$	$\frac{1}{2}(\bar{\ell}\gamma^\mu i \overleftrightarrow{D}^\nu \ell)\widetilde{B}_{\mu\nu}$		
		$\mathcal{O}_{Be}$	$(\bar{e}\gamma^\mu e)\partial^\nu B_{\mu\nu}$		
		$\mathcal{O}'_{Be}$	$\frac{1}{2}(\bar{e}\gamma^\mu i \overleftrightarrow{D}^\nu e)B_{\mu\nu}$		
		$\mathcal{O}'_{\widetilde{B}e}$	$\frac{1}{2}(\bar{e}\gamma^\mu i \overleftrightarrow{D}^\nu e)\widetilde{B}_{\mu\nu}$		

# The Threefold Way of LQ Searches at LHC

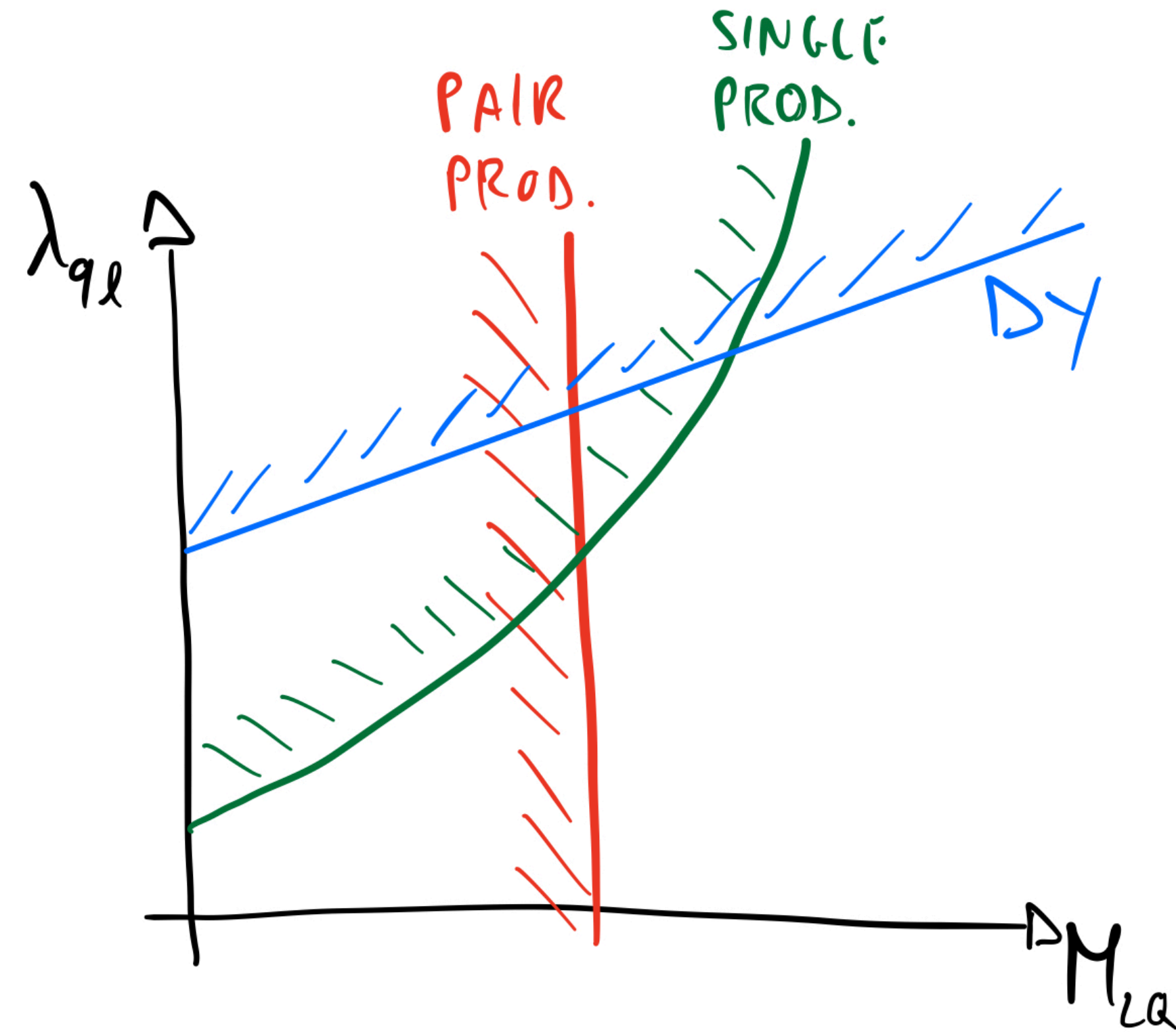
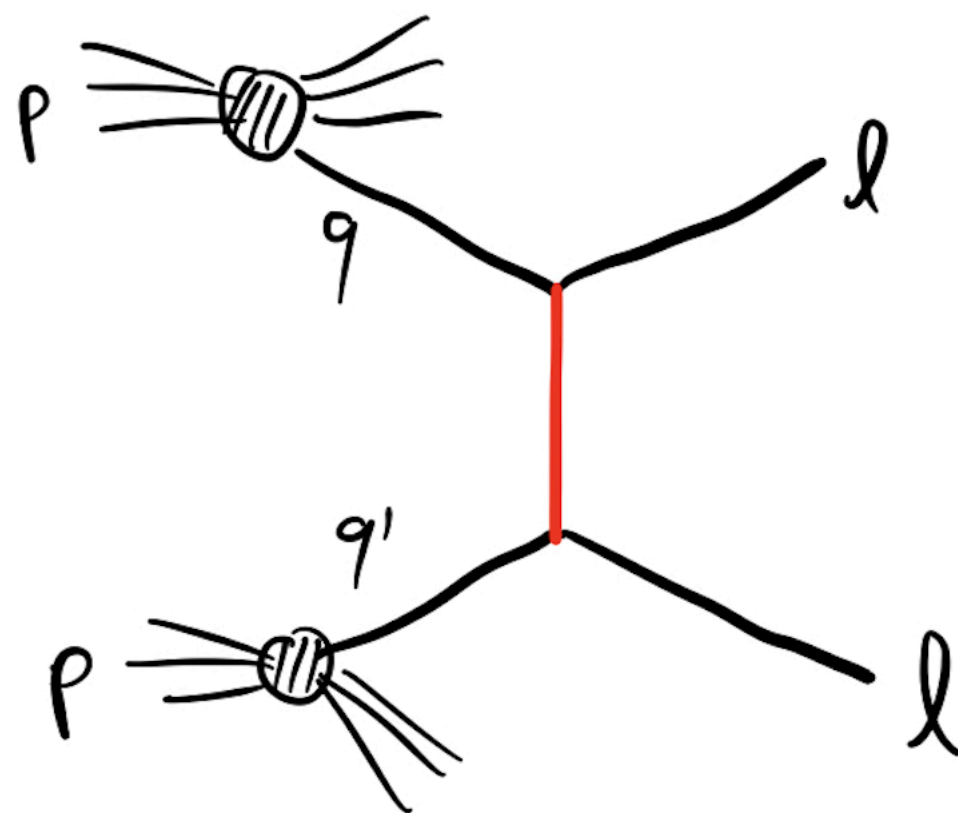
QCD  
pair-production



single-production



High- $p_T$  Drell-Yan



[Diaz, Schmaltz, Zhong 1706.05033, 1810.10017; Dorsner, Greljo 1801.07641]

**In order to cover all couplings it is important to consider all combinations of different lepton & quark combinations in final state!**

# Leptoquark searches at CMS and ATLAS

## CMS

### Leptoquarks

scalar LQ (pair prod.), coupling to 1 <sup>st</sup> gen. fermions, $\beta = 1$	<1.44	1811.01197 ( $2e + 2j$ )
scalar LQ (pair prod.), coupling to 1 <sup>st</sup> gen. fermions, $\beta = 0.5$	<1.27	1811.01197 ( $2e + 2j; e + 2j + E_T^{\text{miss}}$ )
scalar LQ (pair prod.), coupling to 2 <sup>nd</sup> gen. fermions, $\beta = 1$	<1.53	1808.05082 ( $2\mu + 2j$ )
scalar LQ (pair prod.), coupling to 2 <sup>nd</sup> gen. fermions, $\beta = 1$	0.8–1.5	1811.10151 ( $1\mu + 1j + E_T^{\text{miss}}$ )
scalar LQ (pair prod.), coupling to 2 <sup>nd</sup> gen. fermions, $\beta = 0.5$	<1.29	1808.05082 ( $2\mu + 2j; \mu + 2j + E_T^{\text{miss}}$ )
scalar LQ (pair prod.), coupling to 3 <sup>rd</sup> gen. fermions, $\beta = 1$	<1.02	1811.00806 ( $2\tau + 2j$ )
scalar LQ (single prod.), coup. to 3 <sup>rd</sup> gen. ferm., $\beta = 1, \lambda = 1$	<0.74	1806.03472 ( $2\tau + b$ )

CMS  $\tau\tau bb$  [1703.03995](#), [1811.00806](#)  
 CMS  $\tau\tau\tau$  [1803.02864](#)  
 CMS  $\mu\mu jj$  &  $\mu\nu jj$  [CMS PAS EXO-17-003](#)  
 CMS  $\mu\mu tt$  [1809.05558](#)  
 CMS  $w\nu+(jj, bb, tt)$  [1805.10228](#)

ATLAS  $lljj, l\nu jj$  [1902.00377](#)  
 ATLAS  $lljj$  [2006.05872](#)  
 ATLAS  $tt(ee, \mu\mu)$  [2010.02098](#)  
 ATLAS  $LQ \rightarrow (tv, b\tau)$  [1902.08103](#)  
 ATLAS  $LQ \rightarrow (bv, t\tau)$  [2101.12527](#)  
 ATLAS  $tt\tau\tau$  [2101.11582](#)